1(i)	Venn diagram completed correctly		2	B1 fo	or 2 values correct
	$F = \begin{bmatrix} 7 & 3 & 5 \\ 4 & 1 & 0 \\ 3 & 2 \end{bmatrix}$				
1(ii)	$\frac{1}{30}$ oe		2	M1 f	for $\frac{5}{25} \times \frac{4}{24}$ oe
1(iii)	$\frac{45}{21}$ oe nfww		3		5 10 9
	91			M2 f	for $\frac{3}{15} \times \frac{10}{14} \times \frac{3}{13} \times k$ where k is 1, 2 or
				5 00	5 10 0
				or M	1 for $\frac{5}{15} \times \frac{10}{14} \times \frac{9}{13}$ seen and spoilt or
		C		$\frac{a}{x} \times \frac{a}{x}$	$\frac{b}{x-1} \times \frac{c}{x-2} [\times k] \text{ where } x = n(theirF)$
				$\frac{and}{k}$ is 1	, 2 or 3
	2			After	0 scored, SC1 for answer $\frac{4}{9}$ oe
2(a)	0.35 oe			2	M1 for 1 – (0.15 + 0.3 + 0.2) oe
					or B1 for 0.65 oe seen
2(b)	45			1	
3(a)	$\frac{28}{200}$ oe	1			
3(b)	$\frac{165}{200}$ oe	2	Μ	[1 for]	1, 2, 3, 5 soi
	200		А	fter 0 s	scored, SC1 for $\frac{114}{200}$ oe
3(c)	810	2	Μ	1 for	$\frac{19+35}{200}$ [×3000] oe
			01	B1 fo	200 r 810 seen

4(a)	$\frac{7}{9}$ oe		1	
4(b)	$\frac{1}{9}$ or $\frac{8}{72}$ oe nfww		3	M2 for $\frac{3}{9} \times \frac{2}{8} + \frac{2}{9} \times \frac{1}{8}$ oe or M1 for $\frac{3}{9} \times \frac{2}{8}$ or $\frac{2}{9} \times \frac{1}{8}$ seen If 0 scored, SC1 for answer $\frac{13}{81}$ or $\frac{8}{81}$
5(a)(i)a	$\frac{1}{8}$ oe	1		
5(a)(i)b	$\frac{5}{8}$ oe	1		
5(a)(ii)	$\frac{9}{64}$ oe	2	M	1 for $\frac{3}{8} \times \frac{3}{8}$
5(b)	$\frac{13}{40}$ oe	3	M2 or Af	2 for $\frac{7}{16} \times \frac{6}{15} + \frac{6}{16} \times \frac{5}{15} + \frac{3}{16} \times \frac{2}{15}$ oe M1 for $\frac{7}{16} \times \frac{6}{15}$ or $\frac{6}{16} \times \frac{5}{15}$ or $\frac{3}{16} \times \frac{2}{15}$ der 0 scored, SC1 for answer $\frac{47}{128}$
6(a)	$\frac{6}{35}$ oe		1	
6(b)	0 oe		1	
6(c)	$\frac{17}{35}$ oe		2	M1 for $\frac{3}{7} \times \frac{3}{5}$ oe or $\frac{4}{7} \times \frac{2}{5}$ oe
7(a)	Correct tree diagram with four branches added and the five correct probabilities $\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, 1, [0]$	2	B1 2 c	for at least two second branches drawn and or 3 probabilities completed correctly
7(b)	0	1		

8(a)	$\frac{2}{6}$ on first branch		2	B1	for	two or three completed correctly
	$\frac{2}{5}, \frac{4}{5}, \frac{1}{5}$ on second set					
8(b)	$\frac{14}{30}$ oe		2	M1	for	$\frac{4}{6} \times \frac{3}{5}$ oe or their $\frac{2}{6} \times their \frac{1}{5}$ oe
9(a)	$\frac{4}{7}$			1		
	$\frac{2}{7}$ (black) and $\frac{5}{7}$ (white) with two branches and both labels			1		
9(b)	$\frac{13}{35}$ oe			2	FT	$\frac{\frac{3}{5} \times \frac{3}{7} + \frac{2}{5} \times (their\frac{2}{7})}{\frac{3}{5} \times \frac{3}{7}}; \text{ or for } \frac{2}{5} \times (their\frac{2}{7})$
10(i)	$\frac{21}{60}$, $\frac{7}{20}$, $\frac{126}{360}$, 0.35 or 35%			1		
10(ii)	$\frac{210}{3540}$ oe			2 1	M1 f	or $\frac{15}{60} \times \frac{14}{59} [\times 2]$ C1 for $\left(\frac{15}{60}\right)^2$ or answer $\frac{1}{16}$ oe
11(a)	Probabilities 0.7 and 0.3 on the correct branches	3		1		
11(b)(i)	0.49 oe			1		
11(b)(ii)	0.42 oe			1	FT pro	from their diagram, provided their diagram babilities are less than 1, and $0 < ans. < 1$.
12(a)	Correctly completed tree diagras $\frac{n-3}{n-1}$ oe $\frac{n-3}{n}$ oe $\frac{n-4}{n-1}$ oe	am			2	C1 for one correct probability correctly positioned
12(b)	$\frac{3}{n} \times \frac{2}{n-1} = \frac{1}{15}$			I	M1	
	Correct rearrangement with at l one further step to reach $n^2 - n - 90 = 0$	least			A1	

12(c)	10		2 B1 for solutions 10, -9 seen or M1 for $(n - 10)(n + 9) [= 0]$ $1 \pm \sqrt{(-1)^2 - 4 \times 1 \times -90}$		
				or 1	for 2×1 or better
13 (a)	$\frac{2}{10}$,	$\frac{2}{9}, \frac{8}{9}, \frac{1}{9}$ correctly positioned	1		
(b) (i)	$\frac{56}{90}$	0e	1*	¢	
(ii)	$\frac{32}{90}$	oe	2ft	*	M1 for $\frac{8}{10} \times \frac{2}{9} + \frac{2}{10} \times \frac{8}{9}$ ft <i>their</i> tree diagram with fractions < 1
14(b)(i)	2.06[2	25] or 2.063 or $2\frac{1}{16}$	2	N ([×	11 for 0×24] + 1 × 30 + 2 × 50 + 3 × 32 + 4 16 + 5 × 8) ÷ 160
14(b)(ii)	$\frac{24}{160}$	be	1		
14(b)(iii)	$\frac{29}{848}$	be	2	N A	If for $\frac{30}{160} \times \frac{29}{159}$ fter M0, SC1 for answer $\frac{9}{256}$ oe
15(b)(i)	$\frac{1}{8}$ oe			1	
15(b)(ii)	$\frac{1}{40}$ o	e NGS		2	M1 for $\frac{k}{16} \times \frac{k-1}{15}$ or SC1 for answer $\frac{9}{256}$
16(c)	$\frac{9}{64}$			2	M1 for $\frac{3}{8} \times \frac{3}{8}$
17	$\frac{7}{11}$ of	;		1	
18 (i)		$\frac{2}{4}$ oe	1		
(ii)		$\frac{2}{20}$ oe	1		
(iii)		$\frac{12}{20}$ oe	2	B1	for $\frac{3}{5} \times \frac{2}{4}$ or $\frac{2}{5} \times \frac{3}{4}$ seen
(iv)		$\frac{18}{60}$ oe	2	$\frac{B1}{\frac{3}{5}}$	for any correct sequence of three coins, $\times \frac{2}{4} \times \frac{1}{3}$ or $\frac{2}{5} \times \frac{3}{4} \times \frac{1}{3}$ or $\frac{2}{5} \times \frac{1}{4} \times \frac{3}{3}$

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19 (a)	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		1		
(c)	$\frac{4}{12}$ oe ; or FT <i>their table</i>		1√^		
20 (a)	$\frac{1}{4}$ $\frac{1}{4}$ $\frac{1}{4}$ $\frac{1}{4}$ $\frac{1}{4}$			1	
(b) () 5 6 7 8			1	
(i) $\left(\frac{15}{16}\right) \frac{10}{16} \frac{3}{16} = 0$ or FT from <i>their (bi)</i> table			1 √	_0
(c)	$\frac{7}{16}$ oe WWW			2*	M1 for $\frac{1}{4} \times ($ sum of (bii) table) oe, or for $\sum x y$, attempt, where <i>x</i> and <i>y</i> are corresponding values in the two tables
21 (a)	$\frac{28}{80}$ oe			1	
(b) (i) $\frac{992}{6320}$ oe	0		2 N	M1 for $2 \times \frac{32}{80} \times \frac{31}{79}$ or $\frac{32}{80} \times \frac{31}{80}$
(i) $\frac{64}{6320}$ oe	ク		2 N	M1 for $\frac{4}{80} \times \frac{8}{79}$ or $2 \times \frac{4}{80} \times \frac{8}{80}$
22	$\frac{2}{5}$ cao	2	B1 for $\frac{8}{-}$ After 0 s	$\frac{+10+2}{100}$ cored, S	$\frac{22}{300}$ oe SC1 for answer $\frac{17}{25}$
23(a)	$\frac{12-x}{11}, \frac{x}{11}, \frac{11-x}{11}$ oe correctly placed	2	B1 for or	ne corre	ct
23(b)	$\frac{x(12-x)}{66}$ oe simplified single fraction final answer	3	M2 for - <u>1</u> or M1 fo	$\frac{x}{2} \times thei$ r $\frac{x}{12} \times thei$	$r\frac{12-x}{11} + \frac{12-x}{12} \times their\frac{x}{11}$ heir $\frac{12-x}{11}$ or $\frac{12-x}{12} \times their\frac{x}{11}$

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23c	$\frac{x}{12} \times \frac{x-1}{11} = \frac{14}{33}$	M1				
	$x^{2} - x - 56 = 0$ oe Alternative: $x(x - 1) = 56$ cao	A1				
	(x-8)(x+7) = 0 or $[x=] \frac{-(-1) \pm \sqrt{(-1)^2 - 4 \times 1 \times -56}}{2 \times 1}$ Alternative: $8(8-1) = 56$ soi	M1	Dep on M1 FT factorisation/use of formula for <i>their</i> 3-term quadratic			
24	0.13		2	M1 for $1 - (0.15 + 0.3 + 0.42)$ or B1 for 0.87 seen		
25(a)(ii)	23, 43, 53		2	B1 for three correct and one incorrect or for two correct and none incorrect		
25(a)(iii)	0.3 or $\frac{6}{20}$ oe		2	B1 for $\frac{6}{k}$ where <i>k</i> is an integer > 6 or for 24, 32, 36, 52, 56 and 64 identified		
25(b)(i)	35, 22, 38)		
25(b)(ii)	$\frac{77}{200}$ or 0.385	0	2	B1 for $\frac{46+31}{k}$ where <i>k</i> is an integer > 77		
		5		or SC1 for $\frac{105}{200}$ or 0.525		
25(b)(iii)	Large sample		B1			
	$\frac{46}{200} \text{ is a lot bigger than } \frac{1}{6} \text{ oe or}$ $\frac{22}{200} \text{ is a lot smaller than } \frac{1}{6} \text{ oe}$		B1			