

Energetics I — Enthalpy

01 · ENTHALPY BASICS

Exothermic — heat released to the surroundings, ΔH **negative**, products lower in energy, temperature of surroundings rises. **Endothermic** — heat absorbed, ΔH **positive**.

Bond breaking is endothermic, bond making exothermic. A reaction is exothermic when the bonds formed are stronger than the bonds broken.

Standard conditions ($^\circ$): 100 kPa, 298 K, solutions 1 mol dm⁻³, all substances in their standard states. Always give state symbols and units of kJ mol⁻¹.

02 · DEFINITIONS TO QUOTE

ΔH_f° — enthalpy change when one mole of a compound forms from its elements in their standard states. Zero for an element.

ΔH_c° — enthalpy change on complete combustion of one mole of a substance in excess oxygen.

$\Delta H_{\text{neut}}^\circ$ — enthalpy change when one mole of water forms from acid and base. About -57 kJ mol⁻¹ for strong acid + strong base.

Bond enthalpy — energy to break one mole of a bond in the **gaseous** state; the value quoted is a mean over many compounds.

03 · CALORIMETRY

$$q = mc\Delta T \cdot \Delta H = -q \div n$$

m = mass of **water or solution** in g (never the fuel or the solid), c = 4.18 J g⁻¹ K⁻¹, ΔT in K or $^\circ\text{C}$ (same size). q comes out in J — divide by 1000 for kJ.

n = moles of the **limiting** reactant. The minus sign converts "heat gained by water" into "enthalpy change of the reaction". Assume the solution has the density and specific heat capacity of water.

04 · WORKED EXAMPLE — CALORIMETRY

0.850 g of propan-1-ol (M = 60.1) burns and raises 150.0 g of water by 22.5 K. Find ΔH_c° .

$$q = 150.0 \times 4.18 \times 22.5 = \mathbf{14\,108\,J} = 14.1\,\text{kJ}$$

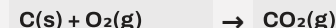
$$n = 0.850 \div 60.1 = \mathbf{0.01414\,mol}$$

$$\Delta H_c^\circ = -14.1 \div 0.01414 = \mathbf{-999\,kJ\,mol^{-1}}$$

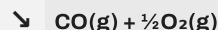
The data-booklet value is -2021 kJ mol⁻¹; the shortfall is heat lost to the air and apparatus and incomplete combustion.

05 · HESS'S LAW

The enthalpy change of a reaction is independent of the route taken, because enthalpy is a state function. Add the steps of any complete path.



$\Delta H_1 = \text{DIRECT ROUTE}$



$\Delta H_2 \text{ THEN } \Delta H_3 = \text{INDIRECT ROUTE}$

$$\Delta H_1 = \Delta H_2 + \Delta H_3$$

Reverse a step and the sign flips; multiply a step and the value multiplies. Arrows pointing the same way around a cycle add; one pointing against the cycle is subtracted.

06 · WORKED EXAMPLE — HESS CYCLE

Find ΔH for $\text{C(s)} + \frac{1}{2}\text{O}_2\text{(g)} \rightarrow \text{CO(g)}$, given $\Delta H_c^\circ[\text{C(s)}] = -394$ and $\Delta H_c^\circ[\text{CO(g)}] = -283$ kJ mol⁻¹.

Both routes end at CO₂(g), so using the cycle above:

$$\Delta H_1 = \Delta H_2 + \Delta H_3 \rightarrow -394 = \Delta H_2 + (-283)$$

$$\Delta H_2 = -394 + 283 = \mathbf{-111\,kJ\,mol^{-1}}$$

07 · EXAM-STYLE QUESTION — DRAW THE CYCLE

Q. Use the enthalpies of formation below to find ΔH for



ΔH_f° : CaCO₃ -1207, CaO -635, CO₂ -394 kJ mol⁻¹.



$\Delta H = \text{WHAT WE WANT}$



$\Delta H_f^\circ \text{ -1207}$

$\Delta H_f^\circ \text{ -635 AND -394}$

A. Both formation arrows start at the elements, so go **up the left arrow (sign flips)** and down the right:

$$\Delta H = \Sigma \Delta H_f^\circ(\text{products}) - \Sigma \Delta H_f^\circ(\text{reactants})$$

$$\Delta H = (-635 - 394) - (-1207) = \mathbf{+178\,kJ\,mol^{-1}}$$

Endothermic — which is why limestone needs a kiln.

08 · THE TWO STANDARD ROUTES

From ΔH_f° :

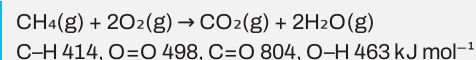
$$\Delta H = \Sigma \Delta H_f^\circ(\text{products}) - \Sigma \Delta H_f^\circ(\text{reactants})$$

From bond enthalpies:

$$\Delta H = \Sigma(\text{bonds broken}) - \Sigma(\text{bonds formed})$$

Multiply every term by its coefficient. Bond enthalpies only apply to gases, so a reaction involving liquids or solids gives an approximate answer — say so if asked to compare.

09 · WORKED EXAMPLE — BOND ENTHALPIES



$$\text{Broken: } 4(414) + 2(498) = 1656 + 996 = \mathbf{2652}$$

$$\text{Formed: } 2(804) + 4(463) = 1608 + 1852 = \mathbf{3460}$$

$$\Delta H = 2652 - 3460 = \mathbf{-808\,kJ\,mol^{-1}}$$

Note H₂O is taken as a gas — using H₂O(l) would need the enthalpy of vaporisation as well.

MARKS LOST HERE

— Using the mass of the fuel or solid in q = mc ΔT instead of the mass of water or solution.

— Forgetting the minus sign, or leaving the answer in J when the question asks for kJ mol⁻¹.

— Dividing by the total moles rather than the moles of the limiting reactant.

— Reversing a Hess step without flipping the sign.

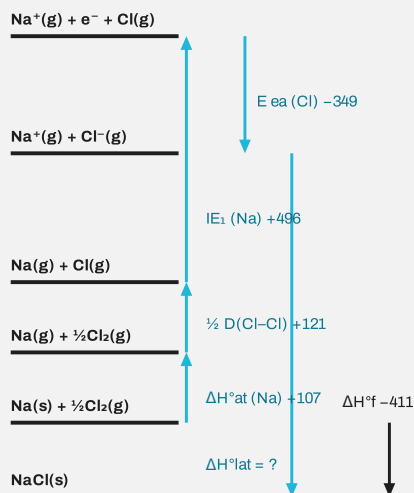
Energetics II — Born–Haber, Entropy, Gibbs

10 · BORN–HABER TERMS

Step	Sign
Atomisation / sublimation	+
Bond dissociation (½ per Cl)	+
Ionisation energy	+
Electron affinity	– (1st)
Lattice enthalpy (formation)	–
Enthalpy of formation	usually –

Lattice enthalpy of formation — enthalpy change when one mole of an ionic solid forms from its gaseous ions. Quoted as **dissociation** in the data booklet, so watch which direction the question wants: the two differ only in sign.

11 · BORN–HABER CYCLE — NaCl



Vertical axis is enthalpy; the diagram is schematic, not to scale.

12 · WORKED EXAMPLE — BORN–HABER

Both routes from Na(s) + ½Cl₂(g) reach NaCl(s):

$$\begin{aligned}\Delta H_f &= \Delta H_{at} + IE_1 + \frac{1}{2}D + E_{ea} + \Delta H_{lat} \\ -411 &= 107 + 496 + 121 + (-349) + \Delta H_{lat} \\ -411 &= 375 + \Delta H_{lat} \\ \Delta H_{lat} &= -411 - 375 = \mathbf{-786 \text{ kJ mol}^{-1}}\end{aligned}$$

For MgCl₂ double the ½D term, add IE₁ and IE₂, and take 2 × Eₑₐ.

13 · LATTICE ENTHALPY TRENDS

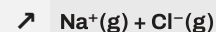
Magnitude ↑ with **larger ionic charge** and **smaller ionic radius**: MgO >> NaCl >> KI. Charge matters more than radius.

The **theoretical** value assumes a perfectly ionic lattice of point charges. Where the experimental (Born–Haber) value is much larger, the bonding has **covalent character** from polarisation of the anion — e.g. AgI.

14 · ENTHALPY OF SOLUTION CYCLE



ΔH°sol = DIRECT ROUTE



–ΔH°lat THEN ΣΔH°hyd

$$\Delta H^{\circ}\text{sol} = -\Delta H^{\circ}\text{lat} + \Sigma\Delta H^{\circ}\text{hyd}$$

$$\begin{aligned}\text{NaCl: } \Delta H_{\text{lat}} &= -786, \Delta H_{\text{hyd}}(\text{Na}^+) = -424, \\ \Delta H_{\text{hyd}}(\text{Cl}^-) &= -359 \\ \Delta H_{\text{sol}} &= +786 + (-424 - 359) = \mathbf{+3 \text{ kJ mol}^{-1}}\end{aligned}$$

Very small, so dissolving NaCl barely changes the temperature; it is driven by entropy.

15 · ENTROPY

$$\Delta S^{\circ} = \Sigma S^{\circ}(\text{products}) - \Sigma S^{\circ}(\text{reactants})$$

Units **J K⁻¹ mol⁻¹** — note the J, not kJ. Entropy measures the dispersal of energy among available states; S° of a perfect crystal at 0 K is zero, and S° values are positive for everything, elements included.

ΔS positive when: solid → liquid → gas, moles of gas increase, a solid dissolves, or one particle becomes many. **Negative** when gas moles fall, as in 2NO + O₂ → 2NO₂.

16 · GIBBS FREE ENERGY

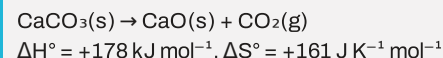
$$\Delta G^{\circ} = \Delta H^{\circ} - T\Delta S^{\circ}$$

T in **kelvin**; divide ΔS by 1000 to convert J to kJ before subtracting. **ΔG negative → spontaneous.**

ΔH	ΔS	Spontaneous?
–	+	always
–	–	low T only
+	+	high T only
+	–	never

At the crossover ΔG = 0, so **T = ΔH ÷ ΔS** — this is the melting or boiling point when the change is a phase change.

17 · WORKED EXAMPLE — GIBBS



$$\text{At } 298 \text{ K: } \Delta G = 178 - (298 \times 0.161) = 178 - 48.0 = \mathbf{+130 \text{ kJ mol}^{-1}} \rightarrow \text{not spontaneous.}$$

Crossover: T = 178 ÷ 0.161 = **1106 K**. Above this temperature ΔG turns negative and the carbonate decomposes.

DATA BOOKLET & MARKS LOST

Look up: ΔH_f, ΔH_c and S° values, bond enthalpies, ionisation energies, electron affinities, lattice and hydration enthalpies, c = 4.18 J g⁻¹ K⁻¹.

— Mixing J and kJ in ΔG = ΔH – TΔS. This is the single most common slip.

— Using the data booklet's lattice *dissociation* value without flipping the sign.

— Forgetting ½ for the bond dissociation of Cl₂, or omitting the second ionisation energy for a 2+ ion.

— Calling a spontaneous reaction fast: ΔG says nothing about rate.