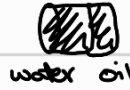


# CH6 FLUID DYNAMICS.

- flow of fluids.
- Interaction of fluids.



## Fluid:

- Anything that flows.
- liquids, gases.

Hydrostatics → fluids at rest.

## Density ( $\rho$ )

$$\rho = \frac{\text{mass (M)}}{\text{Volume (V)}}$$

## Pressure (P) → (Scalar).

→ Normal force exerted by the fluid on unit area which contains the point.

$$P = \frac{F}{A}$$



→ Compressive in nature.

$$[P] = \left[ \frac{N}{m^2} \right] \rightarrow \text{Pascal (Pa)}$$

$$\left\{ \begin{array}{l} 1 \text{ atm} = 1.013 \times 10^5 \text{ Pa} \\ 1 \text{ bar} = 10^5 \text{ Pa} \end{array} \right\} \quad \left\{ 1 \text{ atm} = 1.013 \text{ bar} \right\}$$

## Thrust:

→ Normal force on surface in contact.

$$\text{Thrust} = P \times A$$

## Pascal's law.

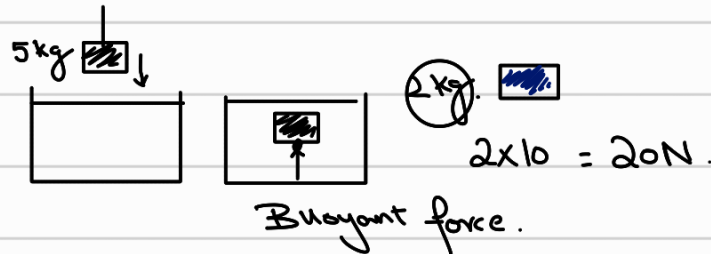
→ Pressure exerted at a point is invariant in all directions.

$$\frac{F_1}{F_2} = \frac{A_1}{A_2}$$



## Archimedes Principle.

→ A body submerged in a fluid feels upward force equal in magnitude to weight of displaced fluid.



## Buoyancy (B).

→ Upward thrust fluid exerts on submerged fluid.

→ It acts on a point on a body known as centre of buoyancy / floatation.

$$B = V\rho g.$$

## Laws of floatation.

- 1)  $W > W'$  → Sink
- 2)  $W = W'$  → floats. immersed
- 3)  $W < W'$  → floats on surface. / partly immersed.

## Viscous Drag $\Rightarrow$ Stokes law.

Viscosity: Measure of force req. to slide layers of liquid over.

$$[\eta] = \text{kgm}^{-1}\text{s}^{-1} = [\text{ML}^{-1}\text{T}^{-1}]$$

$\rightarrow$  Resistance  $\Rightarrow$  Drag force.

$\hookrightarrow$  • Velocity

• Geometric profile.

from Stokes law:

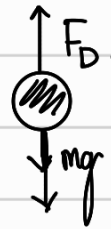
$$F_D = 6\pi\eta r v$$



## Terminal Velocity.

$$F_D = mg$$

$$\Rightarrow v_t = \text{const}$$

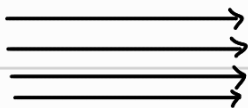


Terminal velocity.

$$v_t = \left( \frac{g}{6\pi\eta r} \right) m = \left( \frac{2\rho g}{9\eta} \right) r^2$$

## Fluid flow.

LAMINAR  
(Streamline)



:

TURBULENT.



## Ideal fluid.

$$\rightarrow \eta = 0$$

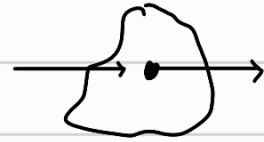
$$\rightarrow \rho = \text{Const}$$

$\rightarrow$  Steady motion.

## Equation of Continuity.

$$\rho A v = \text{Const.} = \frac{\text{mass}}{\text{time}}$$

$$\rho_1 A_1 v_1 = \rho_2 A_2 v_2$$



## Bernoulli's Eq.

$$P + \frac{1}{2} \rho v^2 + \rho g h = \text{Const.}$$

Pressure energy,  $Pv$

Kinetic energy:  $\frac{1}{2} m v^2 \Rightarrow \frac{1}{2} \rho v^2$  per vol.

Potential energy:  $mgh \Rightarrow \rho g h$  per vol.