

1. A fair coin is tossed 30 times, the result of which is tabulated below. Study the table and answer the questions given below the table:

Event	Tally Marks	Frequency
Head		14
Tail		16

- How many times does 'head' appear?
- How many times does 'tail' appear?
- Estimate the probability of the appearance of head?
- Estimate the probability of the appearance of tail?

Solution. From the table, total outcomes $= 30 \Rightarrow n(S) = 30$

From the table, we see that

- Let A = event the times head appears $\Rightarrow n(A) = 14$
- Let B = event the times tail appears $\Rightarrow n(B) = 16$
- Probability that head appears $= P(A) = \frac{n(A)}{n(S)} = \frac{14}{30} = \frac{7}{15}$
- Probability that tail appears $= P(B) = \frac{n(B)}{n(S)} = \frac{16}{30} = \frac{8}{15}$

2. A die is tossed 100 times. The result is tabulated below. Study the table and answer the questions given below the table:

Event	Tally Marks	Frequency
1		14
2		17
3		20
4		18
5		15
6		16

- How many times do 3 dots appear?
- How many times do 5 dots appear?
- How many times does an even number of dots appear?
- How many times does a prime number of dots appear?
- Find the probability of each one of the above cases.

Solution. From the table, total outcomes = 100 $\Rightarrow n(S) = 100$

From the table, we see that

(i) Let A = event, the number of times, 3 dots appear $\Rightarrow n(A) = 20$

(ii) Let B = event, the number of times 5, dots appear $\Rightarrow n(B) = 15$

(iii) Let C = event, the number of times, even dots appear

$$\Rightarrow n(C) = 17 + 18 + 16 = 51$$

(iv) Let D = event, the number of times, prime dots appear

$$\Rightarrow n(D) = 17 + 15 + 20 = 52$$

(v) Required probabilities are as :

$$P(A) = \frac{n(A)}{n(S)} = \frac{20}{100} = \frac{1}{5} \quad P(B) = \frac{n(B)}{n(S)} = \frac{15}{100} = \frac{3}{20}$$

$$P(C) = \frac{n(C)}{n(S)} = \frac{51}{100} \quad P(D) = \frac{n(D)}{n(S)} = \frac{52}{100} = \frac{13}{25}$$

3. The eggs supplied by a poultry farm during a week broke during transit as follows: 1%, 2%, $1\frac{1}{2}\%$, $\frac{1}{2}\%$, 1%, 2%, 1%

Find the probability of the eggs broke in a day. Calculate the number of eggs that will be broken in transiting the following number of eggs:

(i) 7,000 (ii) 8,400 (iii) 10,500

Solution.	Transit	Broken eggs	No. of eggs
	1	1	100
	2	2	100
	3	$1\frac{1}{2} = 1.5$	100
	4	$\frac{1}{2} = 0.5$	100
	5	1	100
	6	2	100
	7	1	100

$$\text{Total eggs} = n(S) = 700$$

Let A = event the eggs broke $\Rightarrow n(A) = 1 + 2 + 1.5 + 0.5 + 1 + 2 + 1 = 9$

$$P(A) = \frac{n(A)}{n(S)} = \frac{9}{700}$$

(i) Number of eggs broke in 7000 = $7000 \times \frac{9}{700} = 90$

$$(ii) \text{ Number of eggs broke in 8400} = 8400 \times \frac{9}{700} = 108$$

$$(i)ii \text{ Number of eggs broke in 10500} = 10500 \times \frac{9}{700} = 135$$

§ 7.7 ADDITION OF PROBABILITIES.

Notations.

We know that $P(E)$ means the probability of an event E .

Now if A and B are any two events, then

$P(A)$ = probability of occurrence of the event A

$P(B)$ = probability of occurrence of the event B

$P(A \cup B)$ = probability of occurrence of the event A or B

$P(A \cap B)$ = probability of occurrence of the event A and B

Theorems of Addition of Probabilities.

I. $P(A \cup B) = P(A \text{ or } B) = P(A) + P(B)$, when A and B are disjoint

II. $P(A \cup B) = P(A) + P(B) - P(A \cap B)$, when A and B are overlapping

