Matter

Deformation of Solids

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Syllabus content

| Section | | AS | A2 |
|------------|-------------------------------------|----|----|
| III Matter | 9. Phases of matter | ~ | |
| | 10. Deformation of solids | ~ | |
| | 11. Ideal gases | | ~ |
| | 12. Temperature | | ~ |
| | 13. Thermal properties of materials | | ~ |

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Section III: Matter

Recommended prior knowledge

Candidates should be able to describe matter in terms of particles, with a qualitative understanding of their behaviour.

Syllabus content

| 10. Deformation of solids | | | | |
|---------------------------------------|---|--|--|--|
| Content | Learning outcomes | | | |
| 10.1 Stress, strain | Candidates should be able to: | | | |
| 10.2 Elastic and plastic behaviour | (a) appreciate that deformation is caused by a force and that, in one dimension, the deformation can be tensile or compressive | | | |
| | (b) describe the behaviour of springs in terms of load, extension, elastic limit, Hooke's law and the spring constant (i.e. force per unit extension) | | | |
| | (c) define and use the terms stress, strain and the Young modulus | | | |
| | (d) describe an experiment to determine the Young modulus of a metal in the form of a wire | | | |
| | (e) distinguish between elastic and plastic deformation of a material | | | |
| | (f) deduce the strain energy in a deformed material from the area under the force-extension graph | | | |
| | (g) demonstrate knowledge of the force-extension graphs for typical ductile, brittle and polymeric materials, including an understanding of ultimate tensile stress. | | | |

Deformation of Solids

Definitions:

- **Stress**: is a measure of the force required to cause a particular deformation.
- **Strain**: is a measure of the degree of deformation.
- Elastic Modulus: the ratio of stress to strain Elastic Modulus = $\frac{\text{stress}}{\text{strain}}$

The elastic modulus determines the amount of force required per unit deformation. A material with large elastic modulus is difficult to deform, while one with small elastic modulus is easier to deform.

Deformation of Solids : Changes in Length

Changes in Length

To stretch or compress something you must exert a force on it at either end.

Tensile Stress is the force per unit crosssectional area exerted on the ends.

(Note the surface whose area we wish to measure is perpendicular to the force.)

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Changes in Length (continued)



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Hooke's Law

- Hooke's Law states that, for relatively small deformations of an object, the displacement of the deformation is directly proportional to the deforming force or load.
- > Forces can cause objects to **deform**.

The way in which an object deforms depends on its dimensions, the material it is made of, the size of the force and direction of the force. For Live Classes, Recorded Lectures, Notes & Past Papers visit: www.megalecture.com If you measure how a spring stretches (extends its length) as you apply increasing force and plot extension (e) against force (F);



This shows that Force is proportional to extension. This is Hooke's law. It can be written as:

F = ke

Where:.

F = tension acting on the spring.

e is extension = (I-I_o); I is the stretched length and I_o is original length, and.

k is the gradient of the graph above. It is known as the spring constant.

The above equation can be rearranged as

$$k = \frac{F}{e}$$

Spring constant = Applied force/extension

The spring constant k is measured in Nm⁻¹ because it is the force per unit extension.

The value of k does not change unless you change the shape of the spring or the material that the spring is made of.

A stiffer spring has a greater value for the spring constant

In fact, a vast majority of materials obey Hooke's law for at least a part of the range of their deformation behaviour. (e.g. glass rods, metal wires).



In the diagram above, if you extend the spring beyond point P, and then unload it completely; it won't return to its original shape. It has been permanently deformed. We call this point the **elastic limit** - the limit of **elastic behaviour**.

If a material returns to its original size and shape when you remove the forces stretching or deforming it (reversible deformation), we say that the material is demonstrating **elastic behaviour**.

If deformation remains (irreversible deformation) after the forces are removed then it is a sign of **plastic behaviour.** https://www.youtube.com/c/MegaLecture

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Calculating stress

• Stress

- Stress is a measure of how strong a material is. This is defined as how much force the material can stand without undergoing some sort of physical change.
- > Hence, the formula for calculating stress is the same as the formula for calculating pressure: $\sigma = \frac{F}{A}$

where σ is stress (in Newtons per square metre but usually Pascals, commonly abbreviated Pa).

Calculating strain

Stress causes strain.

- Applying force on an object causes it to stretch. Strain is a measure of how much an object is being stretched.
 Strain is the ratio of extension to the original length.
- The formula for strain is: $\epsilon = \frac{\Delta l}{l_0} = \frac{l l_0}{l_0} = \frac{l}{l_0} 1$
- Where l₀ is the original length of some bar being stretched, and I is its length after it has been stretched. ΔI is the extension of the bar, the difference between these two lengths.

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- Young's Modulus is a measure of the stiffness of a material. It is defined as the ratio of stress to strain. It states how much a material will stretch (i.e., how much strain it will undergo) as a result of a given amount of stress.
- The formula for calculating it is: $E = \frac{o}{\epsilon}$
- Strain is unit less so Young's Modulus has the same units as stress, i.e. N/m² or Pa.

| Quantity | Equation | Symbol | Units |
|---------------|--|--------------------|---|
| Stress | tension/cross sectional area = F / A | (sigma) σ | N m ⁻² = Pa |
| Strain | extension per original length = ΔL/L | (epsilon) E | no units (because it's a ratio of two lengths) |
| Young Modulus | stress/strain | E | N m ⁻² = Pa |

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Tensile strength & Yield strength

Tensile Strength

Tensile strength which is also known as **Ultimate tensile strength** or **ultimate strength** is the maximum stress that a material can withstand while being stretched or pulled before failing or breaking. Tensile strength is the opposite of compressive strength and the values can be quite different.

> Yield Stress or Yield strength or Yield point

The yield stress is the level of stress at which a material will deform permanently. This is also known as Yield strength or Yield point. Prior to the yield point the material will deform elastically and will return to its original shape when the applied stress is removed. It can be experimentally determined from the slope of a stressstrain curve created during tensile tests conducted on a sample of the material.

- The value of the Young's Modulus is quoted for various materials but the value is only approximate.
- This is because Young's Modulus can vary considerably depending on the exact composition of the material.
- For example, the value for most metals can vary by 5% or more, depending on the precise composition of the alloy and any heat treatment applied during manufacture.
- If a big force only produces a small extension then the material is 'stiff' and E is a big value. If a force produces a big extension then the material is not very stiff - it is easier to stretch and the value of E will be smaller.

For Live Classes, Recorded Lectures, Notes & Past Papers visit: An experiment to wwwere support for Young's Modulus



An experiment to measure the Young's Modulus (continued)

- To minimize errors the control wire is the same length, diameter and material as the test wire. This means that **errors due to expansion (from the surroundings)** during the experiment are avoided as the test wire and control wire would both expand by the same amount and the scale would adjust position and eliminate the error.
- The wire must have **no kinks** in it otherwise there will be big extensions due to the wire straightening out rather than just stretching.
- Care must be taken that the **limit of proportionality** is **not exceeded**. This can be checked by removing the load after each addition of the weight. If the limit has not been exceeded the wire should return to the length it was before the weight was added.
- The wire is as long as possible (usually about 2m long) and it is as thin as possible so that as big an extension as possible can be recorded. (A typical extension for a 5N loading will be 1mm).

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- The test wire is loaded with the weight hanger so that it is taut before readings are taken.
- The vernier scale is read and the result recorded as addition of ON.
- Weights usually starting at ON and increasing in 5N increments to 100N - are then added and a reading of the vernier scale is taken at each addition.
- The experiment should be repeated twice and any anomalous results repeated and checked.

An experiment to measure the Young's Modulus (continued)

- A graph of load against extension is plotted. It should be a straight line through the origin (provided measurements are accurate).
- The gradient of that graph will be F/e. Using that value we can find the value of Young's Modulus for the wire.

$$E = \frac{\text{stress}}{\text{strain}}$$

$$= \frac{F}{A} = \frac{F\ell}{A e}$$

$$= \frac{e}{\ell} \qquad A e$$

$$= \ell/A \times \text{Gradient}$$

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Proportionality limit and Elastic limit

Maximum amount a material can be stretched by a force and still (or may) return to its original shape depends on the material.

• Yield point or Yield strength

The point where there is a large permanent change in length with no extra load force.

yield point :- interface between elasticity and plasticity

- Elastic limit up to which material can sustain the load and return back to its original position.
- Although these two points are so close to each other it can be treated as one, on a case to case basis.
- > It depends upon material whether it's brittle or ductile.



For Live Classes, Recorded Lectures, Notes & Past Papers visit: Explaining Graph in the previous slide.....

- The stretching behavior is summarized in a stress-strain graph in the previous slide. As the stress is increased initially Hooke's Law is obeyed the stress-strain relationship for the wire is linear & elastic.
- Just before the plastic region is reached we get the limit of proportionality - beyond this for a small section we see non-linear behaviour but the stretching is still elastic.
- After the *yield strength*, the material enters the plastic deformation region, which means that the stretch of the wire is permanent. (For example, if the wire is stressed to point A on the graph and the stress is slowly decreased, the stress-strain curve follows the dotted line instead of the original curve to point B and there is a permanent extention when all stress is removed.) At the facture point the wire snaps.
- Differences in the shape and limits of the stress-strain diagram determines whether a material is considered ductile or brittle, elastic or plastic.

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Strength, Ductility & Toughness





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- Whenever we apply force to an object, it will cause deformation. If the deformation caused is within the elastic limit, the work done in deforming the object is stored within it as potential energy. We call this (elastic) 'strain energy'. It can be released from the object by removing the applied force.
- The strain energy then performs work in undeforming the object and returns to its original state.

Force-extension graphs for typical ductile, brittle and polymeric materials, including an understanding of ultimate tensile stress.



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Types of materials



tensile stress to the tensile strain if the limit of proportionality has not been exceeded.



Its dimension is given by $[Y] = \frac{[F_{\perp}][l_{\theta}]}{[A][e]} = ML^{-1}T^{-2}$

Types of materials

 The unit of Young's modulus is kg m⁻¹ s⁻² @ N m⁻² @ Pa.

