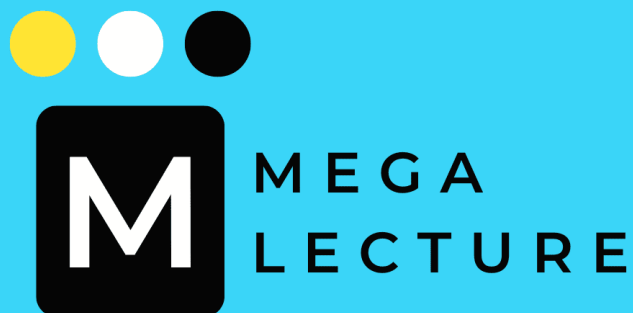




IB DP PHYSICS

Theme A · Space, Time and Motion

MARK SCHEME

A.1 Kinematics · A.2 Forces and Momentum · A.3 Work, Energy and Power
A.4 Rigid Body Mechanics (HL) · A.5 Relativity (HL)

Standard and Higher Level · Syllabus 2025

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Section A — Multiple Choice: Answer Key (15 marks)

1. Answer: **B** — $v = u - gt = 15 - (9.8 \cdot 2) = -4.6 \text{ m s}^{-1}$ (i.e. 4.6 m s^{-1} downward).
2. Answer: **B** — Instantaneous velocity is the gradient of the tangent to an $s-t$ graph; area under a $v-t$ graph would instead give displacement.
3. Answer: **C** — $v^2 = u^2 + 2as \Rightarrow a = (22^2 - 4.0^2)/(2 \cdot 130) = 468/260 = 1.8 \text{ m s}^{-2}$.
4. Answer: **B** — $a = F/m = 15/5.0 = 3.0 \text{ m s}^{-2}$ (Newton's second law).
5. Answer: **B** — Third-law pairs act on different objects, are the same type of interaction, and are equal in magnitude but opposite in direction.
6. Answer: **B** — Momentum conservation: $(2.0 \cdot 3.0) = (2.0 + 4.0)v \Rightarrow v = 6.0/6.0 = 1.0 \text{ m s}^{-1}$.
7. Answer: **C** — $P = Fv = mgv = 500 \cdot 9.8 \cdot 2.0 = 9800 \text{ W} = 9.8 \text{ kW}$.
8. Answer: **B** — Momentum, total energy, and mass are always conserved in an isolated system; kinetic energy is conserved only in elastic collisions.
9. Answer: **B** — $E_p = \frac{1}{2}kx^2 = 0.5 \cdot 200 \cdot 0.15^2 = 2.25 \text{ J}$.
10. Answer: **B** — $\tau = Fr = 20 \cdot 0.30 = 6.0 \text{ N m}$.
11. Answer: **C** — $I = \frac{1}{2}mr^2 = 0.4 \cdot 3.0 \cdot 0.20^2 = 0.048 \text{ kg m}^2$.
12. Answer: **A** — This is the rotational analogue of conservation of linear momentum: L is conserved when net external torque = 0.
13. Answer: **C** — $\gamma = 1/\sqrt{1 - 0.60^2} = 1/\sqrt{0.64} = 1/0.80 = 1.25$.
14. Answer: **B** — Time dilation: a moving clock is observed to run slow compared to a clock at rest in the observer's frame.
15. Answer: **B** — Proper length L_0 is measured in the frame in which the object is at rest; any other observer measures a shorter, contracted length.

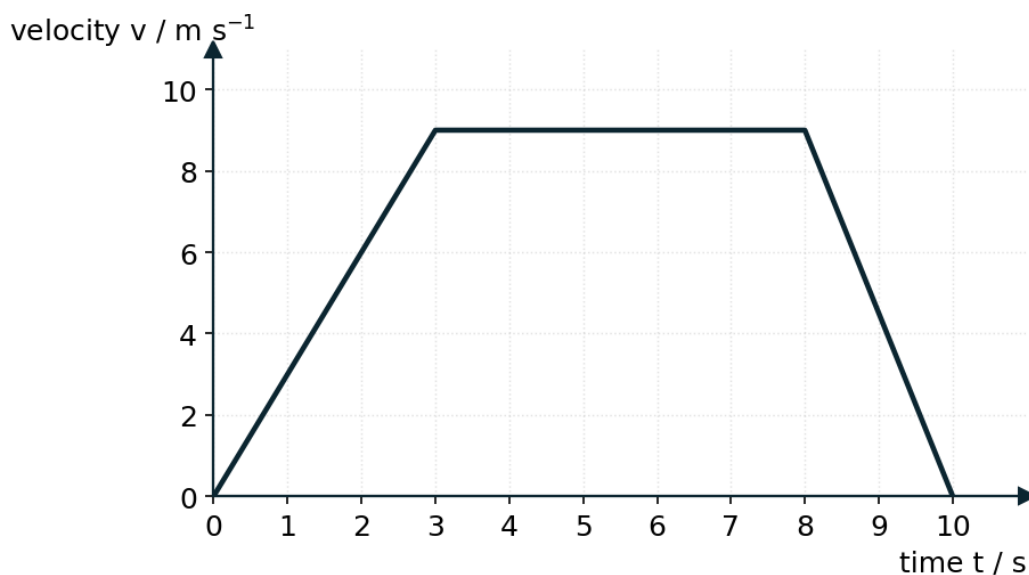
Section B — Structured Questions: Worked Solutions (70 marks)

Mark-scheme notation: M = method mark, A = accuracy mark (dependent on the preceding M mark), R = reasoning mark.

A.1 Kinematics

Question 1 [7 marks]

A sprinter accelerates uniformly from rest to a maximum speed, holds that speed, then decelerates uniformly to rest. The graph below shows her velocity during the run.



Velocity–time graph for the sprint (values on the axes are the given data for this question).

(a) Calculate the sprinter's acceleration during the first 3.0 s. [2]

$$a = \Delta v / \Delta t = 9.0 / 3.0 = \mathbf{3.0 \text{ m s}^{-2}}.$$

M1 A1

(b) Show that the total distance covered during the 10 s run is about 68 m. [3]

$$\text{Distance} = \text{area under the graph} = \frac{1}{2}(3.0)(9.0) + (9.0)(5.0) + \frac{1}{2}(2.0)(9.0) = 13.5 + 45 + 9.0 = \mathbf{67.5 \text{ m}} \approx 68 \text{ m.}$$

M1 M1 A1

(c) Calculate her average velocity for the whole 10 s run. [2]

$$v_{\text{avg}} = \text{total distance} / \text{total time} = 67.5 / 10 = \mathbf{6.75 \text{ m s}^{-1}}.$$

M1 A1

Question 2 [7 marks]

A stone is kicked horizontally at 12 m s^{-1} from the top of a cliff of height 20 m. Air resistance is negligible; take $g = 9.8 \text{ m s}^{-2}$.

(a) Calculate the time taken for the stone to reach the ground. [2]

$$h = \frac{1}{2}gt^2 \Rightarrow t = \sqrt{(2h/g)} = \sqrt{(2 \cdot 20/9.8)} = \mathbf{2.02 \text{ s.}}$$

M1 A1

(b) Calculate the horizontal distance travelled before landing. [2]

$$x = u_x t = 12 \cdot 2.02 = \mathbf{24.2 \text{ m.}}$$

M1 A1

(c) Calculate the stone's speed as it hits the ground.

[3]

$$v_y = gt = 9.8 \cdot 2.02 = 19.8 \text{ m s}^{-1}$$

M1 M1 A1

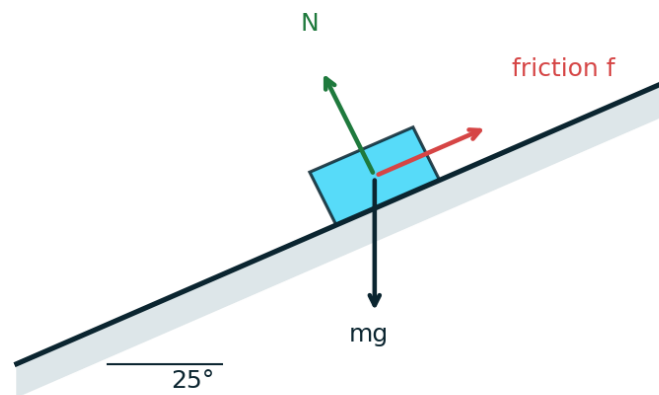
$$v = \sqrt{v_x^2 + v_y^2} = \sqrt{12^2 + 19.8^2} = \mathbf{23.2 \text{ m s}^{-1}}.$$

A.2 Forces and Momentum

Question 3 [7 marks]

A 12 kg box rests on a rough incline at 25° to the horizontal, as shown. The coefficient of static friction between the box and the incline is 0.40. Take $g = 9.8 \text{ m s}^{-2}$.

12 kg box on a rough incline ($\mu = 0.40$)



Forces on the box: weight mg , normal force N , and friction f acting up the slope.

(a) Calculate the component of the box's weight acting along the incline (down the slope).

[2]

$$mg \sin \theta = 12 \cdot 9.8 \cdot \sin 25^\circ = \mathbf{49.7 \text{ N}}.$$

M1 A1

(b) Calculate the normal force acting on the box.

[2]

$$N = mg \cos \theta = 12 \cdot 9.8 \cdot \cos 25^\circ = \mathbf{106.6 \text{ N}}.$$

M1 A1

(c) Determine, showing your reasoning, whether the box remains stationary or begins to slide.

[3]

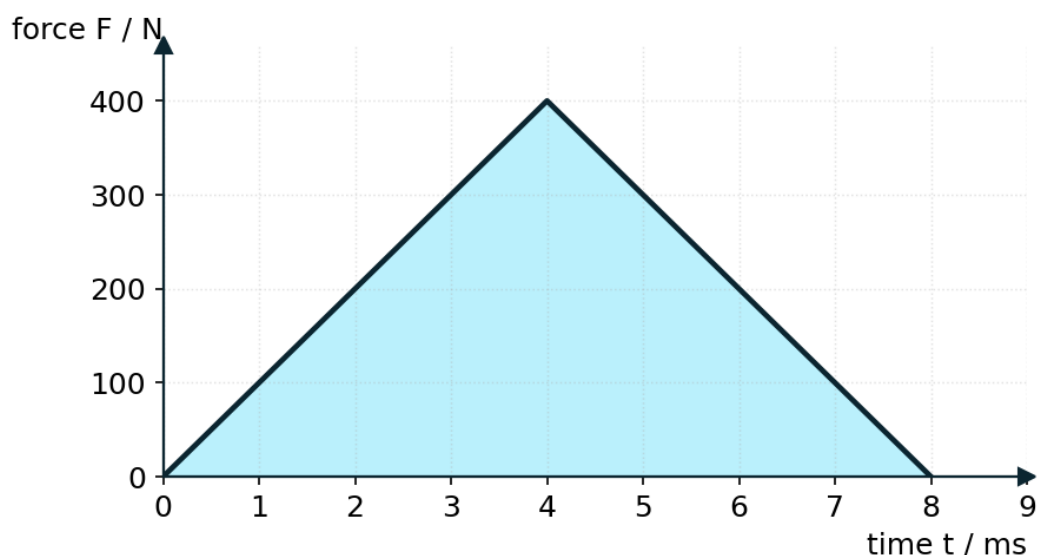
$$\text{Maximum available friction} = \mu N = 0.40 \cdot 106.6 = 42.6 \text{ N}.$$

M1 A1 R1

Since the down-slope component (49.7 N) is **greater than** the maximum friction (42.6 N), the box **slides**.

Question 4 [6 marks]

A 0.50 kg ball is struck by a bat. The graph shows how the force on the ball varies during the 8.0 ms contact time.



Force–time graph for the bat–ball impact (given data).

- (a) Calculate the impulse delivered to the ball during the impact. [2]

Impulse = area under graph = $\frac{1}{2}(400)(8.0 \times 10^{-3}) = 1.60 \text{ N s}$.

M1 A1

- (b) Calculate the change in the ball's velocity, assuming it was at rest just before impact. [2]

$\Delta v = J/m = 1.60/0.50 = 3.2 \text{ m s}^{-1}$.

M1 A1

- (c) Calculate the average force exerted on the ball during the impact. [2]

$F_{\text{avg}} = J/\Delta t = 1.60/(8.0 \times 10^{-3}) = 200 \text{ N}$.

M1 A1

A.3 Work, Energy and Power

Question 5 [8 marks]

A skier of mass 65 kg starts from rest at the top of a slope of vertical height 40 m. Take $g = 9.8 \text{ m s}^{-2}$.

- (a) Calculate the loss in gravitational potential energy as the skier descends to the bottom. [2]

$E_p = mgh = 65 \cdot 9.8 \cdot 40 = 25480 \text{ J}$ ($\approx 2.5 \times 10^4 \text{ J}$).

M1 A1

- (b) Assuming no energy is lost to friction or air resistance, calculate the skier's speed at the bottom of the slope. [3]

Energy conservation: $\frac{1}{2}mv^2 = mgh \Rightarrow v = \sqrt{2gh} = \sqrt{2 \cdot 9.8 \cdot 40} = 28.0 \text{ m s}^{-1}$.

M1 M1 A1

- (c) In reality the skier's speed at the bottom is measured to be 24 m s^{-1} . Calculate the energy transferred to thermal energy by friction and air resistance. [3]

$KE_{\text{actual}} = \frac{1}{2}mv^2 = 0.5 \cdot 65 \cdot 24^2 = 18720 \text{ J}$.

M1 A1 A1

Energy lost = $E_p - KE_{\text{actual}} = 25480 - 18720 = 6760 \text{ J}$ ($\approx 6.8 \times 10^3 \text{ J}$).

Question 6 [6 marks]

An electric motor lifts a 15 kg load a vertical height of 6.0 m in 8.0 s, moving at constant speed. The electrical energy supplied to the motor during this time is 1500 J. Take $g = 9.8 \text{ m s}^{-2}$.

(a) Calculate the useful work done in lifting the load. [2]

$$W = mgh = 15 \cdot 9.8 \cdot 6.0 = \mathbf{882 \text{ J.}}$$
 M1 A1

(b) Calculate the efficiency of the motor. [2]

$$\text{efficiency} = (\text{useful output} / \text{total input}) \times 100\% = (882/1500) \times 100 = \mathbf{58.8\%}.$$
 M1 A1

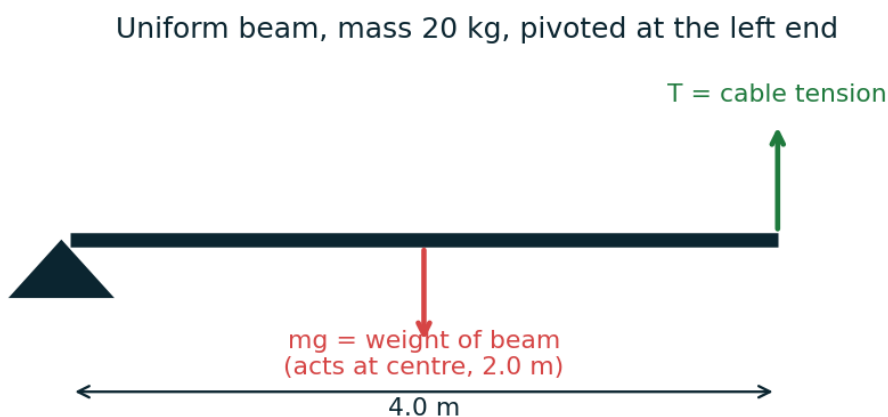
(c) Calculate the useful power output of the motor. [2]

$$P = W/t = 882/8.0 = \mathbf{110 \text{ W.}}$$
 M1 A1

A.4 Rigid Body Mechanics (HL)

Question 7 [8 marks]

A uniform beam of length 4.0 m and mass 20 kg is pivoted (hinged) at one end and held horizontal by a vertical cable attached at its far end, as shown. Take $g = 9.8 \text{ m s}^{-2}$.



Uniform beam in rotational equilibrium about the pivot.

(a) Calculate the torque produced about the pivot by the beam's own weight. [2]

$$\text{Weight acts at the centre of mass, 2.0 m from the pivot: } \tau = mg \cdot 2.0 = 20 \cdot 9.8 \cdot 2.0 = \mathbf{392 \text{ N m.}}$$
 M1 A1

(b) Hence calculate the tension T in the cable, which acts vertically at the far end of the beam, 4.0 m from the pivot. [3]

$$\text{For rotational equilibrium: } T \cdot 4.0 = 392 \Rightarrow T = 392/4.0 = \mathbf{98 \text{ N.}}$$
 M1 M1 A1

(c) An additional 10 kg mass is now hung from the far end of the beam. Calculate the new tension in the cable. [3]

$$\text{Extra torque} = (10 \cdot 9.8) \cdot 4.0 = 392 \text{ N m.}$$
 M1 M1 A1

$$\text{Total torque} = 392 + 392 = 784 \text{ N m.}$$

$$T_{\text{new}} = 784/4.0 = \mathbf{196 \text{ N.}}$$

Question 8 [8 marks]

A solid cylinder of mass 2.0 kg and radius 0.10 m ($I = \frac{1}{2}mr^2$ for a solid cylinder about its central axis) rolls without slipping from rest down a slope, reaching the bottom with a linear speed of 4.0 m s^{-1} . Take $g = 9.8 \text{ m s}^{-2}$.

(a) Calculate the cylinder's angular velocity at the bottom of the slope. [2]

$$\omega = v/r = 4.0/0.10 = \mathbf{40 \text{ rad s}^{-1}}.$$

M1 A1

(b) Show that the cylinder's total kinetic energy at the bottom is about 24 J. [3]

$$I = \frac{1}{2}mr^2 = 0.5 \cdot 2.0 \cdot 0.10^2 = 0.010 \text{ kg m}^2.$$

M1 M1 A1

$$KE_{\text{trans}} = \frac{1}{2}mv^2 = 16 \text{ J}; KE_{\text{rot}} = \frac{1}{2}I\omega^2 = 8 \text{ J}.$$

$$KE_{\text{total}} = 16 + 8 = \mathbf{24 \text{ J}}.$$

(c) Assuming no energy is lost to friction, calculate the vertical height of the slope. [3]

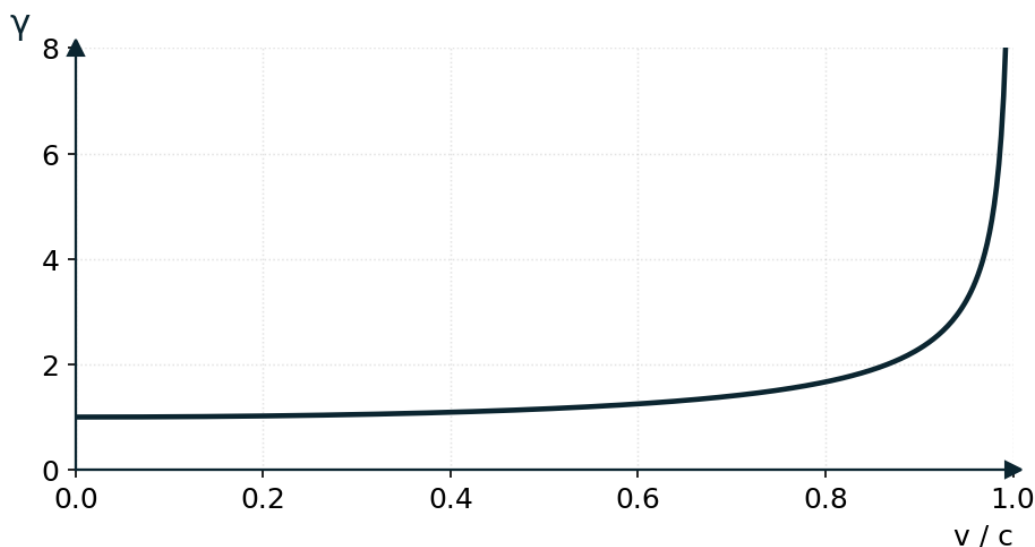
$$\text{Energy conservation: } mgh = KE_{\text{total}} \Rightarrow h = 24/(2.0 \cdot 9.8) = \mathbf{1.22 \text{ m}}.$$

M1 M1 A1

A.5 Relativity (HL)

Question 9 [7 marks]

A muon is created in the upper atmosphere and travels toward the Earth's surface at $v = 0.98c$. In the muon's own rest frame, its (proper) lifetime is $2.2 \mu\text{s}$. The graph below shows how the Lorentz factor γ varies with speed v/c .



γ as a function of v/c (reference curve — read off approximately, then verify by calculation in part (a)).

(a) Calculate the Lorentz factor γ for the muon. [2]

$$\gamma = 1/\sqrt{1 - (v/c)^2} = 1/\sqrt{1 - 0.98^2} = \mathbf{5.03}.$$

M1 A1

(b) Calculate the muon's lifetime as measured by an observer on the ground. [2]

$$\Delta t = \gamma \Delta t_0 = 5.03 \cdot 2.2 = \mathbf{11.1 \mu\text{s}}.$$

M1 A1

(c) Using this dilated lifetime, calculate the distance (in the Earth's frame) that the muon travels before it decays. [3]

$$d = v\Delta t = 0.98 \cdot (3.0 \times 10^8) \cdot (11.1 \times 10^{-6}) = \mathbf{3250 \text{ m}} (\approx 3.25 \text{ km}).$$

M1 M1 A1

Question 10 [6 marks]

A spacecraft has a proper length of 120 m. It travels past the Earth at $v = 0.80c$.

(a) Calculate the Lorentz factor γ for the spacecraft's motion.

[2]

$$\gamma = 1/\sqrt{1 - 0.80^2} = \mathbf{1.667}.$$

M1 A1

(b) Calculate the spacecraft's length as measured by an observer on Earth.

[2]

$$L = L_0/\gamma = 120/1.667 = \mathbf{72.0 \text{ m}}.$$

M1 A1

(c) The crew measure a journey time of 100 s using the spacecraft's own clock. Calculate the time for the same journey as measured by an observer on Earth.

[2]

$$\Delta t_{\text{Earth}} = \gamma \Delta t_0 = 1.667 \cdot 100 = \mathbf{166.7 \text{ s}}.$$

M1 A1