

**Q1.**

- |   |  |                                 |
|---|--|---------------------------------|
| 7 | (i) Obtain modulus $\sqrt{8}$<br>Obtain argument $\frac{1}{4}\pi$ or $45^\circ$  | B1<br>B1 [2]                    |
|   | (ii) Show 1, $i$ and $u$ in relatively correct positions on an Argand diagram<br>Show the perpendicular bisector of the line joining 1 and $i$<br>Show a circle with centre $u$ and radius 1<br>Shade the correct region | B1<br>B1<br>B1<br>B1 [4]        |
|   | (iii) State or imply relevance of the appropriate tangent from $O$ to the circle<br>Carry out complete strategy for finding $ z $ for the critical point<br>Obtain answer $\sqrt{7}$                                     | B1 $\checkmark$<br>M1<br>A1 [3] |

**Q2.**

- |   |  |  |
|---|--|--|
| 8 | (a) <i>EITHER</i> : Substitute $1+i\sqrt{3}$ , attempt complete expansions of the $x^3$ and $x^2$ terms<br>Use $i^2 = -1$ correctly at least once<br>Complete the verification correctly<br>State that the other root is $1-i\sqrt{3}$<br><i>OR1</i> : State that the other root is $1-i\sqrt{3}$<br>State quadratic factor $x^2 - 2x + 4$<br>Divide cubic by 3-term quadratic reaching partial quotient $2x + k$<br>Complete the division obtaining zero remainder<br><i>OR2</i> : State factorisation $(2x + 3)(x^2 - 2x + 4)$ , or equivalent<br>Make reasonable solution attempt at a 3-term quadratic and use $i^2 = -1$<br>Obtain the root $1+i\sqrt{3}$<br>State that the other root is $1-i\sqrt{3}$ | M1<br>B1<br>A1<br>B1<br>B1<br>M1<br>A1<br>B1<br>M1<br>A1<br>B1 [4] |
|   | (b) Show point representing $1+i\sqrt{3}$ in relatively correct position on an Argand diagram<br>Show circle with centre at $1+i\sqrt{3}$ and radius 1<br>Show line for $\arg z = \frac{1}{3}\pi$ making $\frac{1}{3}\pi$ with the real axis<br>Show line from origin passing through centre of circle, or the diameter which would contain the origin if produced<br>Shade the relevant region  | B1<br>B1 $\checkmark$<br>B1<br>B1<br>B1 $\checkmark$ [5]           |

**Q3.**

- 8 (i) Either: Multiply numerator and denominator by  $(1 - 2i)$ , or equivalent M1  
 Obtain  $-3i$  A1  
 State modulus is 3 A1  
 Refer to  $u$  being on negative imaginary axis or equivalent and confirm argument as  $-\frac{1}{2}\pi$  A1
- Or: Using correct processes, divide moduli of numerator and denominator M1  
 Obtain 3 A1  
 Subtract argument of denominator from argument of numerator M1  
 Obtain  $-\tan^{-1}\frac{1}{2} - \tan^{-1}2$  or  $-0.464 - 1.107$  and hence  $-\frac{1}{2}\pi$  or  $-1.57$  A1 [4]
- (ii) Show correct half-line from  $u$  at angle  $\frac{1}{4}\pi$  to real direction B1  
 Use correct trigonometry to find required value M1  
 Obtain  $\frac{3}{2}\sqrt{2}$  or equivalent A1 [3]
- (iii) Show, or imply, locus is a circle with centre  $(1 + i)u$  and radius 1 M1  
 Use correct method to find distance from origin to furthest point of circle M1  
 Obtain  $3\sqrt{2} + 1$  or equivalent A1 [3]

#### Q4.

- 7 (i) Use the quadratic formula, completing the square, or the substitution  $z = x + iy$  to find a root and use  $i^2 = -1$  M1  
 Obtain final answers  $-\sqrt{3} \pm i$ , or equivalent A1 [2]
- (ii) State that the modulus of both roots is 2 B1√  
 State that the argument of  $-\sqrt{3} + i$  is  $150^\circ$  or  $\frac{5}{6}\pi$  (2.62) radians B1√  
 State that the argument of  $-\sqrt{3} - i$  is  $-150^\circ$  (or  $210^\circ$ ) or  $-\frac{5}{6}\pi$  (-2.62) radians or  $\frac{7}{6}\pi$  (3.67) radians B1√ [3]
- (iii) Carry out an attempt to find the sixth power of a root M1  
 Verify that one of the roots satisfies  $z^6 = -64$  A1  
 Verify that the other root satisfies the equation A1 [3]

#### Q5.

- 4 (i) Either Expand  $(1 + 2i)^2$  to obtain  $-3 + 4i$  or unsimplified equivalent B1  
 Multiply numerator and denominator by  $2 - i$  M1  
 Obtain correct numerator  $-2 + 11i$  or correct denominator 5 A1  
 Obtain  $-\frac{2}{5} + \frac{11}{5}i$  or equivalent A1
- Or Expand  $(1 + 2i)^2$  to obtain  $-3 + 4i$  or unsimplified equivalent B1  
 Obtain two equations in  $x$  and  $y$  and solve for  $x$  or  $y$  M1  
 Obtain final answer  $x = -\frac{2}{5}$  A1  
 Obtain final answer  $y = \frac{11}{5}$  A1 [4]
- (ii) Draw a circle M1  
 Show centre at relatively correct position, following their  $u$  A1✓  
 Draw circle passing through the origin A1 [3]

### Q6.

- 10 (a) EITHER: Eliminate  $u$  or  $w$  and obtain an equation in  $w$  or in  $u$  M1  
 Obtain a quadratic in  $u$  or  $w$ , e.g.  $u^2 - 4iu - 5 = 0$  or  $w^2 + 4iw - 5 = 0$  A1  
 Solve a 3-term quadratic for  $u$  or for  $w$  M1
- OR1: Having squared the first equation, eliminate  $u$  or  $w$  and obtain an equation in  $w$  or  $u$  M1  
 Obtain a 2-term quadratic in  $u$  or  $w$ , e.g.  $u^2 = -3 + 4i$  A1  
 Solve a 2-term quadratic for  $u$  or for  $w$  M1
- OR2: Using  $u = a + ib$ ,  $w = c + id$ , equate real and imaginary parts and obtain 4 equations in  $a, b, c$  and  $d$  M1  
 Obtain 4 correct equations A1  
 Solve for  $a$  and  $b$ , or for  $c$  and  $d$  M1  
 Obtain answer  $u = 1 + 2i$ ,  $w = 1 - 2i$  A1  
 Obtain answer  $u = -1 + 2i$ ,  $w = -1 - 2i$  and no other A1 [5]
- (b) (i) Show point representing  $2 - 2i$  in relatively correct position B1  
 Show a circle with centre  $2 - 2i$  and radius 2 B1✓  
 Show line for  $\arg z = -\frac{1}{4}\pi$  B1  
 Show line for  $\operatorname{Re} z = 1$  B1  
 Shade the relevant region B1 [5]
- (ii) State answer  $2 + \sqrt{2}$ , or equivalent (accept 3.41) B1 [1]

### Q7.

- 7 (a) State or imply  $3a+3bi+2i(a-bi)=17+8i$  B1  
 Consider real and imaginary parts to obtain two linear equations in  $a$  and  $b$  M1\*  
 Solve two simultaneous linear equations for  $a$  or  $b$  M1 (dep\*)  
 Obtain  $7-2i$  A1 [4]
- (b) Either Show or imply a triangle with side 2 B1  
 State at least two of the angles  $\frac{1}{4}\pi, \frac{2}{3}\pi$  and  $\frac{1}{12}\pi$  B1  
 State or imply argument is  $\frac{1}{4}\pi$  B1  
 Use sine rule or equivalent to find  $r$  M1  
 Obtain  $6.69e^{\frac{1}{2}\pi i}$  A1
- Or State  $y = x$ . B1  
 State  $y = \frac{1}{\sqrt{3}}x + 2$  or  $\frac{\sqrt{3}}{2} = \frac{x}{\sqrt{x^2 + (y-2)^2}}$  or  $\frac{1}{2} = \frac{y-2}{\sqrt{x^2 + (y-2)^2}}$  B1  
 State or imply argument is  $\frac{\pi}{4}$  B1  
 Solve for  $x$  or  $y$ . M1  
 Obtain  $6.69e^{\frac{1}{2}\pi i}$  A1 [5]

### Q8.

- 7 (i) Show that  $a^2 + b^2 = (a+ib)(a-ib)$  B1  
 Show that  $(a+ib-ki)^* = a-ib+ki$  B1 [2]
- (ii) Square both sides and express the given equation in terms of  $z$  and  $z^*$  M1  
 Obtain a correct equation in any form, e.g.  $(z-10i)(z^*+10i) = 4(z-4i)(z^*+4i)$  A1  
 Obtain the given equation A1  
 Either express  $|z-2i| = 4$  in terms of  $z$  and  $z^*$  or reduce the given equation to the form  $|z-u| = r$  M1  
 Obtain the given answer correctly A1 [5]
- (iii) State that the locus is a circle with centre  $2i$  and radius  $5$  B1 [1]

### Q9.

7	<p>(i) Substitute <math>x = -2 + i</math> in the equation and attempt expansion of <math>(-2 + i)^3</math>          Use <math>i^2 = -1</math> correctly at least once and solve for <math>k</math>          Obtain <math>k = 20</math></p> <p>(ii) State that the other complex root is <math>-2 - i</math></p>	<p>M1 M1 A1 [3]</p> <p>B1 [1]</p>
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<p>(iii) Obtain modulus <math>\sqrt{5}</math>          Obtain argument <math>153.4^\circ</math> or 2.68 radians</p> <p>(iv) Show point representing <math>u</math> in relatively correct position in an Argand diagram          Show vertical line through <math>z = 1</math>          Show the correct half-lines from <math>u</math> of gradient zero and 1          Shade the relevant region          [SR: For parts (i) and (ii) allow the following alternative method:          State that the other complex root is <math>-2 - i</math>          State quadratic factor <math>x^2 + 4x + 5</math>          Divide cubic by 3-term quadratic, equate remainder to zero and solve for <math>k</math>, or, using          3-term quadratic, factorise cubic and obtain <math>k</math>          Obtain <math>k = 20</math></p>	<p>B1 B1 [2]</p> <p>B1 B1 B1 B1 [4]</p> <p>B1 B1 M1 A1]</p>
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**Q10.**

6	<p>(i) State modulus is 2 State argument is <math>\frac{1}{6}\pi</math>, or <math>30^\circ</math>, or 0.524 radians</p>	B1 B1	[2]
	<p>(ii) (a) State answer <math>3\sqrt{3} + i</math></p> <p>(b) <i>EITHER</i>: Multiply numerator and denominator by <math>\sqrt{3} - i</math>, or equivalent Simplify denominator to 4 or numerator to <math>2\sqrt{3} + 2i</math> Obtain final answer <math>\frac{1}{2}\sqrt{3} + \frac{1}{2}i</math>, or equivalent</p> <p><i>OR 1</i>: Obtain two equations in <math>x</math> and <math>y</math> and solve for <math>x</math> or for <math>y</math> Obtain <math>x = \frac{1}{2}\sqrt{3}</math> or <math>y = \frac{1}{2}</math> Obtain final answer <math>\frac{1}{2}\sqrt{3} + \frac{1}{2}i</math>, or equivalent</p> <p><i>OR 2</i>: Using the correct processes express <math>iz^*/z</math> in polar form Obtain <math>x = \frac{1}{2}\sqrt{3}</math> or <math>y = \frac{1}{2}</math> Obtain final answer <math>\frac{1}{2}\sqrt{3} + \frac{1}{2}i</math>, or equivalent</p>	B1 M1 A1 A1 M1 A1 A1 M1 A1 A1	[4]
	<p>(iii) Plot <math>A</math> and <math>B</math> in relatively correct positions <i>EITHER</i>: Use fact that angle <math>AOB = \arg(iz^*) - \arg z</math> Obtain the given answer</p> <p><i>OR 1</i>: Obtain <math>\tan \hat{AOB}</math> from gradients of <math>OA</math> and <math>OB</math> and the correct <math>\tan(A - B)</math> formula Obtain the given answer</p> <p><i>OR 2</i>: Obtain <math>\cos \hat{AOB}</math> by using correct cosine formula or scalar product Obtain the given answer</p>	B1 M1 A1 M1 A1 M1 A1	[3]

### Q11.

3	<p>(i) Attempt multiplication and use <math>i^2 = -1</math> Obtain <math>3 + 4i</math> Obtain 5 for <u>modulus</u></p> <p>(ii) Draw complete circle with centre corresponding to their <math>w^2</math> ... ... and radius corresponding to their <math> w^2 </math> Shade the correct region</p>	M1 A1 B1	[3]
		B1√ B1√ cwo B1	[3]

### Q12.



- 10 (a) EITHER: Square  $x + iy$  and equate real and imaginary parts to 1 and  $-2\sqrt{6}$  respectively M1\*  
 Obtain  $x^2 - y^2 = 1$  and  $2xy = -2\sqrt{6}$  A1  
 Eliminate one variable and find an equation in the other M1(dep\*)  
 Obtain  $x^4 - x^2 - 6 = 0$  or  $y^4 + y^2 - 6 = 0$ , or 3-term equivalent A1  
 Obtain answers  $\pm(\sqrt{3} - i\sqrt{2})$  A1 [5]
- OR:  
 Denoting  $1 - 2\sqrt{6}i$  by  $Re^{i\theta}$ , state, or imply, square roots are  $\pm\sqrt{R}cis(\frac{1}{2}\theta)$   
 and find values of  $R$  and either  $\cos \theta$  or  $\sin \theta$  or  $\tan \theta$  M1\*  
 Obtain  $\pm\sqrt{5}(\cos\frac{1}{2}\theta + i\sin\frac{1}{2}\theta)$ , and  $\cos\theta = \frac{1}{5}$  or  $\sin\theta = -\frac{2\sqrt{6}}{5}$  or  
 $\tan\theta = -2\sqrt{6}$  A1  
 Use correct method to find an exact value of  $\cos\frac{1}{2}\theta$  or  $\sin\frac{1}{2}\theta$  M1(dep\*)  
 Obtain  $\cos\frac{1}{2}\theta = \pm\sqrt{\frac{3}{5}}$  and  $\sin\frac{1}{2}\theta = \pm\sqrt{\frac{2}{5}}$ , or equivalent A1  
 Obtain answers  $\pm(\sqrt{3} - i\sqrt{2})$ , or equivalent A1  
 [Condone omission of  $\pm$  except in the final answers.]
- (b) Show point representing  $3i$  on a sketch of an Argand diagram B1  
 Show a circle with centre at the point representing  $3i$  and radius 2 B1√  
 Shade the interior of the circle B1√  
 Carry out a complete method for finding the greatest value of  $\arg z$  M1  
 Obtain answer  $131.8^\circ$  or  $2.30$  (or  $2.3$ ) radians A1 [5]  
 [The f.t. is on solutions where the centre is at the point representing  $-3i$ .]

### Q13.

6	(i) Use correct method for finding modulus of their $w^2$ or $w^3$ or both	M1	[4]
	Obtain $ w^2  = 2$ and $ w^3  = 2\sqrt{2}$ or equivalent	A1	
	Use correct method for finding argument of their $w^2$ or $w^3$ or both	M1	
	Obtain $\arg(w^2) = -\frac{1}{2}\pi$ or $\frac{3}{2}\pi$ and $\arg(w^3) = \frac{1}{4}\pi$	A1ft	
	(ii) Obtain centre $-\frac{1}{2} - \frac{1}{2}i$ (their $w^2$ )	B1ft	
	Calculate the diameter or radius using $ w - w^2 $ $w^2$ or right-angled triangle or cosine rule or equivalent	M1	
Obtain radius $\frac{1}{2}\sqrt{10}$ or equivalent	A1	[4]	
Obtain $ z + \frac{1}{2} + \frac{1}{2}i  = \frac{1}{2}\sqrt{10}$ or equivalent	A1ft		

### Q14.

- 9 (i) EITHER Substitute  $x = 1 + \sqrt{2}i$  and attempt the expansions of the  $x^2$  and  $x^4$  terms M1  
 Use  $i^2 = -1$  correctly at least once B1  
 Complete the verification A1  
 State second root  $1 - \sqrt{2}i$  B1
- OR 1 State second root  $1 - \sqrt{2}i$  B1  
 Carry out a complete method for finding a quadratic factor with zeros  $1 \pm \sqrt{2}i$  M1  
 Obtain  $x^2 - 2x + 3$ , or equivalent A1  
 Show that the division of  $p(x)$  by  $x^2 - 2x + 3$  gives zero remainder and complete the verification A1
- OR 2 Substitute  $x = 1 + \sqrt{2}i$  and use correct method to express  $x^2$  and  $x^4$  in polar form M1  
 Obtain  $x^2$  and  $x^4$  in any correct polar form (allow decimals here) B1  
 Complete an exact verification A1  
 State second root  $1 - \sqrt{2}i$ , or its polar equivalent (allow decimals here) B1 [4]
- (ii) Carry out a complete method for finding a quadratic factor with zeros  $1 \pm \sqrt{2}i$  M1\*  
 Obtain  $x^2 - 2x + 3$ , or equivalent A1  
 Attempt division of  $p(x)$  by  $x^2 - 2x + 3$  reaching a partial quotient  $x^2 + kx$ , or equivalent M1 (dep\*)  
 Obtain quadratic factor  $x^2 - 2x + 2$  A1  
 Find the zeros of the second quadratic factor, using  $i^2 = -1$  M1 (dep\*)  
 Obtain roots  $-1 + i$  and  $-1 - i$  A1 [6]  
 [The second M1 is earned if inspection reaches an unknown factor  $x^2 + Bx + C$  and an equation in  $B$  and/or  $C$ , or an unknown factor  $Ax^2 + Bx + (6/3)$  and an equation in  $A$  and/or  $B$ ]  
 [If part (i) is attempted by the OR 1 method, then an attempt at part (ii) which uses or quotes relevant working or results obtained in part (i) should be marked using the scheme for part (ii)]

## Q15.

- 10 (a) Expand and simplify as far as  $iw^2 = -8i$  or equivalent B1  
 Obtain first answer  $i\sqrt{8}$ , or equivalent B1  
 Obtain second answer  $-i\sqrt{8}$ , or equivalent and no others B1 [3]
- (b) (i) Draw circle with centre in first quadrant M1  
 Draw correct circle with interior shaded or indicated A1 [2]
- (ii) Identify ends of diameter corresponding to line through origin and centre M1  
 Obtain  $p = 3.66$  and  $q = 7.66$  A1  
 Show tangents from origin to circle M1  
 Evaluate  $\sin^{-1}\left(\frac{1}{4}\sqrt{2}\right)$  M1  
 Obtain  $\alpha = \frac{1}{4}\pi - \sin^{-1}\left(\frac{1}{4}\sqrt{2}\right)$  or equivalent and hence 0.424 A1  
 Obtain  $\beta = \frac{1}{4}\pi + \sin^{-1}\left(\frac{1}{4}\sqrt{2}\right)$  or equivalent and hence 1.15 A1 [6]

## Q16.



- 8 (a) EITHER: Solve for  $u$  or for  $v$  M1  
 Obtain  $u = \frac{2i-6}{1-2i}$  or  $v = \frac{5}{1-2i}$ , or equivalent A1  
 EITHER: Multiply a numerator and denominator by conjugate of denominator, or equivalent  
 OR: Set  $u$  or  $v$  equal to  $x + iy$ , obtain two equations by equating real and imaginary parts and solve for  $x$  or for  $y$  M1  
 OR: Using  $a + ib$  and  $c + id$  for  $u$  and  $v$ , equate real and imaginary parts and obtain four equations in  $a, b, c$  and  $d$  M1  
 Obtain  $b + 2d = 2, a + 2c = 0, a + d = 0$  and  $-b + c = 3$ , or equivalent A1  
 Solve for one unknown M1  
 Obtain final answer  $u = -2 - 2i$ , or equivalent A1  
 Obtain final answer  $v = 1 + 2i$ , or equivalent A1 [5]
- (b) Show a circle with centre  $-i$  B1  
 Show a circle with radius 1 B1  
 Show correct half line from 2 at an angle of  $\frac{3}{4}\pi$  to the real axis B1  
 Use a correct method for finding the least value of the modulus M1  
 Obtain final answer  $\frac{3}{\sqrt{2}} - 1$ , or equivalent, e.g. 1.12 (allow 1.1) A1 [5]

**Q17.**

- 9 (a) Solve using formula, including simplification under square root sign M1\*  
 Obtain  $\frac{-2 \pm 4i}{2(2-i)}$  or similarly simplified equivalents A1  
 Multiply by  $\frac{2+i}{2+i}$  or equivalent in at least one case M1(d\*M)  
 Obtain final answer  $-\frac{4}{5} + \frac{3}{5}i$  A1  
 Obtain final answer  $-i$  A1 [5]

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- (b) Show  $w$  in first quadrant with modulus and argument relatively correct B1  
 Show  $w^3$  in second quadrant with modulus and argument relatively correct B1  
 Show  $w^*$  in fourth quadrant with modulus and argument relatively correct B1  
 Use correct method for area of triangle M1  
 Obtain 10 by calculation A1 [5]

**Q18.**

- 5 (i) Either Multiply numerator and denominator by  $\sqrt{3} + i$  and use  $i^2 = -1$  M1  
 Obtain correct numerator  $18 + 18\sqrt{3}i$  or correct denominator 4 B1  
 Obtain  $\frac{9}{2} + \frac{9}{2}\sqrt{3}i$  or  $(18 + 18\sqrt{3}i)/4$  A1  
 Obtain modulus or argument M1  
 Obtain  $9e^{\frac{1}{3}\pi i}$  A1 [5]
- OR Obtain modulus and argument of numerator or denominator, or both moduli or both arguments M1  
 Obtain moduli and argument 18 and  $\frac{1}{6}\pi$  or 2 and  $-\frac{1}{6}\pi$   
 or moduli 18 and 2 or arguments  $\frac{1}{6}\pi$  and  $-\frac{1}{6}\pi$  (allow degrees) B1  
 Obtain  $18e^{\frac{1}{6}\pi i} \div 2e^{-\frac{1}{6}\pi i}$  or equivalent A1  
 Divide moduli and subtract arguments M1  
 Obtain  $9e^{\frac{1}{3}\pi i}$  A1 [5]
- (ii) State  $3e^{\frac{1}{6}\pi i}$ , following through their answer to part (i) B1✓  
 State  $3e^{\frac{1}{6}\pi i + \frac{1}{2}\pi i}$ , following through their answer to part (i) B1✓  
 Obtain  $3e^{-\frac{5}{6}\pi i}$  B1 [3]

**Q19.**

- 7 (a) EITHER: Multiply numerator and denominator by  $1 - 4i$ , or equivalent, and use  $i^2 = -1$  M1  
 Simplify numerator to  $-17 - 17i$ , or denominator to 17 A1  
 Obtain final answer  $-1 - i$  A1
- OR: Using  $i^2 = -1$ , obtain two equations in  $x$  and  $y$ , and solve for  $x$  or for  $y$  M1  
 Obtain  $x = -1$  or  $y = -1$ , or equivalent A1  
 Obtain final answer  $-1 - i$  A1 3
- (b) (i) Show a point representing  $2 + i$  in relatively correct position B1  
 Show a circle with centre  $2 + i$  and radius 1 B1✓  
 Show the perpendicular bisector of the line segment joining  $i$  and 2 B1  
 Shade the correct region B1 4
- (ii) State or imply that the angle between the tangents from the origin to the circle is required M1  
 Obtain answer 0.927 radians (or  $53.1^\circ$ ) A1 2

**Q20.**

- 5 (i) Substitute  $z = 1 + i$  and obtain  $w = \frac{1+2i}{1+i}$  B1
- EITHER:* Multiply numerator and denominator by the conjugate of the denominator, or equivalent M1
- Simplify numerator to  $3 + i$  or denominator to 2 A1
- Obtain final answer  $\frac{3}{2} + \frac{1}{2}i$ , or equivalent A1
- OR:* Obtain two equations in  $x$  and  $y$ , and solve for  $x$  or for  $y$  M1
- Obtain  $x = \frac{3}{2}$  or  $y = \frac{1}{2}$ , or equivalent A1
- Obtain final answer  $\frac{3}{2} + \frac{1}{2}i$ , or equivalent A1 [4]

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- (ii) *EITHER:* Substitute  $w = z$  and obtain a 3-term quadratic equation in  $z$ ,  
 e.g.  $iz^2 + z - i = 0$  B1
- Solve a 3-term quadratic for  $z$  or substitute  $z = x + iy$  and use a correct method to solve for  $x$  and  $y$  M1
- OR:* Substitute  $w = x + iy$  and obtain two correct equations in  $x$  and  $y$  by equating real and imaginary parts B1
- Solve for  $x$  and  $y$  M1
- Obtain a correct solution in any form, e.g.  $z = \frac{-1 \pm \sqrt{3}i}{2i}$  A1
- Obtain final answer  $-\frac{\sqrt{3}}{2} + \frac{1}{2}i$  A1 [4]

## Q21.

- 5 (i) State or imply  $iw = -3 + 5i$  B1
- Carry out multiplication by  $\frac{4-i}{4-i}$  M1
- Obtain final answer  $-\frac{7}{17} + \frac{23}{17}i$  or equivalent A1 [3]
- (ii) Multiply  $w$  by  $z$  to obtain  $17 + 17i$  B1
- State  $\arg w = \tan^{-1} \frac{3}{5}$  or  $\arg z = \tan^{-1} \frac{1}{4}$  B1
- State  $\arg wz = \arg w + \arg z$  M1
- Confirm given result  $\tan^{-1} \frac{3}{5} + \tan^{-1} \frac{1}{4} = \frac{1}{4}\pi$  legitimately A1 [4]

