

Diffraction grating theory

02 February 2021 16:01

CONCEPT OF DIFFRACTION GRATING

29 January 2021 14:59

- A diffracting grating is an optical instrument constructed either using glass or Plastic
- This instrument has many microscopic slits on it, so that when light is allowed to fall on this instrument (diffraction grating), diffraction occurs, causing the light to spread.
- If a screen is positioned in the background (as shown on the next slide), then the spreading of light can be displayed on the screen.
- The angle through which the light spread is denoted as θ (it is generally measured from the central line). This angle θ can be worked out using the equation

$$d \sin \theta = n \lambda$$

where λ = wavelength of light

θ = angle through which the light diffracts

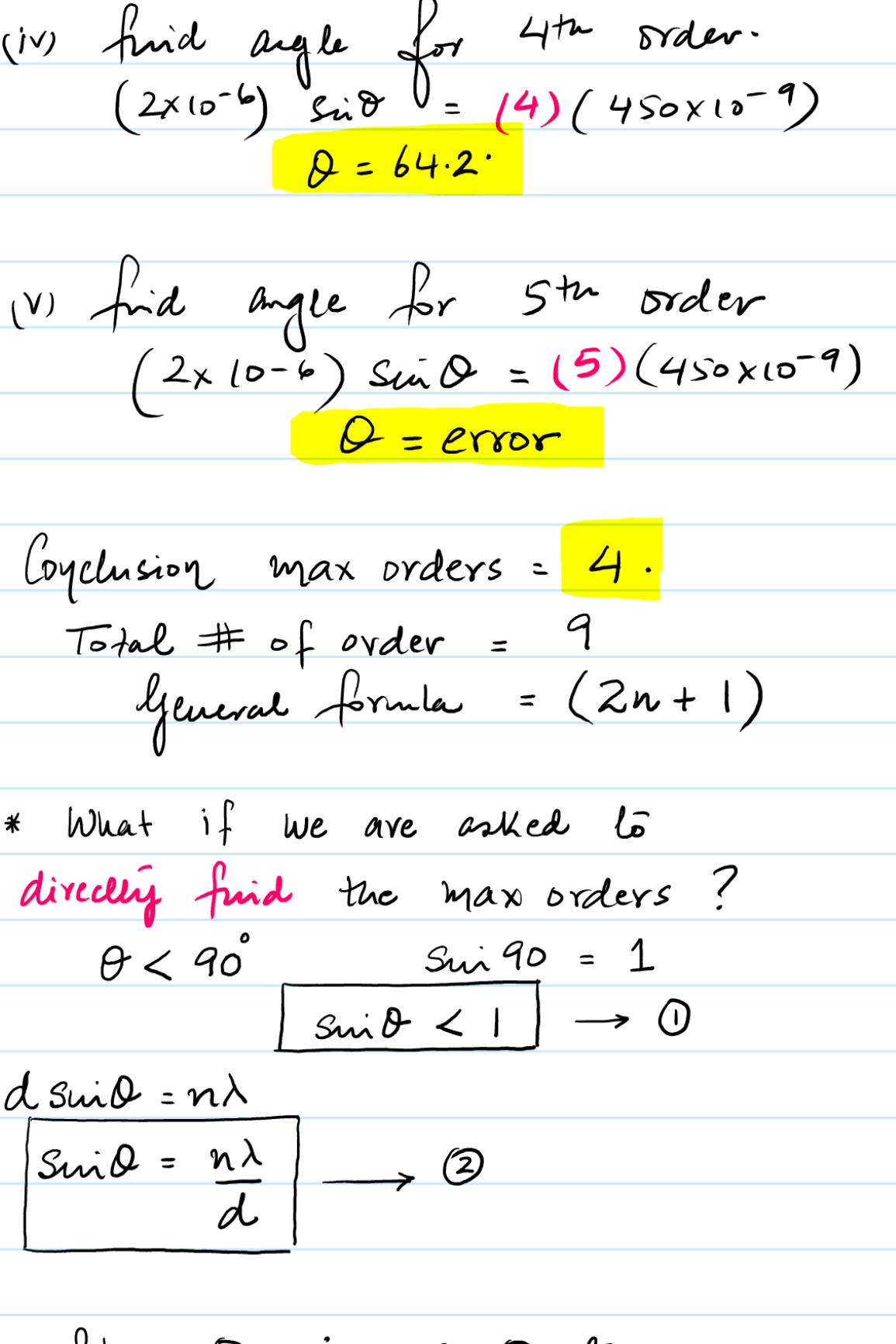
n denotes the number of order i.e.

$n = 1, 2, 3, 4, 5$ etc &

d is a constant known as the grating spacing. (This constant value is provided by the manufacturer in unit of m)

Simplified diagram for a diffraction grating.

diffraction grating.



$$d \sin \theta = n \lambda$$

Q: A certain diffraction grating has a grating spacing (d) = $2.0 \times 10^{-6} \text{ m}$.

Light of wavelength (λ) = 450 nm is allowed to fall onto the grating

(i) find angle for 1st order

$$d \sin \theta = n \lambda$$

$$(2 \times 10^{-6}) \sin \theta = (1)(450 \times 10^{-9})$$

$$\theta = 13^\circ$$

(ii) find angle for 2nd order

$$(2 \times 10^{-6}) \sin \theta = (2)(450 \times 10^{-9})$$

$$\theta = 26.7^\circ$$

(iii) find angle for 3rd order

$$(2 \times 10^{-6}) \sin \theta = (3)(450 \times 10^{-9})$$

$$\theta = 42.5^\circ$$

(iv) find angle for 4th order

$$(2 \times 10^{-6}) \sin \theta = (4)(450 \times 10^{-9})$$

$$\theta = 64.2^\circ$$

(v) find angle for 5th order

$$(2 \times 10^{-6}) \sin \theta = (5)(450 \times 10^{-9})$$

$$\theta = \text{error}$$

Conclusion max orders = 4.

Total # of order = 9

General formula = $(2n + 1)$

* What if we are asked to directly find the max orders?

$$\theta < 90^\circ \quad \sin 90^\circ = 1$$

$$\sin \theta < 1 \rightarrow ①$$

$$d \sin \theta = n \lambda$$

$$\sin \theta = \frac{n \lambda}{d} \rightarrow ②$$

replace ② into eq ① to get a formula which "directly" gives you max order

g. formula

$$\frac{n \lambda}{d} < 1$$

$$\frac{n(450 \times 10^{-9})}{(2.0 \times 10^{-6})} < 1$$

$$n < 4.44 \therefore n = 4$$

Q: The experiment is now repeated using a different light whose wavelength $\lambda = 620 \text{ nm}$

(i) find angle for 1st order

$$(2.0 \times 10^{-6}) \sin \theta = (1)(620 \times 10^{-9})$$

$$\theta = 18.1^\circ$$

(ii) find angle for 2nd order

$$(2.0 \times 10^{-6}) \sin \theta = (2)(620 \times 10^{-9})$$

$$\theta = 38.3^\circ$$

(iii) find angle for 3rd order

$$(2.0 \times 10^{-6}) \sin \theta = (3)(620 \times 10^{-9})$$

$$\theta = 68.4^\circ$$

(iv) find angle for 4th order

$$\theta = \text{error}$$

$$d \sin \theta = n \lambda$$

$$\sin \theta = \frac{n \lambda}{d}$$

$$\sin \theta \propto \lambda \text{ as } \lambda \uparrow$$

$$\lambda \uparrow, \text{ the angle } \theta \text{ will also } \uparrow$$

$$d \sin \theta = n \lambda$$

$$\sin \theta \propto \frac{1}{\lambda}$$

$$n \propto \frac{1}{\lambda} \text{ as } \lambda \uparrow, \text{ the}$$

number of orders will ↓

Q: Cal. the angular separation in the 1st order for the two wavelength ($\lambda = 450 \text{ nm}$ & $\lambda = 620 \text{ nm}$)

$$\theta_1 = 13^\circ \quad \theta_2 = 18.1^\circ$$

$$\text{Angular separation} = 5.1^\circ$$

[difference b/w the angles in a particular order]

Q: angular separation in the 2nd order

$$\theta_1 = 26.7^\circ \quad \theta_2 = 38.3^\circ$$

$$\text{Angular separation} = 11.6^\circ$$

Q: angular separation in the 3rd order

$$\theta_1 = 42.5^\circ \quad \theta_2 = 68.4^\circ$$

$$\text{Angular separation} = 25.9^\circ$$

Q: angular separation in the 4th order

$$\theta_1 = 64.2^\circ \quad \theta_2 = \text{error}$$

not possible.

Conclusion: Angular Separation INCREASES as the number of orders increase

∴ we can conclude that

MAXIMUM ANGULAR SEPARATION WILL

ALWAYS ARISE IN THE HIGHEST ORDER.