

MEGA LECTURE

Q1.

<p>7 (i) $\sin \frac{1}{2}\theta = \frac{6}{10}$ Angle $DOE = 1.287$ radians.</p> <p>(ii) $P = 12 + 12 + 2 \times 10 \times \text{angle } BOD$ Angle $BOD = (\pi - 1.287)$ $\rightarrow 61.1$</p> <p>(iii) Sector $DOE = \frac{1}{2} \times 10^2 \times 1.287$ Triangle $DOE = \frac{1}{2} \times 10^2 \times \sin 1.287$ Area = $\pi \times 10^2 - (2 \text{ sectors} - 2 \text{ triangles})$ (or $48 + 48 + 2 \times \frac{1}{2} \times 10^2 \times (\pi - 1.287)$) M1 M1 $\rightarrow 281$ or 282</p>	<p>M1 A1 [2] M1 M1 A1 [3] M1 M1 A1 [3]</p>	<p>Use of trig with/without radians co – answer given. Use of $s = r\theta$ for arc length. Correct angle co Correct formula used with radians. Correct formula used with radians. co</p>
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Q2.

<p>9 (i) $AS = r \tan \theta$ Area $OAB = r^2 \tan \theta$ or $(OAS) = \frac{1}{2} r^2 \tan \theta$ Area of sector = $\frac{1}{2} r^2 \times 2\theta = r^2 \theta$ Shaded area = $r^2 (\tan \theta - \theta)$ OE</p> <p>(ii) $\cos \frac{\pi}{3} = \frac{6}{OA} \Rightarrow OA = 12$ $AP = 6$ $AS = 6 \tan \frac{\pi}{3} (\Rightarrow AB = 12\sqrt{3})$ Arc $(PST) = 12 \frac{\pi}{3}$ Perimeter = $12 + 12\sqrt{3} + 4\pi$</p>	<p>M1 A1 B1 A1 [4] M1 A1 B1 B1 A1 [5]</p>	<p>Or $(AP) = 2r \tan \theta$ or $(AO) = \frac{r}{\cos \theta}$ Or $OAB = \frac{1}{2} r^2 \sin 2\theta$ Or area sector $(OPS) = \frac{1}{2} r^2 \theta$ Allow e.g. $r^2 \tan \theta - \frac{1}{2} r^2 2\theta$ Or arc $(PS) = 6 \frac{\pi}{3}$ or arc $(ST) = 6 \frac{\pi}{3}$ Allow unsimplified 4π</p>
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Q3.

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<p>7 (i) $AX = 6 \tan \frac{\pi}{3} = 6\sqrt{3}$</p> <p>(ii) Area of triangle = $\frac{1}{2} \times 6 \times 6\sqrt{3}$ Area of sector = $\frac{1}{2} 6^2 \times \frac{\pi}{3}$ Area shaded = $18\sqrt{3} - 6\pi$</p> <p>(iii) Arc $AB = 6 \times \frac{\pi}{3} = 2\pi$ $OX = 6 \div \cos \frac{\pi}{3} = 12$, $BX = 6$ Perimeter = $6\sqrt{3} + 2\pi + 6$</p>	<p>B1 ag [1]</p> <p>M1 Use of $\frac{1}{2}bh$ M1 Use of $\frac{1}{2}r^2\theta$ A1 co [3]</p> <p>M1 Use of $r\theta$ B1 Use of trig to find (OX and then) BX. M1 A1 [4]</p>
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Q4.

<p>3 AO (or r) = $\sqrt{3}$ Area $\Delta = \sqrt{3}$ (or area $\Delta AQC = \frac{\sqrt{3}}{2}$) Area sector $APR = \frac{1}{2} (\sqrt{3})^2 \times \frac{\pi}{3} = \frac{\pi}{2}$ Shaded region = $\sqrt{3} - \frac{\pi}{2}$ oe cao</p>	<p>B1 soi Allow 1.73 B1[✓] soi ft <i>their</i> $\sqrt{3}$ Allow 1.73 ft <i>their</i> $\sqrt{3}$. Allow 1.57. SCA1 for $\pi/4$ M1A1[✓] from $\frac{1}{2} (\sqrt{3})^2 \times \frac{\pi}{6}$ provided $\Delta = \frac{\sqrt{3}}{2}$ A1 [5]</p>
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Q5.

<p>8 (i) $OBX = 90^\circ$, $\cos \theta = \frac{r}{2r}$ $\rightarrow \theta = \frac{1}{3}\pi$.</p> <p>(ii) Arc length $AB = \frac{1}{3} r\pi$ $BX = r \tan(\frac{1}{3}\pi) = r\sqrt{3}$ $P = r + (\frac{1}{3} r\pi + r\sqrt{3})$</p> <p>(iii) Area = $\frac{1}{2} r^2 \sqrt{3} - \frac{1}{6} r^2 \pi$</p>	<p>M1 Needs $90^\circ + \cos$ (or Pyth + sin or tan) A1 co ag [2]</p> <p>B1 $r +$ sum of other two B1 B1 [3]</p> <p>B1[✓] B1 \checkmark on $\tan(\frac{1}{3}\pi)$, co [2]</p>
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Q6.

MEGA LECTURE

<p>3 (i) $(OAB) - \frac{1}{2} \times 8^2 \alpha$, $(OAC) - \frac{1}{2} \times \pi \times 4^2$</p> <p style="margin-left: 40px;">$\alpha - \frac{\pi}{8}$</p> <p>(ii) $8 + 8 \times \text{their } \alpha + \frac{1}{2} \times 8 \times \pi$</p> <p style="margin-left: 40px;">$8 + 5\pi$</p>	<p>B1B1</p> <p>B1</p> <p style="text-align: right;">[3]</p>	<p>Accept 25.1 (for <i>OAC</i>)</p>
	<p>B1 ✓</p> <p>B1</p> <p style="text-align: right;">[2]</p>	<p>23.7 gets B1B0</p> <p>SC B1 for e.g. 5π (omitted <i>OB</i>)</p>

Q7.

<p>2 (i) $\frac{1}{2} \cdot 3^2 \pi = \frac{1}{2} 9^2 \theta - \frac{1}{2} 3^2 \theta$</p> <p style="margin-left: 40px;">$\rightarrow \theta = \frac{1}{4} \pi$</p> <p>(ii) $P = 6 + 6 + 3 \times \frac{1}{4} \pi + 9 \times \frac{1}{4} \pi = 21.4 \text{ cm.}$</p> <p style="margin-left: 40px;">or $12 + 3\pi$</p>	<p>M1 A1</p> <p>A1</p> <p style="text-align: right;">[3]</p>	<p>M1 needs $\frac{1}{2} r^2 \theta$ once. A1 all correct.</p> <p>Answer given</p> <p>M1 is for use of $s = r\theta$ once.</p>
	<p>M1</p> <p>A1</p> <p style="text-align: right;">[2]</p>	

Q8.

<p>5 $r = 6 \text{ cm}$</p> <p>(i) $AB = \sqrt{(6^2 + 6^2)} = \sqrt{72}$</p> <p style="margin-left: 40px;">Angle $BAD = \frac{1}{4} \pi$ or 45°</p> <p style="margin-left: 40px;">Arc length = $\sqrt{72} \times \frac{1}{4} \pi = 6.66(7)$</p> <p>(ii) Sector area = $\frac{1}{2} r^2 \theta = \frac{1}{2} \times 72 \times \frac{1}{4} \pi$</p> <p style="margin-left: 40px;">Area of triangle = $\frac{1}{2} \times 6 \times 6$</p> <p style="margin-left: 40px;">Shaded area = 10.3 or $9\pi - 18$</p>	<p>B1</p> <p>B1</p> <p>M1 A1</p> <p style="text-align: right;">[4]</p>	<p>Use of Pythagoras – or trig (8.5 ok)</p> <p>In degrees or radians</p> <p>Use of $s = r\theta$ with θ in rads only – or correct with degrees. Use of $r = 6 \text{ M0}$.</p> <p>Use of $\frac{1}{2} r^2 \theta$ with θ in rad, and $r \neq 6$.</p> <p>co</p> <p>co</p>
	<p>M1</p> <p>B1</p> <p>A1</p> <p style="text-align: right;">[3]</p>	

Q9.

<p>9 (i) $RS^2 = 10^2 - 6^2$</p> <p style="margin-left: 40px;">$\rightarrow RS = 8 \text{ cm.}$</p> <p>(ii) $\sin \theta = 8/10$ oe</p> <p style="margin-left: 40px;">$\rightarrow \text{angle } RPO = 0.9273 \text{ radians}$</p> <p>(iii) Region = trapezium – 2 sectors</p> <p style="margin-left: 40px;">Area of trapezium = 40 cm^2</p> <p style="margin-left: 40px;">Large sector = $\frac{1}{2} \times 8^2 \times 0.9273$</p> <p style="margin-left: 40px;">Small sector angle = $(\pi - 0.9273)$</p> <p style="margin-left: 40px;">Small sector = $\frac{1}{2} \times 2^2 \times 2.214$</p> <p style="margin-left: 40px;">$\rightarrow 5.90 \text{ cm}^2$</p>	<p>M1</p> <p>A1</p> <p style="text-align: right;">[2]</p>	<p>Use of Pythagoras (or other)</p> <p>Answer given.</p> <p>Use of trig – even if with degrees.</p> <p>co in radians. (Accept 0.927)</p> <p>co</p> <p>Use of $\frac{1}{2} r^2 \theta$.</p> <p>Use of $\frac{1}{2} r^2 \theta$ with angle = $\pi -$ (ii)</p> <p>co</p>
	<p>M1</p> <p>A1</p> <p style="text-align: right;">[2]</p>	
	<p>B1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p style="text-align: right;">[4]</p>	

Q10.

8	(i) $1/2 \times 5^2 \times 1.2$ $1/2 \times 5^2 \times \sin 1.2$ $2[1/2 \times 5^2 \times 1.2 - 1/2 \times 5^2 \times \sin 1.2]$ 6.70	B1 B1 M1 A1	[4]	Subtraction and multiplication by 2 Accept 6.7 or anything rounding to 6.70
	(ii) $5 \cos 0.6$ $5 - "5 \cos 0.6"$ $10(1 - \cos 0.6)$ 1.75	M1 M1 M1 A1	[4]	Subtraction from 5 Multiplication by 2

Q11.

5	(i) Arc $AB = r\theta$ $OC = r \sin \theta$ or $BC = r \cos \theta$ $r(1 + \theta + \cos \theta + \sin \theta)$ correctly derived	M1 M1 A1	[3]	oe eg $BC = r \sin \frac{\theta}{\tan \theta}$ etc OC & BC reversed loses M1A1
	(ii) Sector $OAB = \frac{1}{2} \times 10^2 \times \frac{\pi}{5}$ (-31.42) $\Delta OCB = \frac{1}{2 \left(10 \cos \frac{\pi}{5} \right) \left(10 \sin \frac{\pi}{5} \right)}$ (-23.78) Total area = 55.2	M1 M1 A1	[3]	oe Δ in terms of π and 10 Allow OC & BC reversed (ie max 4/6)

Q12.

4	(i) $10^2 \sin 0.8 = 71.7$	M1A1	[2]	Completely correct method for a triangle
	(ii) sector(s) = $(2) \times \frac{1}{2} \times 10^2 \times 0.8 = (2) \times 40$ Total area = 80	M1 A1	[2]	Correct formula used for a sector
	(iii) arc(s) = $(2) \times 10 \times 0.8$ $16 + 20 = 36$	M1 A1	[2]	Correct formula used for an arc

Q13.

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<p>6 (i) $AC = r - r \cos \theta$</p> <p>(ii) arc $AB = \frac{4\pi}{3}$ arc $AD = \frac{\pi}{2} \times \text{their } AC = \frac{\pi}{2} \times (4 - 4 \cos \frac{\pi}{3}) = \pi$</p> <p>$BD = 4 \sin \frac{\pi}{3} - \text{their } AC = 2\sqrt{3} - 2$</p> <p>Perimeter = $\frac{7\pi}{3} + 2\sqrt{3} - 2$</p>	<p>B1 [1]</p> <p>B1 M1A1</p> <p>M1A1</p> <p>A1 [6]</p>	<p>Allow $\pi \times \text{their } AC$ for M1. Allow 3.14</p> <p>Allow 1.46</p> <p>cao Accept $\sqrt{12}$</p>
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Q14.

<p>4 area $\Delta = 2\sqrt{3}$ $\tan A = \frac{2\sqrt{3}}{2} \Rightarrow A = \frac{\pi}{3}$ Area sector = $\frac{1}{2} \times 2^2 \times \frac{\pi}{3} = \frac{2\pi}{3}$ Shaded area</p>	<p>B1 B1 M1 A1</p> <p style="text-align: right;">[4]</p>	<p>Accept 60°</p> <p>Use of $\frac{1}{2}r^2\theta$ with θ in radians</p> <p>cao</p>
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Q15.

<p>6 (i) $r(2\pi - \alpha) + 2r\alpha + 2r$ $2\pi r + r\alpha + 2r$</p> <p>(ii) $\frac{1}{2}(2r)^2\alpha + \pi r^2 - \frac{1}{2}r^2\alpha$ $\frac{3r^2\alpha}{2} + \pi r^2$</p> <p>(iii) $\pi r^2 - \frac{1}{2}r^2\alpha - 2r^2\alpha$ $\alpha - \frac{2}{5}\pi$</p>	<p>B1B1 B1</p> <p style="text-align: right;">[3]</p> <p>B1B1</p> <p>B1 [3]</p> <p>M1</p> <p>A1 [2]</p>	<p>fit for $r\alpha$ instead of $2r\alpha$ or omission $2r$ SC1 for $2r\alpha + 4r$. (Plate = shaded part)</p> <p>Either B1 can be scored in (iii)</p> <p>For equating <i>their</i> 2 parts from (ii)</p>
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Q16.

<p>6 (i) sector areas are $\frac{1}{2}11^2\alpha, \frac{1}{2}5^2\alpha$</p> <p>$k - \frac{\frac{1}{2} \times 11^2\alpha - \frac{1}{2} \times 5^2\alpha}{\frac{1}{2} \times 5^2\alpha}$</p> <p>$k - \frac{96}{25}$ or 3.84</p>	<p>B1</p> <p>M1</p> <p>A1 [3]</p>	<p>Sight of $11^2, 5^2$</p> <p>Or $\frac{11^2 - 5^2}{5^2}$</p>
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**MEGA LECTURE**

<p>(ii) perimeter shaded region= $11\alpha + 5\alpha + 6 + 6 = 16\alpha + 12$ perimeter unshaded region = $5\alpha + 5 + 5 = 5\alpha + 10$ $16\alpha + 12 = 2(5\alpha + 10)$ $\alpha = 4/3$ or 1.33</p>	<p>B1 B1 M1 A1 [4]</p>	
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