## Arc length \& Area of Sector worksheet

1


NOT TO
SCALE
$E, F, G$ and $H$ are points on a circle with centre $O$ and radius 6 cm .
$E \hat{H} O=30^{\circ}$ and $E \hat{F} G=116^{\circ}$.
Calculate the shaded area.
$\mathrm{cm}^{2}$


NOT TO
SCALE

The diagram shows the major sector of a circle with centre $O$ and radius 3 cm .
Calculate the area of this sector.
Give your answer in the form $k \pi$, where $k$ is an integer.

3


NOT TO
SCALE
$P$ and $Q$ are points on the circumference of a different circle, centre $O$.
$P R$ and $Q R$ are tangents to the circle at $P$ and $Q$ respectively.
$O P=8 \mathrm{~cm}$ and $P \hat{O} Q=130^{\circ}$.
(i) Find $P R$.
(ii) Calculate the percentage of quadrilateral $O P R Q$ that is shaded.


The diagram shows two circles, both with centre $O$.
The radius of the small circle is 3 cm and the radius of the large circle is 6 cm .
The minor sector $A O B$ has an angle of $60^{\circ}$.
The total area of the shaded regions is $k \pi \mathrm{~cm}^{2}$.
Find the value of $k$.

$$
\begin{equation*}
k= \tag{4}
\end{equation*}
$$


$A C$ and $B D$ are diameters of the circle, centre $O$.
$A C=12 \mathrm{~cm}$ and $A \hat{O} B=130^{\circ}$.
(a) Calculate the area of triangle $A O B$.
$\qquad$
(b) Calculate the area of the sector $A O D$.

6 (a)

$O A B$ is a sector of a circle, centre $O$, radius 11 cm .
$A \hat{O} B=134^{\circ}$.
(i) Calculate the length of the arc $A B$.

Answer $\qquad$ cm [2]
(ii) Calculate the shortest distance from $O$ to the line $A B$.

7 (a) The ventilation shaft for a tunnel is in the shape of a cylinder.
The cylinder has radius 0.4 m and length 15 m .
Calculate the volume of the cylinder.
$\qquad$ $m^{3}[2]$
(b) The diagram shows the cross-section of the tunnel.


The cross-section of the tunnel is a major segment of a circle, centre $O$.
The radius of the circle is 4.5 m and $A O B=110^{\circ}$
Calculate the area of the cross-section of the tunnel.

$O A B$ is a sector of a circle, centre $O$, and radius 10 cm .
$A \hat{O} B=72^{\circ}$ and $C$ is the point on the arc $A B$ such that $O C$ bisects $A \hat{O} B$.
(a) Calculate the perimeter of sector $O A B$.
$\qquad$ cm [3]
(b) (i) Calculate the area of sector $O A B$.
$\mathrm{cm}^{2}$ [2]
(ii) Calculate the total shaded area.
$\mathrm{cm}^{2}$ [3]

9 (a) $P$ and $Q$ are points on the circumference of a circle, centre $O$, radius $R \mathrm{~cm}$. The minor arc $P Q=20 \mathrm{~cm}$ and $P \hat{O} Q=48^{\circ}$.
(i) Show that $R=23.9$, correct to one decimal place.

(ii) Calculate the area of the minor sector $P O Q$.
(iii) The minor sector $P O Q$ is removed from the circle and the remaining major sector is shaped to form an open cone of radius $r \mathrm{~cm}$.


Calculate $r$.


The diagram shows a sector of a circle with radius $3 r \mathrm{~cm}$ and angle $a^{\circ}$ and a circle with radius $r \mathrm{~cm}$.
The ratio of the area of the sector to the area of the circle with radius $r \mathrm{~cm}$ is $8: 1$.
(a) Find the value of $a$.

$$
\begin{equation*}
\text { Answer } a= \tag{3}
\end{equation*}
$$

(b) Find an expression, in terms of $\pi$ and $r$, for the perimeter of the sector.
$\qquad$

11 (a) $O A B$ is a sector of a circle, centre $O$, radius 6 cm .
$A \hat{O} B=25^{\circ}$.
(i) Calculate the length of the arc $A B$.

(ii) Calculate the area of the sector $O A B$.

## Answer

$\qquad$ $\mathrm{cm}^{2}$ [2]
(b) The sector $O A B$ from part (a) is the cross-section of a slice of cheese.

The slice has a height of 5 cm .
(i) Calculate the volume of this slice of cheese.


Answer $\qquad$ $\mathrm{cm}^{3}$ [1]
(ii) Calculate the total surface area of this slice of cheese.
$\qquad$


The angle of a sector of a circle, radius 6 cm , is $40^{\circ}$.
(i) The area of the sector is $k \pi \mathrm{~cm}^{2}$.

Find the value of $k$.
(ii) Find an expression, in terms of $\pi$, for the perimeter of the sector. Give your answer in the form $(a+b \pi)$ centimetres.
(iii) A geometrically similar sector has perimeter $(72+n \pi)$ centimetres.

Find the value of $n$.


A hollow cone has a base radius 6 cm and slant height 10 cm .
The curved surface of the cone is cut, and opened out into the shape of a sector of a circle, with angle $x^{\circ}$ and radius $r \mathrm{~cm}$.
(a) Write down the value of $r$.

$$
\text { Answer } r=
$$

(b) Calculate $x$.

$$
\text { Answer } x=
$$

$14 \quad P$ and $Q$ are points on the circle centre $O$ with radius 4 cm .
$P \hat{O} Q=130^{\circ}$.

(i) Calculate the area of triangle $P O Q$.
(ii) Calculate the area of the major segment, shown unshaded in the diagram.
$\qquad$ $\mathrm{cm}^{2}$
15


The diagram shows a sector $A O B$ of a circle with centre $O$ and radius 6 cm . The angle of the sector is $310^{\circ}$.
(a) Calculate the total perimeter of the sector.
cm [3]
(b) Calculate the area of the sector.

$A D$ and $B C$ are arcs of circles with centre $O$.
$A$ is a point on $O B$, and $D$ is a point on $O C$.
$O A=20 \mathrm{~cm}$ and $A B=25 \mathrm{~cm}$.
$A \hat{O} D=150^{\circ}$.
(a) Calculate the perimeter of the shaded shape $A B C D$.
cm [3]
(b) Calculate the area of the shaded shape $A B C D$.
$\mathrm{cm}^{2}$ [3]
(c) The shape $A B C D$ is used to make a lampshade by joining $A B$ and $D C$.


Calculate the radius, $r \mathrm{~cm}$, of the circular top of the lampshade.

