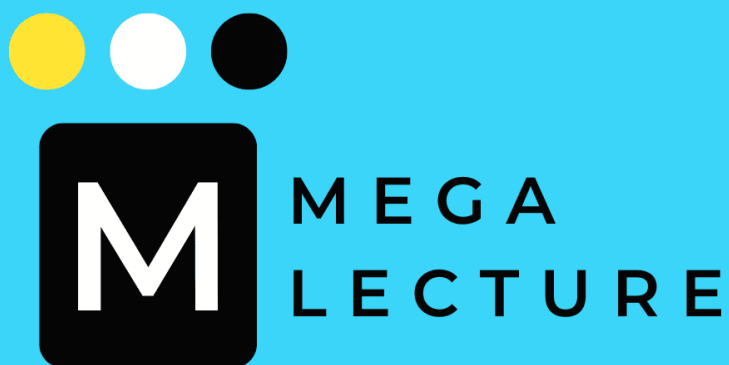




# IB DP CHEMISTRY

**Reactivity 1: What Drives Chemical Reactions?**

## **Reactivity 1.2 Energy Cycles in Reactions**

Revision Notes · Standard and Higher Level

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## What the syllabus requires

Reactivity 1.2 asks a simple question with powerful consequences: if we cannot measure an enthalpy change directly, can we *calculate* it from data we already have? The answer is yes, because enthalpy is a state function. Use this checklist before the exam.

| Understanding             | You should be able to...                                                                                                         |
|---------------------------|----------------------------------------------------------------------------------------------------------------------------------|
| Hess's law                | State that the enthalpy change of a reaction is independent of the route taken, and use energy cycles to exploit this.           |
| Enthalpies of formation   | Calculate $\Delta H^\circ_r$ from standard enthalpies of formation of reactants and products.                                    |
| Enthalpies of combustion  | Calculate $\Delta H^\circ_r$ from standard enthalpies of combustion of reactants and products.                                   |
| Hess cycles               | Combine given equations (reversing and scaling as needed) to reach a target equation and its enthalpy change.                    |
| Bond enthalpies           | Estimate $\Delta H^\circ$ of a gas-phase reaction from average bond enthalpies of bonds broken and made.                         |
| Born–Haber cycles (HL)    | Construct a Born–Haber cycle and determine an unknown step such as lattice enthalpy or electron affinity.                        |
| Enthalpy of solution (HL) | Relate $\Delta H^\circ_{\text{sol}}$ to lattice enthalpy and hydration enthalpies, and account for trends in hydration enthalpy. |

**Exam note:** Hess cycles, formation, combustion and bond enthalpies are **SL and HL**.  
Born–Haber cycles and the solution/hydration cycle are **HL only** (flagged with “(HL)” below).  
All numerical data in an exam is supplied — you are marked on the cycle and the arithmetic.

## 1. Hess's law and state functions

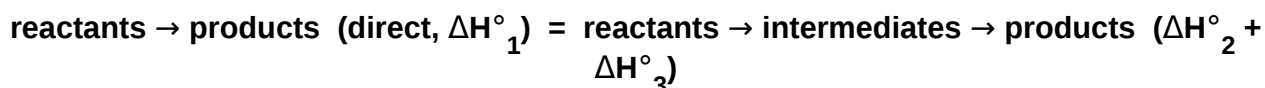
Enthalpy,  $H$ , is a **state function**: its value depends only on the current state of the system (temperature, pressure, amount and identity of substances), not on how that state was reached. It follows that the change in enthalpy between reactants and products,  $\Delta H^\circ$ , depends only on the initial and final states — not on the pathway.

**Hess's law:** the total enthalpy change for a reaction is the same whether the reaction takes place in one step or in several steps.

This is a direct consequence of the conservation of energy: if a route from reactants to products and back released or absorbed net energy, we could build a perpetual-motion machine. Because we cannot, every route must give the same  $\Delta H^\circ$ .

### Energy cycle diagrams

An energy cycle draws the direct reaction as one arrow and an indirect route (through intermediates such as elements, or gaseous ions, or combustion products) as a chain of arrows. Because both routes start and finish at the same states, their enthalpy changes are equal:



The whole of this topic is the same three moves applied to different intermediates: (1) draw the two routes, (2) equate them, (3) rearrange for the unknown. The only rules are that **reversing** a step changes the sign of its  $\Delta H^\circ$ , and **scaling** an equation by a factor scales its  $\Delta H^\circ$  by the same factor.

**Standard conditions:** A standard enthalpy change  $\Delta H^\circ$  (note the degree sign) is measured at 100 kPa and a stated temperature, usually 298 K, with all substances in their standard states. Always keep state symbols — they change the value (for example water as liquid versus gas).

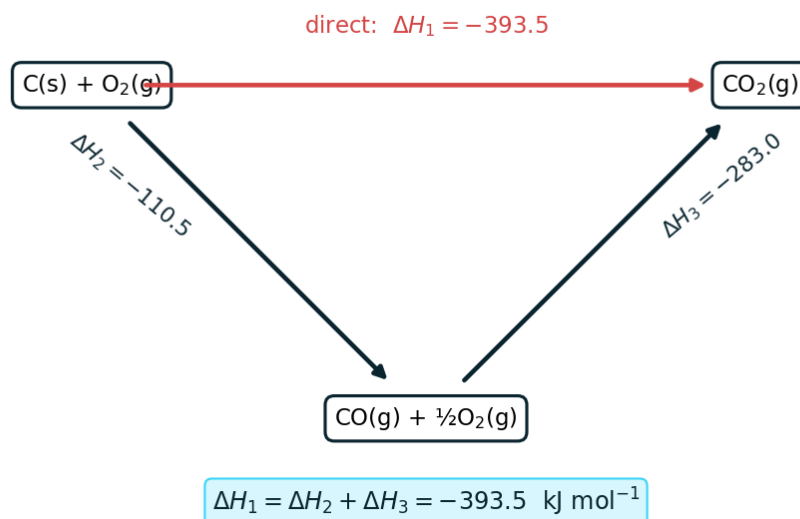


Figure 1. Hess's law cycle: the direct enthalpy change  $\Delta H_1$  equals the indirect route  $\Delta H_2 + \Delta H_3$ . Here  $-393.5 = (-110.5) + (-283.0) \text{ kJ mol}^{-1}$ .

## 2. Using enthalpies of formation

The **standard enthalpy of formation**,  $\Delta H^\circ_f$ , is the enthalpy change when **one mole** of a compound forms from its elements in their standard states. By definition,  $\Delta H^\circ_f$  of any element in its standard state is **zero** (for example  $\text{O}_2\text{(g)}$ ,  $\text{C(graphite)}$ ,  $\text{Na(s)}$ ).

Imagine breaking all reactants down into their elements and then building the products from those elements. The elements are the shared intermediate, so:

$$\Delta H^\circ_r = \sum \Delta H^\circ_f(\text{products}) - \sum \Delta H^\circ_f(\text{reactants})$$

Multiply each  $\Delta H^\circ_f$  by the stoichiometric coefficient of that species in the balanced equation. "Products minus reactants" is the direction that comes straight from the cycle: down from elements to products, up (reversed) from reactants to elements.

**Worked example 1 — combustion of methane from formation data**

Find  $\Delta H^\circ_r$  for  $\text{CH}_4(\text{g}) + 2\text{O}_2(\text{g}) \rightarrow \text{CO}_2(\text{g}) + 2\text{H}_2\text{O}(\text{l})$ .

Data /  $\text{kJ mol}^{-1}$ :  $\Delta H^\circ_f[\text{CH}_4] = -74.8$ ;  $\Delta H^\circ_f[\text{CO}_2] = -393.5$ ;  $\Delta H^\circ_f[\text{H}_2\text{O}(\text{l})] = -285.8$ ;  $\Delta H^\circ_f[\text{O}_2] = 0$ .

$$\begin{aligned}\Delta H^\circ_r &= [(-393.5) + 2(-285.8)] - [(-74.8) + 2(0)] \\ &= [-393.5 - 571.6] - [-74.8] = -965.1 + 74.8 = \mathbf{-890.3 \text{ kJ mol}^{-1}} \text{ (exothermic)}.\end{aligned}$$

**Worked example 2 — combustion of ethanol from formation data**

Find  $\Delta H^\circ_r$  for  $\text{C}_2\text{H}_5\text{OH}(\text{l}) + 3\text{O}_2(\text{g}) \rightarrow 2\text{CO}_2(\text{g}) + 3\text{H}_2\text{O}(\text{l})$ .

Data /  $\text{kJ mol}^{-1}$ :  $\Delta H^\circ_f[\text{C}_2\text{H}_5\text{OH}(\text{l})] = -277.7$ ;  $\Delta H^\circ_f[\text{CO}_2] = -393.5$ ;  $\Delta H^\circ_f[\text{H}_2\text{O}(\text{l})] = -285.8$ .

$$\begin{aligned}\Delta H^\circ_r &= [2(-393.5) + 3(-285.8)] - [(-277.7) + 3(0)] \\ &= [-787.0 - 857.4] + 277.7 = -1644.4 + 277.7 = \mathbf{-1366.7 \text{ kJ mol}^{-1}}.\end{aligned}$$

Watch the coefficients: the  $\times 2$  and  $\times 3$  are the commonest place to drop marks.

### 3. Using enthalpies of combustion

The **standard enthalpy of combustion**,  $\Delta H^\circ_c$ , is the enthalpy change when **one mole** of a substance burns completely in oxygen under standard conditions. Here the shared intermediate is the set of combustion products ( $\text{CO}_2$  and  $\text{H}_2\text{O}$ ). Burning the reactants and burning the products must reach the same place, so:

$$\Delta H^\circ_r = \Sigma \Delta H^\circ_c(\text{reactants}) - \Sigma \Delta H^\circ_c(\text{products})$$

Notice the direction is **reversed** relative to the formation equation (reactants minus products). The reason is geometric: on a combustion cycle the arrows point *down* from both reactants and products to the common combustion products, so building the target means going down the reactant arrow and *up* the product arrow.

**Worked example 3 — enthalpy of formation of methane from combustion data**

Find  $\Delta H^\circ_f[\text{CH}_4]$  for  $\text{C}(\text{s}) + 2\text{H}_2(\text{g}) \rightarrow \text{CH}_4(\text{g})$ .

Data /  $\text{kJ mol}^{-1}$ :  $\Delta H^\circ_c[\text{C}] = -393.5$ ;  $\Delta H^\circ_c[\text{H}_2] = -285.8$ ;  $\Delta H^\circ_c[\text{CH}_4] = -890.3$ .

$$\begin{aligned}\Delta H^\circ_r &= \Sigma \Delta H^\circ_c(\text{reactants}) - \Sigma \Delta H^\circ_c(\text{products}) = [(-393.5) + 2(-285.8)] - [(-890.3)] \\ &= [-393.5 - 571.6] + 890.3 = -965.1 + 890.3 = \mathbf{-74.8 \text{ kJ mol}^{-1}}.\end{aligned}$$

This is the reverse calculation of Worked example 1 — combustion and formation data are two ways into the same cycle.

**Why the signs differ:** Formation uses “products – reactants”; combustion uses “reactants – products”. Do not memorise them blindly — sketch the cycle and the direction falls out every time. Elements have  $\Delta H^\circ_f = 0$  but a non-zero  $\Delta H^\circ_c$  (e.g. carbon burns).

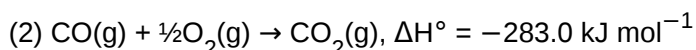
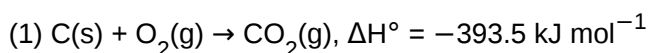
## 4. Constructing Hess cycles from given equations

Often you are handed two or three thermochemical equations and asked for the  $\Delta H^\circ$  of a target equation that is some combination of them. Treat the equations like algebra: add, subtract, reverse and scale them until the species cancel to leave the target. Apply the identical operations to the  $\Delta H^\circ$  values.

- **Reverse** an equation  $\rightarrow$  change the sign of  $\Delta H^\circ$ .
- **Multiply** an equation by  $n \rightarrow$  multiply  $\Delta H^\circ$  by  $n$ .
- **Add** equations  $\rightarrow$  add their  $\Delta H^\circ$  values; species on opposite sides cancel.

### Worked example 4 — target by subtraction

Find  $\Delta H^\circ$  for  $\text{C(s)} + \frac{1}{2}\text{O}_2(\text{g}) \rightarrow \text{CO(g)}$ , given:

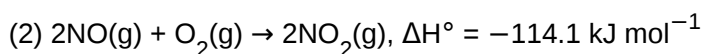
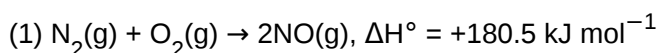


Target = (1) – (2): reverse (2) and add.  $\text{C} + \text{O}_2$  gives  $\text{CO}_2$ ; then  $\text{CO}_2$  gives  $\text{CO} + \frac{1}{2}\text{O}_2$ .  $\text{CO}_2$  and  $\frac{1}{2}\text{O}_2$  cancel to leave  $\text{C} + \frac{1}{2}\text{O}_2 \rightarrow \text{CO}$ .

$\Delta H^\circ = (-393.5) - (-283.0) = -110.5 \text{ kJ mol}^{-1}$ . (This step cannot be measured directly — some  $\text{CO}_2$  always forms — which is exactly why Hess's law is needed.)

### Worked example 5 — target by addition and scaling

Find  $\Delta H^\circ$  for  $\text{N}_2(\text{g}) + 2\text{O}_2(\text{g}) \rightarrow 2\text{NO}_2(\text{g})$ , given:



Add (1) + (2): the 2NO produced in (1) is consumed in (2) and cancels, leaving  $\text{N}_2 + 2\text{O}_2 \rightarrow 2\text{NO}_2$ .

$\Delta H^\circ = (+180.5) + (-114.1) = +66.4 \text{ kJ mol}^{-1}$  (endothermic).

## 5. Bond enthalpies

The **average bond enthalpy** is the energy needed to break one mole of a given type of bond in the **gaseous** state, averaged over a range of molecules. Breaking bonds is always **endothermic** (+); making bonds is always **exothermic** (–). Treat a reaction as breaking every bond in the reactants and remaking every bond in the products:

$$\Delta H^\circ \approx \Sigma(\text{bonds broken}) - \Sigma(\text{bonds made})$$

The relation is **approximate** and carries a “ $\approx$ ” for two reasons: the values are averages that ignore the specific molecular environment, and the equation is only valid when every species is a **gas** (bond enthalpies say nothing about the energy of forming a liquid or solid). If a reactant or product is a liquid or solid, bond enthalpies alone will not give an accurate answer.

### Worked example 6 — hydrogenation of ethene

Estimate  $\Delta H^\circ$  for  $\text{C}_2\text{H}_4(\text{g}) + \text{H}_2(\text{g}) \rightarrow \text{C}_2\text{H}_6(\text{g})$ .

Bond enthalpies /  $\text{kJ mol}^{-1}$ : C=C 614, C–C 346, C–H 414, H–H 436.

Net change: break one C=C and one H–H; make one C–C and two new C–H (the four original C–H bonds are unchanged and cancel).

$$\Delta H^\circ = [614 + 436] - [346 + 2(414)] = 1050 - 1174 = -124 \text{ kJ mol}^{-1}.$$

The experimental value is about  $-137 \text{ kJ mol}^{-1}$ ; the  $\sim 13 \text{ kJ mol}^{-1}$  gap is the price of using average bond enthalpies.

### Worked example 7 — combustion of methane (gaseous water)

Estimate  $\Delta H^\circ$  for  $\text{CH}_4(\text{g}) + 2\text{O}_2(\text{g}) \rightarrow \text{CO}_2(\text{g}) + 2\text{H}_2\text{O}(\text{g})$ .

Bond enthalpies /  $\text{kJ mol}^{-1}$ : C–H 414, O=O 498, C=O (in  $\text{CO}_2$ ) 804, O–H 463.

Broken:  $4 \text{ C–H} + 2 \text{ O=O} = 4(414) + 2(498) = 1656 + 996 = 2652$ .

Made:  $2 \text{ C=O} + 4 \text{ O–H} = 2(804) + 4(463) = 1608 + 1852 = 3460$ .

$$\Delta H^\circ = 2652 - 3460 = -808 \text{ kJ mol}^{-1}.$$

This differs from the  $-890 \text{ kJ mol}^{-1}$  of Worked example 1 because bond enthalpies require **gaseous** water; condensing  $2\text{H}_2\text{O}(\text{g})$  to  $2\text{H}_2\text{O}(\text{l})$  would release a further  $\sim 88 \text{ kJ mol}^{-1}$ .

**Ozone / resonance trap:** Use the specific value quoted (e.g. C=O in  $\text{CO}_2$  is  $804 \text{ kJ mol}^{-1}$ , not the general  $\sim 745$  for a carbonyl). Always count every bond, including all the C–H bonds you might be tempted to ignore.

## 6. Born–Haber cycles (HL)

A Born–Haber cycle is a Hess cycle for the formation of an ionic compound. It builds the compound by two routes: directly from the elements ( $\Delta H^\circ_f$ ), or the long way round — atomising the elements, ionising the gaseous atoms, then bringing the gaseous ions together to form the lattice.

The steps for a compound  $\text{M}^+\text{X}^-(\text{s})$  are:

| Step                                      | Process                                                                                                                                            | Sign            |
|-------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------|-----------------|
| Atomisation, $\Delta H^\circ_{\text{at}}$ | Element $\rightarrow$ gaseous atoms (e.g. $\text{Na}(\text{s}) \rightarrow \text{Na}(\text{g})$ ; $\frac{1}{2}\text{Cl}_2 \rightarrow \text{Cl}$ ) | endothermic (+) |
| Ionisation energy, IE                     | Gaseous atom $\rightarrow$ gaseous cation + $\text{e}^-$                                                                                           | endothermic (+) |

| Step                                            | Process                                                       | Sign                    |
|-------------------------------------------------|---------------------------------------------------------------|-------------------------|
| Electron affinity, EA                           | Gaseous atom + $e^- \rightarrow$ gaseous anion                | usually exothermic (–)  |
| Lattice enthalpy, $\Delta H^\circ_{\text{lat}}$ | Gaseous ions $\rightarrow$ ionic solid (formation of lattice) | strongly exothermic (–) |
| Formation, $\Delta H^\circ_f$                   | Elements $\rightarrow$ ionic solid (the direct route)         | usually exothermic (–)  |

Equating the direct route with the long route gives the master equation:

$$\Delta H^\circ_f = \Delta H^\circ_{\text{at}}(\text{metal}) + \text{IE} + \Delta H^\circ_{\text{at}}(\text{non-metal}) + \text{EA} + \Delta H^\circ_{\text{lat}}$$

Any one unknown — most often the lattice enthalpy, which cannot be measured directly — is found by rearrangement.

### Worked example 8 — lattice enthalpy of sodium chloride

Find the lattice enthalpy (of formation)  $\Delta H^\circ_{\text{lat}}$  for NaCl, given /  $\text{kJ mol}^{-1}$ :

$\Delta H^\circ_f[\text{NaCl}] = -411$ ;  $\Delta H^\circ_{\text{at}}[\text{Na}] = +107$ ;  $\text{IE}_1[\text{Na}] = +496$ ;  $\Delta H^\circ_{\text{at}}[\text{Cl}] = +121$  ( $= \frac{1}{2} \times 242$ );  $\text{EA}_1[\text{Cl}] = -349$ .

Rearrange:  $\Delta H^\circ_{\text{lat}} = \Delta H^\circ_f - [\Delta H^\circ_{\text{at}}(\text{Na}) + \text{IE} + \Delta H^\circ_{\text{at}}(\text{Cl}) + \text{EA}]$ .

Bracket =  $107 + 496 + 121 + (-349) = +375$ .

$\Delta H^\circ_{\text{lat}} = (-411) - (+375) = -786 \text{ kJ mol}^{-1}$  (lattice dissociation =  $+786 \text{ kJ mol}^{-1}$ ).

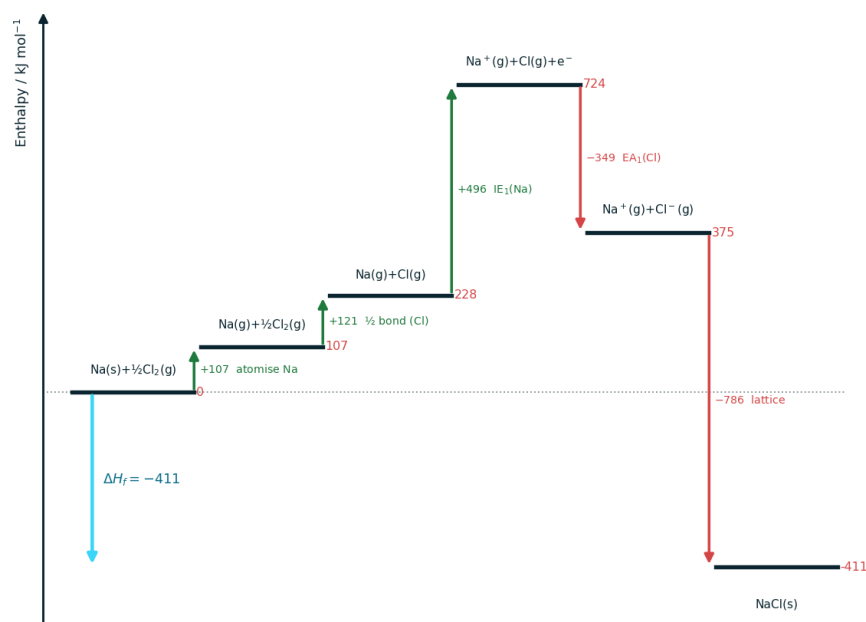


Figure 2. Born–Haber cycle for NaCl (HL): the direct formation  $\Delta H^\circ_f$  ( $-411 \text{ kJ mol}^{-1}$ ) equals the long route (atomise, ionise, electron affinity, lattice). Solving gives lattice enthalpy  $-786 \text{ kJ mol}^{-1}$ ; the sum around the cycle is 0.

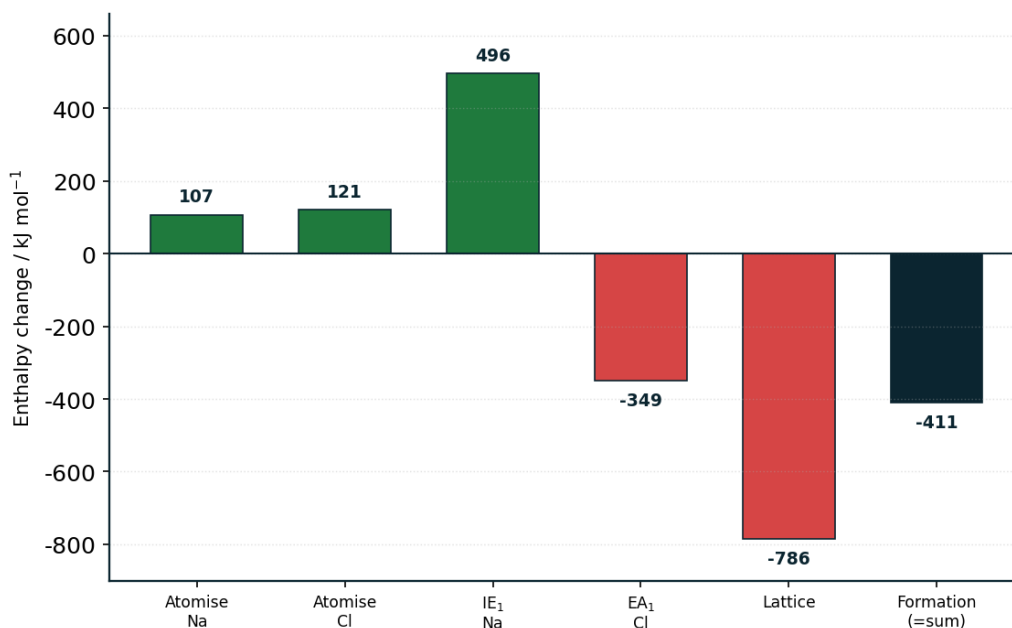


Figure 3. Signed component enthalpies of the NaCl Born–Haber cycle (green endothermic, red exothermic). The five steps sum to the formation enthalpy  $\Delta H_f^\circ = -411 \text{ kJ mol}^{-1}$ .

## Comparing ionic compounds

Lattice enthalpy becomes more exothermic (larger magnitude) as the **ionic charges increase** and as the **ionic radii decrease**, because the electrostatic attraction between ions rises. So the magnitude of the lattice enthalpy follows  $\text{MgO} > \text{NaCl}$ , and  $\text{NaF} > \text{NaCl} > \text{NaBr} > \text{NaI}$ . A large lattice enthalpy is why MgO is so much harder to melt than NaCl.

**Sign discipline (HL):** Data booklets usually list **lattice dissociation** enthalpies as positive (solid  $\rightarrow$  gaseous ions). If your cycle is built with gaseous ions  $\rightarrow$  solid, you need the negative (formation) value. State which one you are using and keep it consistent — a wrong sign here is the classic HL error.

## 7. Enthalpy of solution and hydration (HL)

When an ionic solid dissolves in water, the lattice must first be pulled apart into gaseous ions (endothermic, = the lattice dissociation enthalpy), and those gaseous ions are then surrounded and stabilised by water molecules (exothermic, = the hydration enthalpies). The **enthalpy of solution**,  $\Delta H_{\text{sol}}^\circ$ , is the sum:

$$\Delta H_{\text{sol}}^\circ = -\Delta H_{\text{lat}}^\circ + \sum \Delta H_{\text{hyd}}^\circ$$

Here  $\Delta H_{\text{lat}}^\circ$  is the (negative) lattice enthalpy of formation, so “ $-\Delta H_{\text{lat}}^\circ$ ” is the positive energy needed to break the lattice; each  $\Delta H_{\text{hyd}}^\circ$  (for the cation and the anion) is negative. The **hydration enthalpy** is the enthalpy change when one mole of gaseous ions is dissolved in water to give an infinitely dilute solution:  $X^{n\pm}(\text{g}) \rightarrow X^{n\pm}(\text{aq})$ .

**Worked example 9 — enthalpy of solution of sodium chloride**

Find  $\Delta H^\circ_{\text{sol}}[\text{NaCl}]$  given /  $\text{kJ mol}^{-1}$ : lattice dissociation  $-\Delta H^\circ_{\text{lat}} = +786$ ;  $\Delta H^\circ_{\text{hyd}}[\text{Na}^+] = -406$ ;  $\Delta H^\circ_{\text{hyd}}[\text{Cl}^-] = -378$ .

$$\Delta H^\circ_{\text{sol}} = +786 + (-406) + (-378) = +786 - 784$$

= **+2 kJ mol<sup>-1</sup>** — very slightly endothermic, which is why a NaCl solution cools almost imperceptibly as it dissolves.

The two large numbers (breaking the lattice, hydrating the ions) nearly cancel, so  $\Delta H^\circ_{\text{sol}}$  is a small difference of large quantities — round carefully.

**Trends in hydration enthalpy**

Hydration enthalpy becomes more exothermic (larger magnitude) as the **ionic charge increases** and as the **ionic radius decreases**, because a smaller, more highly charged ion has a greater charge density and attracts the polar water molecules more strongly.

| Ion              | Radius trend | Hydration enthalpy / kJ mol <sup>-1</sup> | Comment                                     |
|------------------|--------------|-------------------------------------------|---------------------------------------------|
| Li <sup>+</sup>  | smallest     | -519                                      | most exothermic of the group 1 cations      |
| Na <sup>+</sup>  | larger       | -406                                      | charge density falls down the group         |
| K <sup>+</sup>   | larger still | -322                                      | least exothermic shown                      |
| Mg <sup>2+</sup> | small, 2+    | -1920                                     | high charge, small radius → very exothermic |

**Same logic, twice:** Both lattice enthalpy and hydration enthalpy are governed by the **same** two factors — ionic charge and ionic radius. Higher charge and smaller radius make *both* more exothermic, which is why  $\Delta H^\circ_{\text{sol}}$  (a small difference between them) is hard to predict by inspection.

**8. Common pitfalls**

- **Direction in a cycle:** formation uses products – reactants; combustion uses reactants – products. Sketch the cycle rather than guessing.
- **Forgetting to reverse a sign:** reversing an equation flips the sign of  $\Delta H^\circ$ ; scaling multiplies it. Do both to the equation and to  $\Delta H^\circ$  together.
- **Coefficients:** multiply each  $\Delta H^\circ_f$ ,  $\Delta H^\circ_c$  or bond enthalpy by the number of moles in the balanced equation (the  $\times 2$ ,  $\times 3$  traps).
- **Average vs exact:** bond-enthalpy answers are estimates ( $\approx$ ); formation/combustion answers are, in principle, exact. Never quote a bond-enthalpy result as if it were exact.
- **States:** bond enthalpies apply to **gases only**;  $\text{H}_2\text{O}(\text{l})$  and  $\text{H}_2\text{O}(\text{g})$  give different answers. Keep state symbols throughout.
- **Lattice-enthalpy sign (HL):** decide up front whether you are using the dissociation (+) or formation (–) value and stay consistent.

- **Elements:**  $\Delta H_f^\circ$  of an element = 0, but its  $\Delta H_c^\circ$  is not zero. Do not set combustion enthalpies of elements to zero.

## 9. Quick reference

| Tool                | Equation                                                                                                                           | Use when...                             |
|---------------------|------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------|
| Formation data      | $\Delta H_r^\circ = \sum \Delta H_f^\circ(\text{prod}) - \sum \Delta H_f^\circ(\text{react})$                                      | given $\Delta H_f^\circ$ of all species |
| Combustion data     | $\Delta H_r^\circ = \sum \Delta H_c^\circ(\text{react}) - \sum \Delta H_c^\circ(\text{prod})$                                      | given $\Delta H_c^\circ$ of all species |
| Bond enthalpies     | $\Delta H^\circ \approx \Sigma(\text{broken}) - \Sigma(\text{made})$                                                               | all species gaseous; estimate only      |
| Born–Haber (HL)     | $\Delta H_f^\circ = \Delta H_{\text{at}}^\circ + \text{IE} + \Delta H_{\text{at}}^\circ + \text{EA} + \Delta H_{\text{lat}}^\circ$ | ionic solid; find lattice / EA / IE     |
| Solution cycle (HL) | $\Delta H_{\text{sol}}^\circ = -\Delta H_{\text{lat}}^\circ + \sum \Delta H_{\text{hyd}}^\circ$                                    | dissolving an ionic solid in water      |
| Golden rules        | reverse → flip sign; scale → × the $\Delta H^\circ$                                                                                | every Hess calculation                  |

## 10. Test yourself

Attempt all ten without notes, then check against the full worked answers. All data is in  $\text{kJ mol}^{-1}$ .

**Q1 (formation).** Find  $\Delta H_r^\circ$  for  $2\text{H}_2\text{S}(\text{g}) + 3\text{O}_2(\text{g}) \rightarrow 2\text{SO}_2(\text{g}) + 2\text{H}_2\text{O}(\text{l})$ .  $\Delta H_f^\circ$ :  $\text{H}_2\text{S} -21$ ,  $\text{SO}_2 -297$ ,  $\text{H}_2\text{O}(\text{l}) -286$ .

**Q2 (formation).** Find  $\Delta H_r^\circ$  for  $\text{C}_2\text{H}_4(\text{g}) + \text{H}_2\text{O}(\text{l}) \rightarrow \text{C}_2\text{H}_5\text{OH}(\text{l})$ .  $\Delta H_f^\circ$ :  $\text{C}_2\text{H}_4 +52$ ,  $\text{H}_2\text{O}(\text{l}) -286$ ,  $\text{C}_2\text{H}_5\text{OH} -278$ .

**Q3 (combustion).** Find  $\Delta H_f^\circ$  for  $2\text{C}(\text{s}) + \text{H}_2(\text{g}) \rightarrow \text{C}_2\text{H}_2(\text{g})$ .  $\Delta H_c^\circ$ :  $\text{C} -394$ ,  $\text{H}_2 -286$ ,  $\text{C}_2\text{H}_2 -1300$ .

**Q4 (combustion).** Find  $\Delta H_f^\circ$  for  $\text{C}(\text{s}) + 2\text{H}_2(\text{g}) + \frac{1}{2}\text{O}_2(\text{g}) \rightarrow \text{CH}_3\text{OH}(\text{l})$ .  $\Delta H_c^\circ$ :  $\text{C} -394$ ,  $\text{H}_2 -286$ ,  $\text{CH}_3\text{OH} -726$ .

**Q5 (Hess).** Find  $\Delta H_f^\circ$  for  $2\text{C}(\text{s}) + 3\text{H}_2(\text{g}) \rightarrow \text{C}_2\text{H}_6(\text{g})$  from (1)  $\text{C} + \text{O}_2 \rightarrow \text{CO}_2$ ,  $-394$ ; (2)  $\text{H}_2 + \frac{1}{2}\text{O}_2 \rightarrow \text{H}_2\text{O}$ ,  $-286$ ; (3)  $\text{C}_2\text{H}_6 + 3\frac{1}{2}\text{O}_2 \rightarrow 2\text{CO}_2 + 3\text{H}_2\text{O}$ ,  $-1560$ .

**Q6 (Hess).** Find  $\Delta H_r^\circ$  for  $\text{Fe}_2\text{O}_3(\text{s}) + 3\text{CO}(\text{g}) \rightarrow 2\text{Fe}(\text{s}) + 3\text{CO}_2(\text{g})$ .  $\Delta H_f^\circ$ :  $\text{Fe}_2\text{O}_3 -824$ ,  $\text{CO} -111$ ,  $\text{CO}_2 -394$ .

**Q7 (bond enthalpy).** Estimate  $\Delta H^\circ$  for  $\text{H}_2(\text{g}) + \text{Cl}_2(\text{g}) \rightarrow 2\text{HCl}(\text{g})$ . Bonds:  $\text{H}-\text{H} 436$ ,  $\text{Cl}-\text{Cl} 242$ ,  $\text{H}-\text{Cl} 431$ .

**Q8 (bond enthalpy).** Estimate  $\Delta H^\circ$  for  $\text{N}_2(\text{g}) + 3\text{H}_2(\text{g}) \rightarrow 2\text{NH}_3(\text{g})$ . Bonds:  $\text{N}\equiv\text{N} 945$ ,  $\text{H}-\text{H} 436$ ,  $\text{N}-\text{H} 391$ .

**Q9 (Born–Haber, HL).** Find the lattice enthalpy (formation)  $\Delta H_{\text{lat}}^\circ$  for  $\text{KCl}$ .  $\Delta H_f^\circ -437$ ;  $\Delta H_{\text{at}}^\circ[\text{K}] +90$ ;  $\text{IE}_1[\text{K}] +419$ ;  $\Delta H_{\text{at}}^\circ[\text{Cl}] +121$ ;  $\text{EA}_1[\text{Cl}] -349$ .

**Q10 (solution, HL).** Find  $\Delta H_{\text{sol}}^\circ[\text{KCl}]$  given lattice dissociation  $+718$ ,  $\Delta H_{\text{hyd}}^\circ[\text{K}^+] -322$ ,  $\Delta H_{\text{hyd}}^\circ[\text{Cl}^-] -378$ .

### Worked answers

**A1.**  $\Delta H_r^\circ = [2(-297) + 2(-286)] - [2(-21) + 0] = [-594 - 572] - (-42) = -1166 + 42 = -1124 \text{ kJ mol}^{-1}$ .

**A2.**  $\Delta H_r^\circ = [-278] - [(+52) + (-286)] = -278 - (-234) = -278 + 234 = -44 \text{ kJ mol}^{-1}$ .

**A3.** Using  $\Sigma\Delta H^\circ_{\text{c}}(\text{react}) - \Sigma\Delta H^\circ_{\text{c}}(\text{prod})$ :  $\Delta H^\circ_{\text{f}} = [2(-394) + (-286)] - [(-1300)] = [-788 - 286] + 1300 = -1074 + 1300 = \mathbf{+226 \text{ kJ mol}^{-1}}$  (endothermic — ethyne is energetically unstable relative to its elements).

**A4.**  $\Delta H^\circ_{\text{f}} = [(-394) + 2(-286)] - [(-726)] = [-394 - 572] + 726 = -966 + 726 = \mathbf{-240 \text{ kJ mol}^{-1}}$ . ( $\text{O}_2$  is an element: no  $\Delta H^\circ_{\text{c}}$  term.)

**A5.** Target =  $2 \times (1) + 3 \times (2) - (3)$ :  $\Delta H^\circ_{\text{f}} = 2(-394) + 3(-286) - (-1560) = -788 - 858 + 1560 = \mathbf{-86 \text{ kJ mol}^{-1}}$ .

**A6.**  $\Delta H^\circ_{\text{r}} = [2(0) + 3(-394)] - [(-824) + 3(-111)] = -1182 - (-1157) = -1182 + 1157 = \mathbf{-25 \text{ kJ mol}^{-1}}$ .

**A7.** Broken  $436 + 242 = 678$ ; made  $2(431) = 862$ .  $\Delta H^\circ = 678 - 862 = \mathbf{-184 \text{ kJ mol}^{-1}}$ .

**A8.** Broken  $945 + 3(436) = 945 + 1308 = 2253$ ; made  $6(391) = 2346$ .  $\Delta H^\circ = 2253 - 2346 = \mathbf{-93 \text{ kJ mol}^{-1}}$  (per 2 mol  $\text{NH}_3$ ; experimental  $-92$ ).

**A9.**  $\Delta H^\circ_{\text{lat}} = \Delta H^\circ_{\text{f}} - [\Delta H^\circ_{\text{at}}(\text{K}) + \text{IE} + \Delta H^\circ_{\text{at}}(\text{Cl}) + \text{EA}] = (-437) - [90 + 419 + 121 + (-349)] = (-437) - (+281) = \mathbf{-718 \text{ kJ mol}^{-1}}$  (dissociation  $+718$ ).

**A10.**  $\Delta H^\circ_{\text{sol}} = +718 + (-322) + (-378) = +718 - 700 = \mathbf{+18 \text{ kJ mol}^{-1}}$  (endothermic; KCl dissolving cools the solution).