

Mechanics

The study of *Physics* begins with mechanics.

Mechanics is the branch of physics that focuses on the motion of objects and the forces that cause the motion to change.

There are two parts to mechanics: *Kinematics* and *Dynamics*.

Kinematics deals with the concepts that are needed to describe motion, without any reference to forces.

Dynamics deals with the effect that forces have on motion.

Introduction

Kinematics is the science of describing the motion of objects using words, diagrams, graphs, and equations.

The goal of kinematics is to develop mental models to describe the motion of real-world objects.

We will learn to describe motion using:

- 1. Words
- 2. Diagrams
- 3. Graphs
- 4. Equations

Describing Motion with words

The motion of objects can be **<u>described by words</u>**.

Even a person without a background in physics has a collection of words, which can be used to describe moving objects. For example, going faster, stopped, slowing down, speeding up, and turning provide a sufficient vocabulary for describing the motion of objects.

In physics, we use these words as the language of kinematics. **1. Distance and Displacement 2. Speed and Velocity**

3. Acceleration

These words which are used to describe the motion of objects can be divided into two categories.

The quantity is either a **vector** or **scalar**.

1. Scalars are quantities which are described by a magnitude only.

2. Vectors are quantities which are described by both a magnitude and a direction.

Distance	Displacement
Distance refers to the total length of travel irrespective of the direction of the motion.	Displacement refers to the distance moved in a particular direction. It is the object's overall
	change in position.
It is a scalar quantity.	It is a vector quantity.
SI unit: metre (m)	SI unit: metre (m)
Other common units:	Other common units:
kilometre (km), centimetre	kilometre (km), centimetre
(cm)	(cm)

mob: +92 323 509 4443, email: megalecture@gmail.com Distance vs. Displacement

- You drive the path, and your odometer goes up (your distance).
- Your displacement is the shorter directed distance from start to stop (green arrow) Jale C. Kni

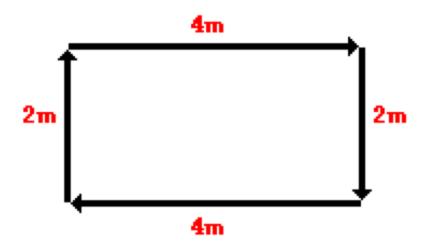
start



stop

Example 1

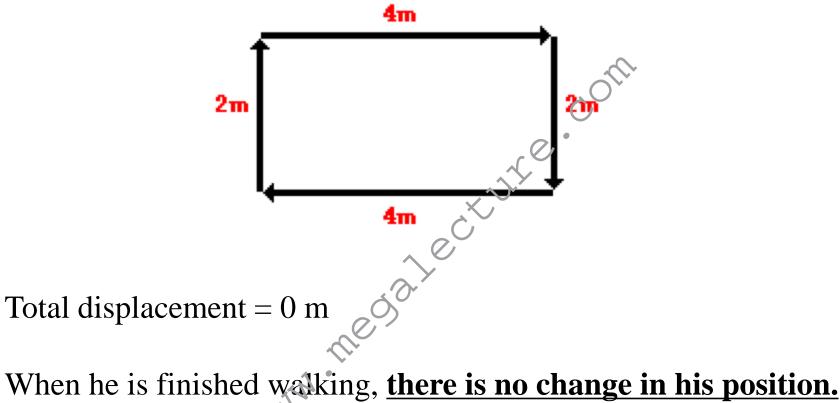
A student walks 4 m East, 2 m South, 4 m West, and finally 2 m North.



Total distance = 12 m

During the course of his motion, the total length of travel is 12 m.

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The 4 m east is "canceled by" the 4 m west; and the 2 m south is "canceled by" the 2 m north.

Speed	Velocity
Speed is the rate of change of distance . It is a scalar quantity .	Velocity is the distance travelled in a specific direction.
	It is also defined as the rate of change of displacement.
	It is a vector quantity.
Speed = $\frac{\text{distance travelled}}{\text{time taken}}$	Velocity= change in displacement time taken

When evaluating the velocity of an object, one must keep track of direction.

The direction of the velocity vector is the same as the direction which an object is moving. (It would not matter whether the object is speeding up or slowing down.)

For example:

If an object is moving rightwards, then its velocity is described as being rightwards.

Boeing 747 moving towards the west with a speed of 260m/s has a velocity of 260m/s, west. Note that speed has no direction (it is a scalar) and velocity at any instant is simply the speed with a direction.

Instantaneous Speed and Average Speed

As an object moves, it often undergoes changes in speed.

The speed at any instant is known as the **instantaneous speed**. (From the value of the speedometer)

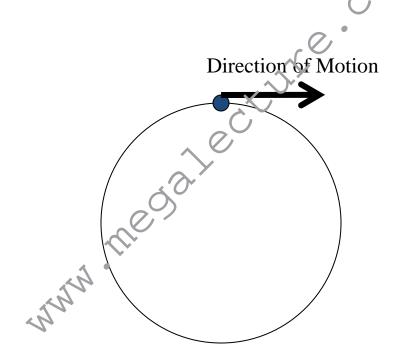


The average speed of the entire journey can be calculated:

Average Speed = $\frac{\text{Total distance travelled}}{\text{Total time taken}}$

mpb: +92 323 509 4443, email: megalecture@gmail.com <u>Speed Vs Velocity</u>

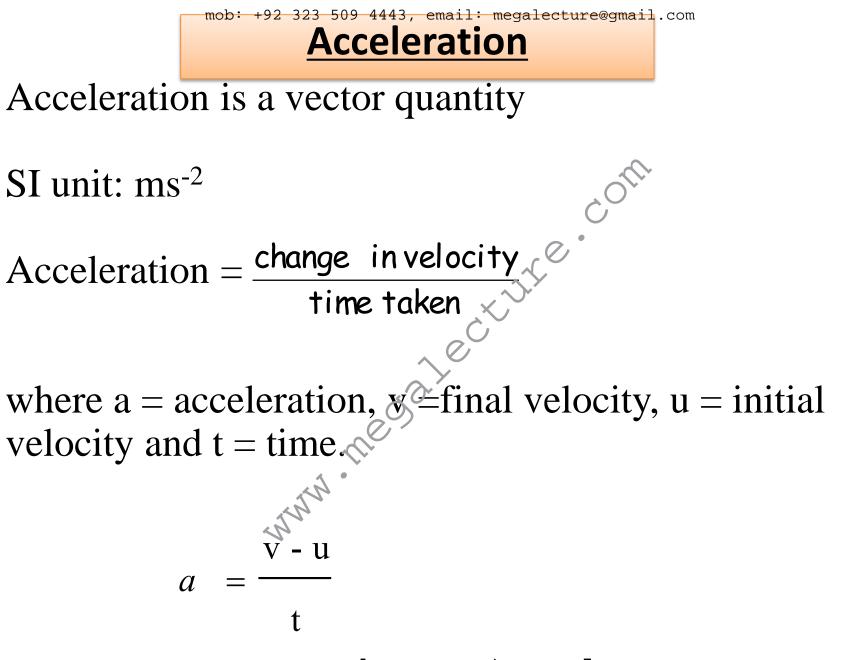
An object is moving in a circle at a **constant speed** of 10 m s⁻¹. We say that it has a constant speed but **its velocity is not constant**. Why?



The direction of the object keeps changing.

- An object whose velocity is changing is said to accelerate.
- If the direction and / or speed of a moving object changes, the object is accelerating
- Acceleration is the rate of change of velocity

Time (s)	Velocity (m/s)
0	0
1	10
2	20
3	30
4	40
5	50



Describing Motion with Graphs

1.Plot and interpret a distance-time graph and a speed-time graph.

- 2. Deduce from the shape of a distance-time graph when a body is:
 - (a) at rest
 - (b) moving with uniform speed
 - (c) moving with non-uniform speed
- 3. Deduce from the shape of a Velocity-time graph when a body is:
 - (a) at rest
 - (b) moving with uniform speed
 - (c) moving with uniform acceleration
 - (d) moving with non-uniform acceleration

4. Calculate the area under a speed-time graph to determine the distance travelled for motion with uniform speed or uniform acceleration.

Key Concepts

Distance-time Graph

Gradient of the <u>Distance-time Graph</u> is the speed of the moving object

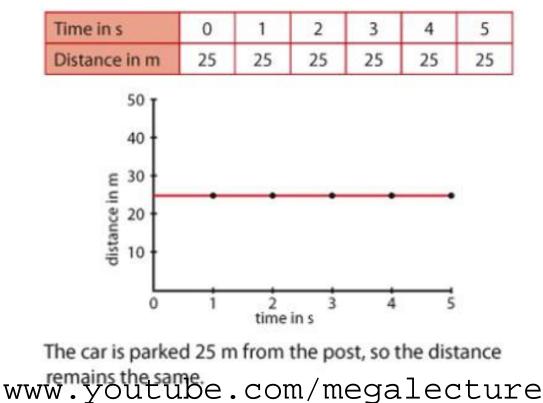
Speed-time Graph

Gradient of the <u>Speed-time Graph</u> is the acceleration of the moving object.

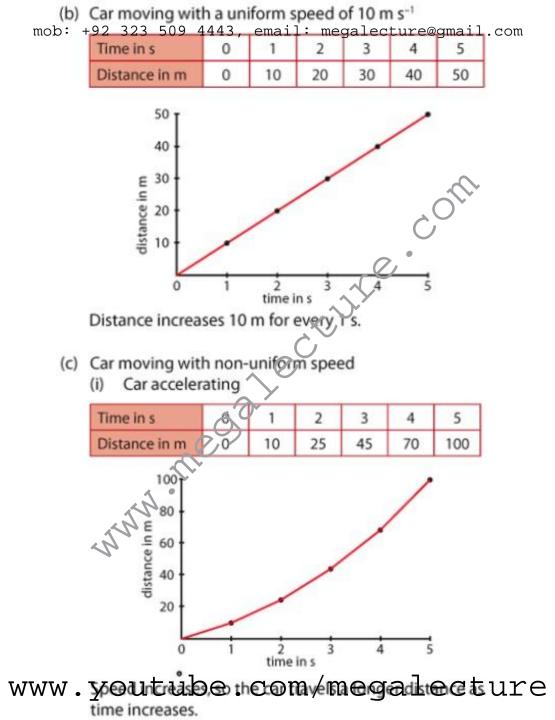
Area under the Speed-time Graph is the distance travelled.

mob: +92 Distance-time Graph 1.com

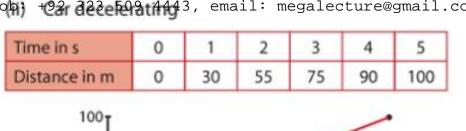
A car has travelled past a lamp post on the road and the distance of the car from the lamp post is measured every second. The distance and the time readings are recorded and a graph is plotted using the data. The following pages are the results for four possible journeys. The steeper the line, the greater the speed.



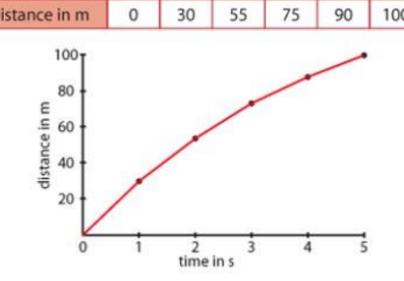
(a) Car at rest



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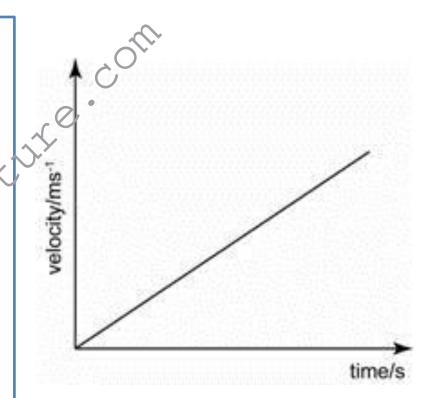
Speed decreases, so the car travels a shorter distance as time increases.

The gradient of the distance-time graph gives the speed of the moving object.

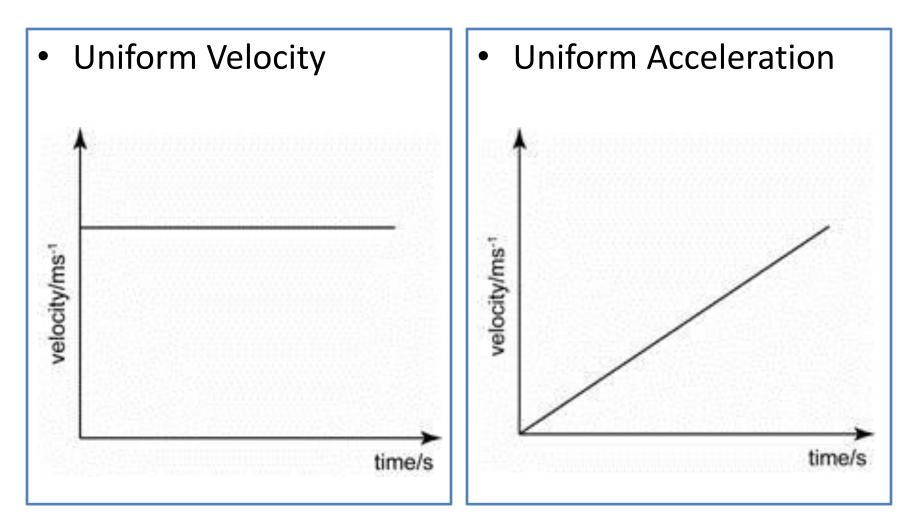
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Velocity - Time Graph

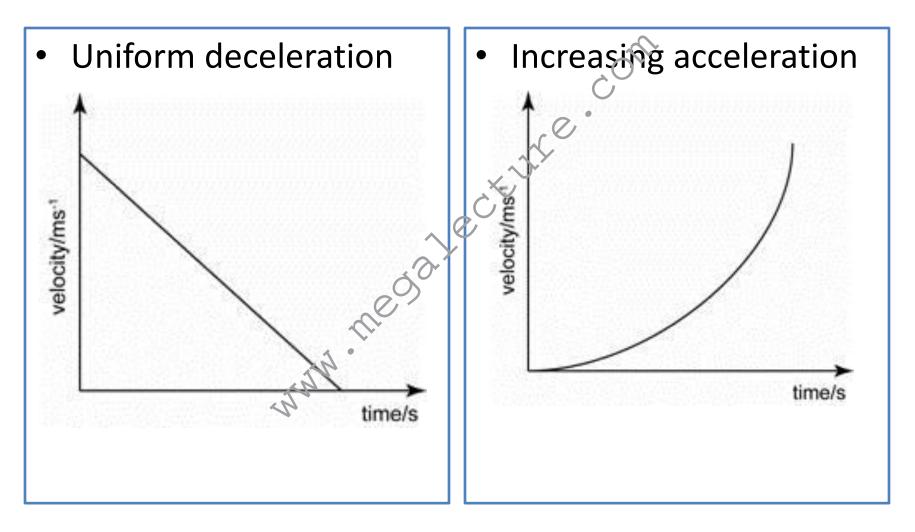
- The gradient of the velocity-time gradient gives a value of the changing rate in velocity, which is the acceleration of the object.
- The area below the velocity-time graph gives a value of the object's displacement.



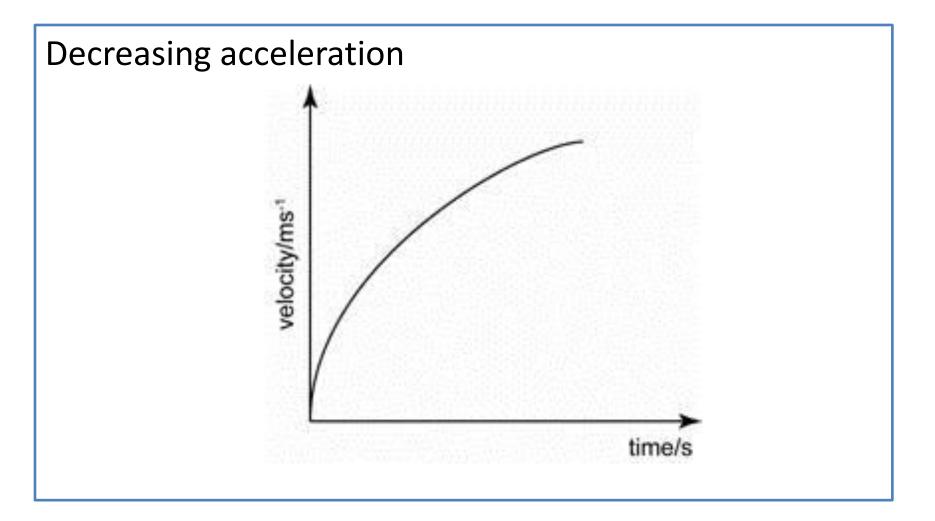
Analysing Velocity - Time Graph



Analysing Velocity - Time Graph



Analysing Velocity - Time Graph

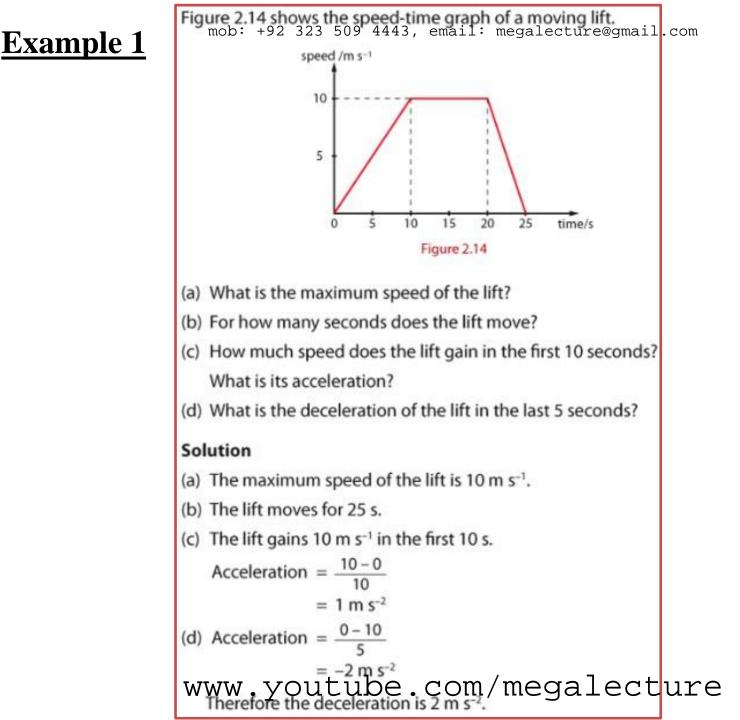


How do you find the gradient of velocity-time graph?

- You need to select two points on the graph, for example (x₁,y₁) and (x₂,y₂).
- Once you have selected the points you put then into the equation m=(y₂-y₁)/(x₂-x₁)

\blacktriangleright m = the gradient

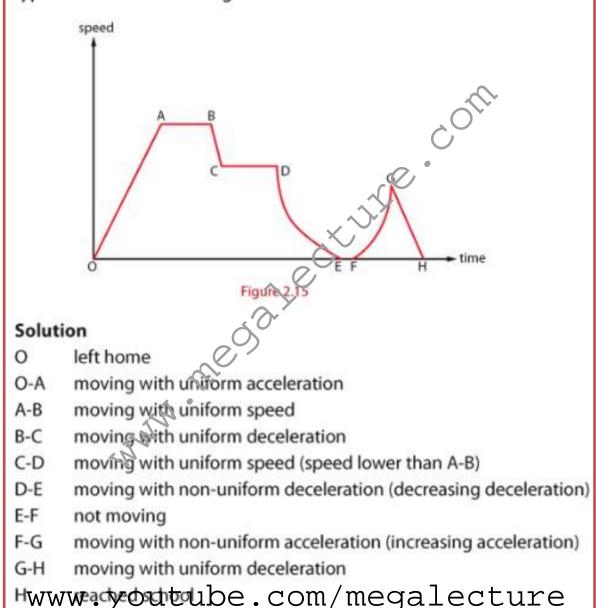
- The gradient represents the acceleration.
- In other words, we take the vertical reading from the graph where the acceleration finishes and divide it by the horizontal reading where the acceleration finishes.



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Figure 2.15+ 910-323 the speed time graph nona Journey of a bound of the graph and describe the type of motion in each stage.



Area under a speed-time graph megalecture@gmail.com

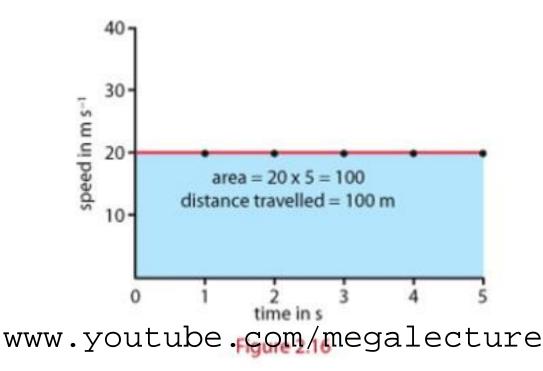
The figure below shows the speed-time graph of a car travelling with a uniform speed of 20 ms⁻¹. The distance travelled by the car is given by:

```
Distance = speed x time = 20 \times 5
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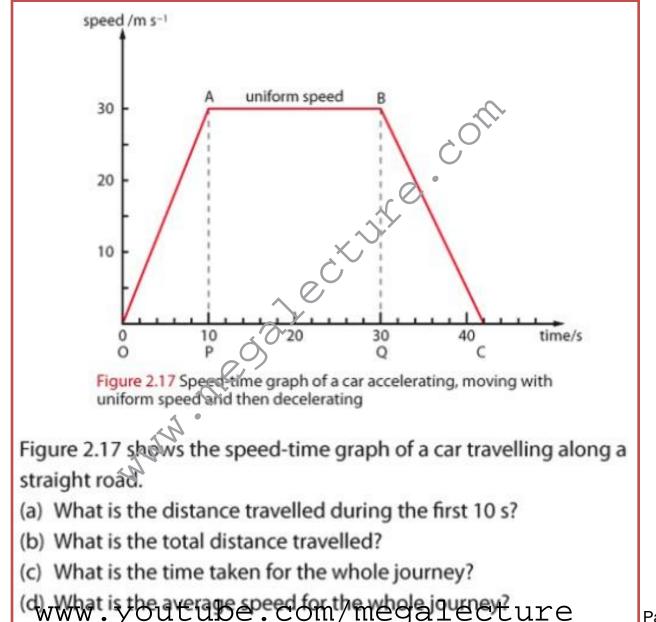
= 100 m

The same information of distance travelled can also be obtained by calculating the area under the speed-time graph.

The area under a speed-time graph gives the distance travelled.



Example 3 - Question



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Example 3 - Solution 509 4443, email: megalecture@gmail.com

Solution (a) During the first 10 s, distance travelled = area of triangle OAP $=\frac{1}{2} \times 10 \times 30$ $= 150 \, \text{m}$ (b) Total distance travelled = area of trapezium OABC $=\frac{1}{2} \times (20 + 42) \times 30$ = 930 m (c) Time taken for the whole journey = 42 s Total distance travelled (d) Average speed for the whole journey Total time taken $=\frac{930}{42}$ $= 22.1 \text{ m s}^{-1}$

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com

<u>http://www.youtpbe.com/watch?v=go9uekKOcK</u>

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<u>http://www.youtube.com/watch?v=FHtvDA0W34</u>

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Uniformly accelerated motion

• Free fall is motion with no acceleration other than that provided by gravity.





- A free-falling object is an object which is falling under the sole influence of gravity.
- Any object which is being acted upon only be the force of gravity is said to be in a state of free fall.

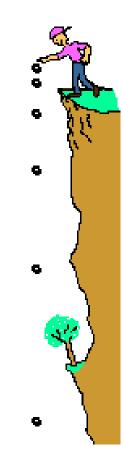
Any object which is moving and being acted upon only be the force of gravity is said to be "in a state of free fall."

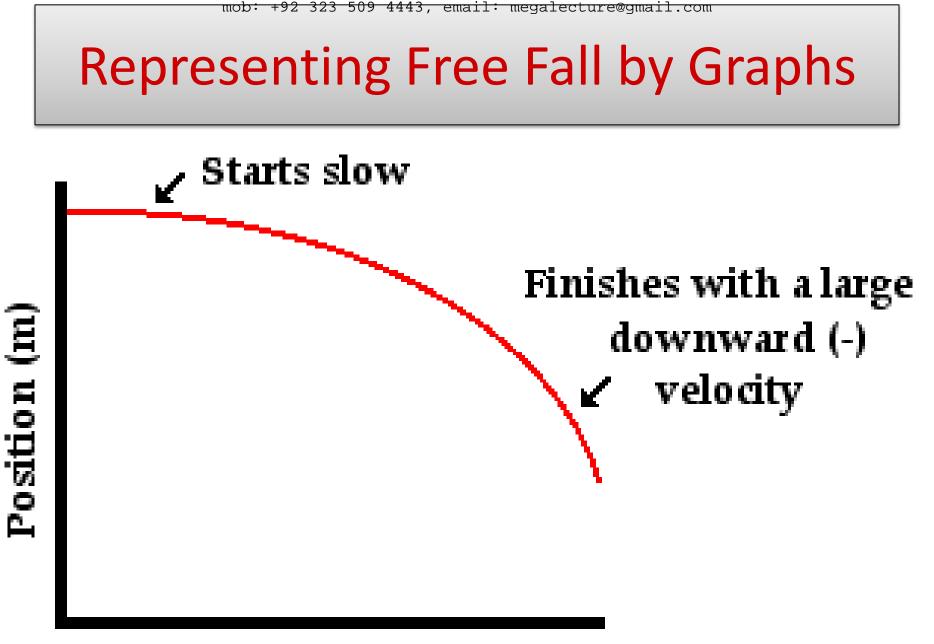
- all objects fall freely at $g \approx 10$ m s⁻² when near the earth and air resistance is negligible.
- speed of a free-falling body increases by 9.8 m s⁻¹ every second or when a body is thrown up, its speed decreases by 9.8 m s⁻¹ every second.

Although the acceleration due to gravity is considered constant, it tends to vary slightly over the earth since the earth is not a perfect sphere.

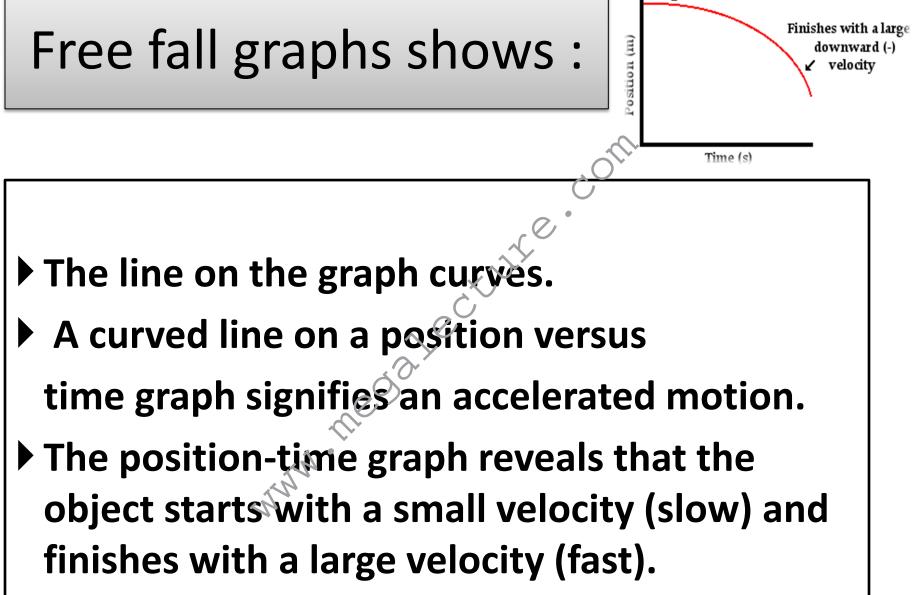
Examples

- Examples of objects in Free fall
- A spacecraft (in space) with its rockets off (e.g. in a continuous orbit, or going up for some minutes, and then down)
- > The Moon orbiting around the Earth.
- Examples of objects not in Free fall
- Standing on the ground: the gravitational acceleration is counteracted by the normal force from the ground.
- Flying horizontally in an airplane: the wings' lift is also providing an acceleration.





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Check your Understanding !!

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Questions to answer !

 "Doesn't a more massive object accelerate at a greater rate than a less massive object?" "Wouldn't an elephant free-fall faster than a mouse?"

 The answer to the question (doesn't a more massive object accelerate at a greater rate than a less massive object?) is absolutely NOT!

That is, absolutely not if we are considering the specific type of falling motion known as free-fall.
 Free-fall is the motion of objects which move under the sole influence of gravity; free-falling objects do not encounter air resistance.

□ More massive objects will only fall faster if there is an appreciable amount of air resistance present.

Force of gravity means the dog accelerates

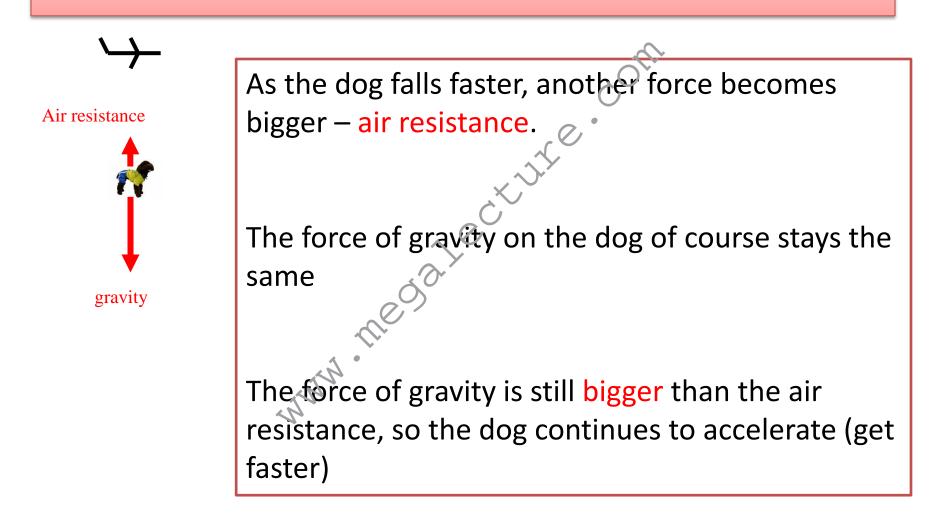
gravity

To start, the dog is falling slowly (it has not had time to speed up).

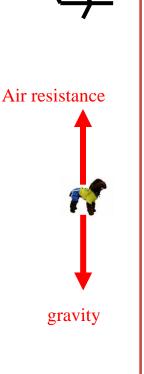
There is really only one force acting on the dog, the force of gravity.

The dog falls faster (accelerates) due to this force.

Gravity is still bigger than air resistance



Gravity = air resistance Terminal Velocity

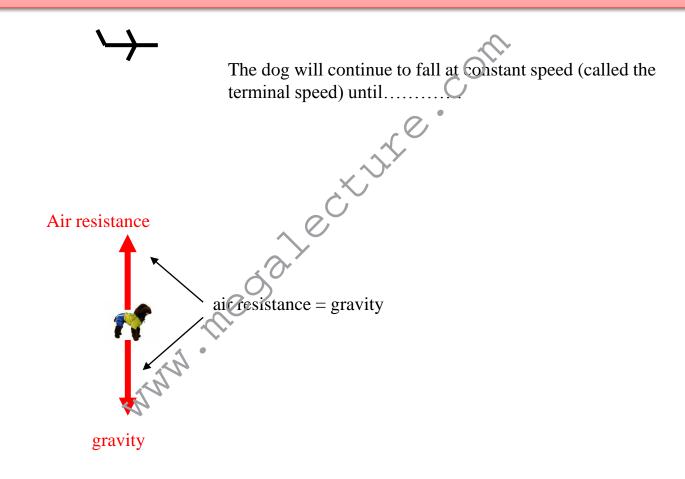


As the dog falls faster and air resistance increases, eventually the air resistance becomes as big as (equal to) the force of gravity.

The dog stops getting faster (accelerating) and falls at constant speed.

This velocity is called the terminal Velocity

Terminal Speed



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- Acceleration is defined as the rate of change of velocity with respect to time, in a given direction. The SI units of acceleration are ms⁻².
- This would mean that if an object has an acceleration of 1 ms⁻² it will increase its velocity (in a given direction) 1 ms⁻¹ every second that it accelerates.

It means that acceleration is constant.

This meaning that velocity is varying with respect to time, we see this by this formula (v - u) / t (Time).

It means....

- If an object is held stationary in a uniform gravitational field and when it is released, it will fall. It will do so with uniform acceleration.
- Near the surface of the earth the acceleration is approximately 9.8 ms⁻².
- This means that every second that the object falls its velocity will increase by 9.8 ms⁻¹.

Check your understanding !

•What happens if an object is thrown up?

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What happens if an object is thrown up?

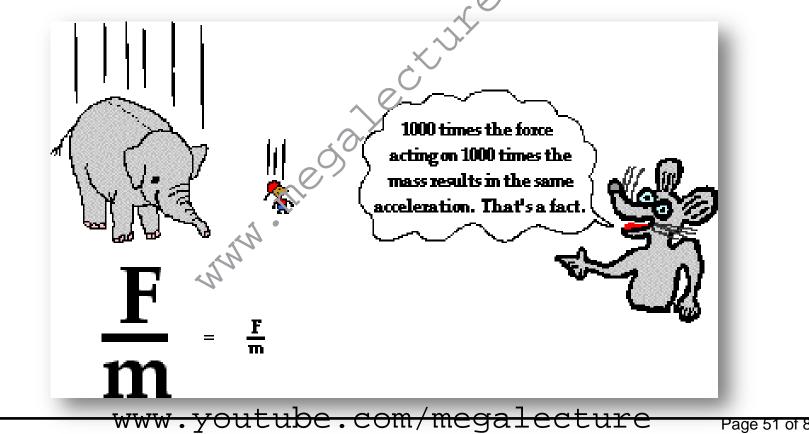
- The acceleration is still downward. If an object is thrown up with an initial velocity of 30 ms⁻¹, after one second it will only be going 20 ms⁻¹ up, after 2 seconds it will only be going 10 ms⁻¹, after 3 seconds the object will have zero velocity!
- Even if the objects velocity is zero the acceleration is not zero.

An experiment with 'g'.

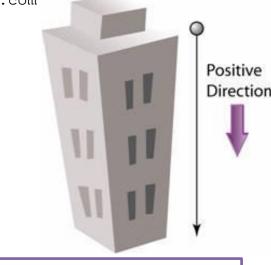
- College building
- Stop watch
- A group of students on top floor
- A group of students on ground floor
- Need to check the distance between top floor and ground, time to calculate velocity.
- (This experiment will be carried out during next lesson)
- Upon investigation, g constant is found with one of the equations we have derived and it is as follows :

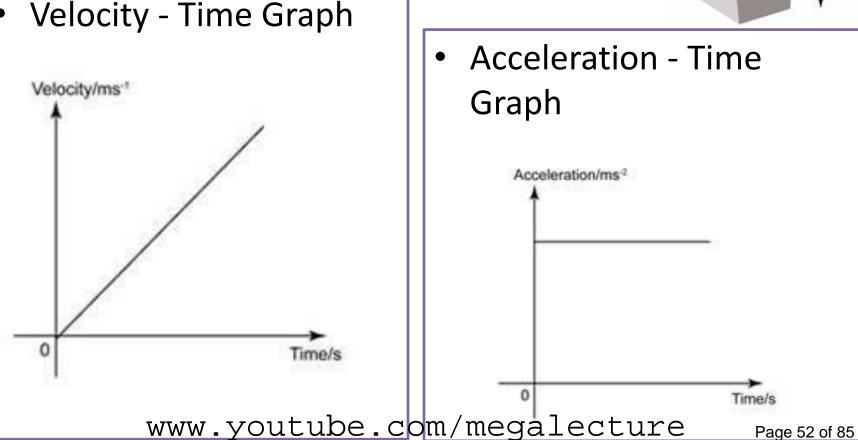
Remember (will study in Ch.4 Dynamics)

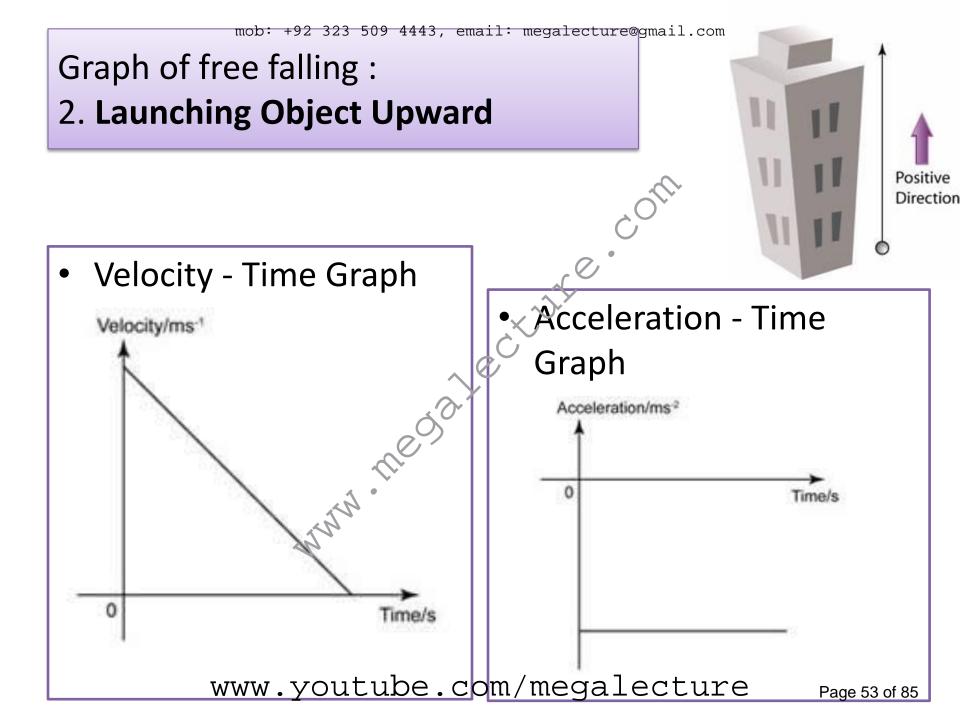
• The actual explanation of why all objects accelerate at the same rate involves the concepts of force and mass.



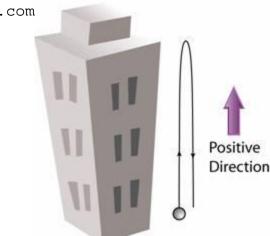
Graph of free falling : **1. Dropping an object from high place**

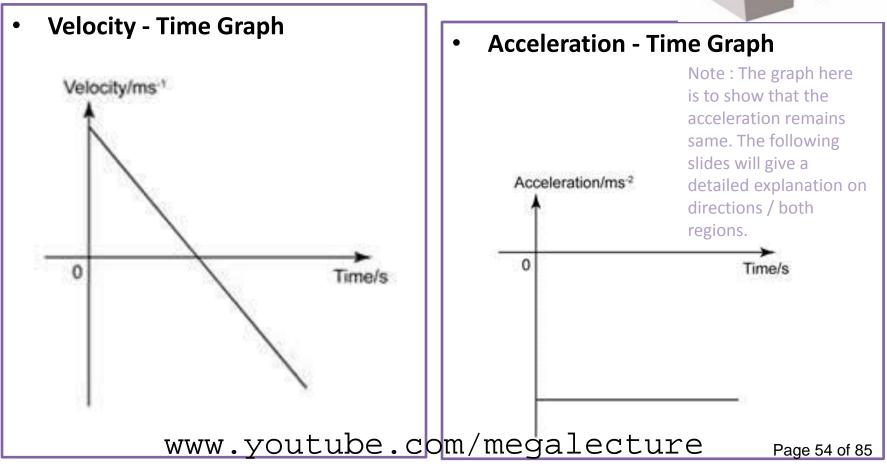


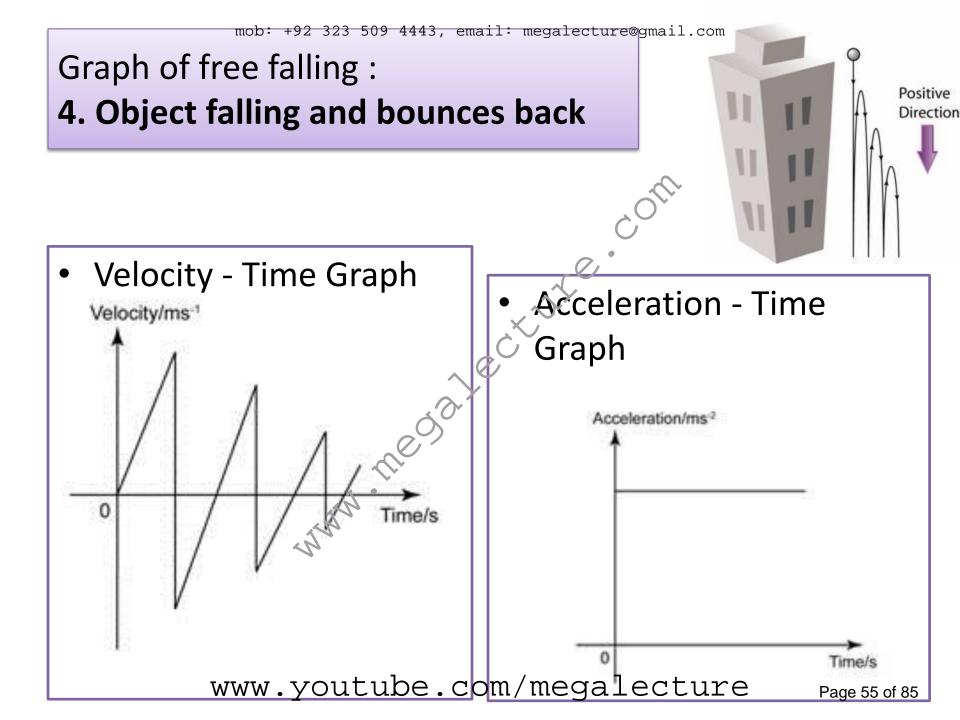


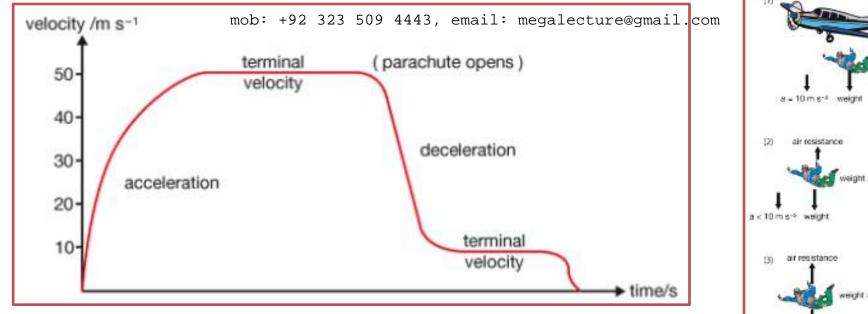


Graph of free falling : **3 . Object moving upward and fall back to the ground**



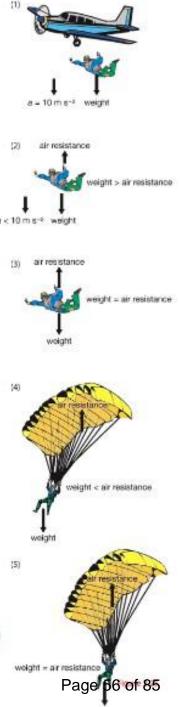






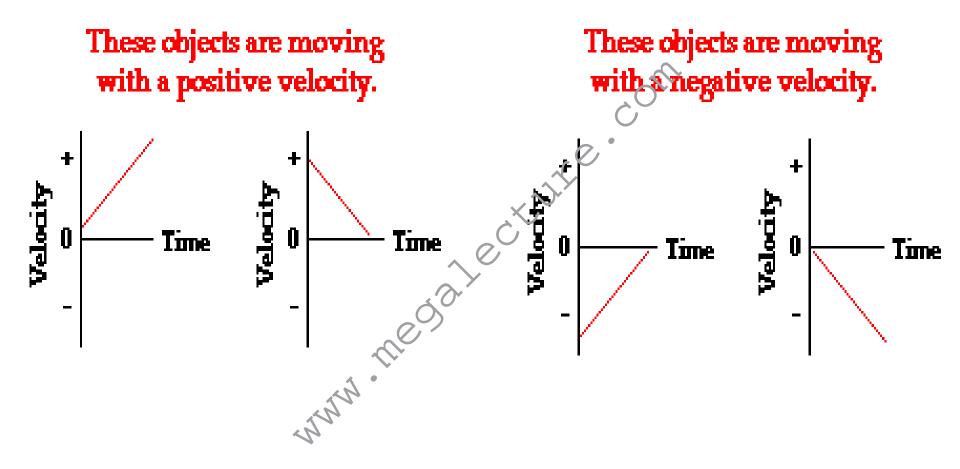
At the point when the air resistance equals to the weight, there is no acceleration and the object will fall with "terminal velocity".

A small dense object, like a steel ball bearing, has a high terminal velocity. A light object, like a raindrop, or an object with large surface area like a piece of paper, has a low terminal velocity.

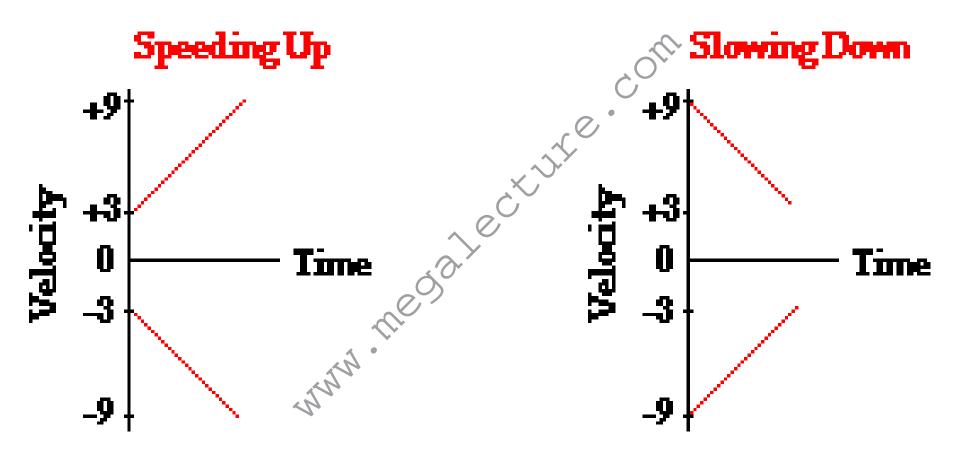


- How can one tell whether the object is moving in the positive direction (i.e., positive velocity) or in the negative direction (i.e., negative velocity)?
- And how can one tell if the object is speeding up or slowing down?

- Since the graph is a velocity-time graph, the velocity would be positive whenever the line lies in the positive region (above the x-axis) of the graph.
- Similarly, the velocity would be negative whenever the line lies in the negative region (below the x-axis) of the graph.
- A **positive velocity** means the object is moving in the positive direction; and a **negative velocity** means the object is moving in the negative direction.
- So one knows an object is moving in the positive direction if the line is located in the positive region of the graph (whether it is sloping up or sloping down). And one knows that an object is moving in the negative direction if the line is located in the negative region of the graph (whether it is sloping up or sloping down).
- And finally, if a line crosses over the x-axis from the positive region to the negative region of the graph (or vice versa), then the object has changed directions.



- Now how can one tell if the object is speeding up or slowing down?
- Speeding up means that the magnitude of the velocity is getting large. For instance, an object with a velocity changing from +3 m/s to + 9 m/s is speeding up. Similarly, an object with a velocity changing from -3 m/s to -9 m/s is also speeding up.
- In each case, the magnitude of the velocity is increasing; the speed is getting bigger.
- Given this fact, one would believe that an object is speeding up if the line on a velocity-time graph is changing from near the 0-velocity point to a location further away from the 0-velocity point. That is, if the line is getting further away from the x-axis (the 0-velocity point), then the object is speeding up. And conversely, if the line is approaching the x-axis, then the object is slowing down.



Equations of Motion mob: +92 323 509 4443, email: megalecture@gmail.com

There are 4 equations that you can use whenever an object moves with <u>constant, uniform acceleration in a straight line</u>. The equations are written in terms of the 5 symbols in the box:

s = displacement (m)

```
u = initial velocity (ms<sup>-1</sup>)
```

- v = final velocity (ms⁻¹)
- a = constant acceleration (ms⁻²)
- t = time interval (s)

Since a = (v - u) / t323 509 4443, email: megalecture@gmail.com

v = u + at ... (1)

If acceleration is constant, the average velocity during the motion will be half way between v and u. This is equal to 1/2(u + v). cture

 $\frac{1}{2}(u + v) = s/t$

<u>s = ½(u + v)t ... (2)</u>

Using equation (1) to replace v in equation (2):

$$s = \frac{1}{2}(u + u + at)t$$

 $s = \frac{1}{2}(2u + at)t$
 $s = ut + \frac{1}{2}at^{2} ... (3)$

From equation (1), t = (v - u)/a: megalecture@gmail.com Using this to replace t in equation (2): $s = \frac{1}{2}(u + v)[(v - u)/a]$ 2as = (u + v) (v - u) $2as = v^2 - u^2$ $v^2 = u^2 + 2as$... (4)

Note:

- You can only use these equations only if the acceleration is constant.
- Notice that each equation contains only 4 of our 5 "s, u, v, a, t" variables. So if know any 3 of the variables, we can use these equations to find the other regalecture Page 64 of 85

A cheetah starts from rest and accelerates at 2.0 ms⁻² due east for 10 s. Calculate (a) the cheetah's final velocity, (b) the distance the cheetah covers in this 10 s.

Solution:

(a) Using equation (1): v = u + at

 $v = 0 + (2.0 \text{ ms}^{-2} \times 10 \text{ s}) = 20 \text{ ms}^{-1} \text{ due east}$ (b) Using equation (2): $s = \frac{1}{2}(u + v)t$

s = ½(0+20 ms⁻¹) x 10 s = 100 m due east

You could also find the displacement by plotting a velocity-time graph for this motion. The magnitude of the displacement is equal to the area under the graph.

An athlete accelerates out of her blocks at 5.0 ms⁻². (a) How long does it take her to run the first 10 m? (b) What is her velocity at this point?

Solution:

```
(a) Using equation (3): s = ut + \frac{1}{2}at^2
                              10 \text{ m} = 0 + (1/2 \text{ x} 5.0 \text{ ms}^{-2} \text{ x} \text{ t}^2)
                                   t^2 = 4.0 s^2
                                         t = 2.0 s
(b) Using equation (1): v = u + at
                                   v = 0 + (5.0 \text{ ms}^{-2} \text{ x} 2.0 \text{ s})
                                        v = 10 \text{ ms}^{-1}
```

A bicycle's brakes can produce a deceleration of 2.5 ms⁻². How far will the bicycle travel before stopping, if it is moving at 10 ms⁻¹ when the brakes are applied?

Solution:

 $- u^{2} + 2as$ $0 = (10 \text{ ms}^{-1})^{2} + (2 \text{ x} (-2.5 \text{ ms}^{-2}) \text{ x} \text{ s})$ $0 = 100 \text{ m}^{2}\text{s}^{-2} + (5.0 \text{ ms}^{-2} \text{ x} \text{ s})$ $s = 20 \text{ m}^{-1}$ Using equation (4): $v^2 = u^2 + 2as$

A student flips a coin into the air. Its initial velocity is 8.0 ms⁻¹. Taking g = 10 ms⁻² and ignoring air resistance, calculate: (a) the maximum height, h, the coin reaches, (b) the velocity of the coin on returning to his hand, (c) the time that the coin is in the air.

Solution: (upward motion to be negative)

```
(a) v^2 = u^2 + 2as

0 = (8.0 \text{ ms}^{-1})^2 + (2 \text{ x} (-10 \text{ ms}^{-2}) \text{ x} \text{ h})

h = 3.2 \text{ m}
```

(b) The acceleration is the same going up and coming down. If the coin decelerates from 8.0 ms⁻¹ to 0 ms⁻¹ on the way up, it will accelerate from 0 ms⁻¹ to 8 ms⁻¹ on the way down. The motion is symmetrical. So the velocity on returning to his hand is 8.0 ms⁻¹ downwards.

```
(c) v = u + at
0 = 8.0 ms<sup>-1</sup> + (-10 ms<sup>-2</sup> x t)
t = 0.8 s
```

The coin will take the same time between moving up and coming down. So total time in the air = 1.89. YOUTUBE.COM/megalecture Page 68 of 85

You-tube videos links with explanation on : Newtonian Mechanism - Kinematics

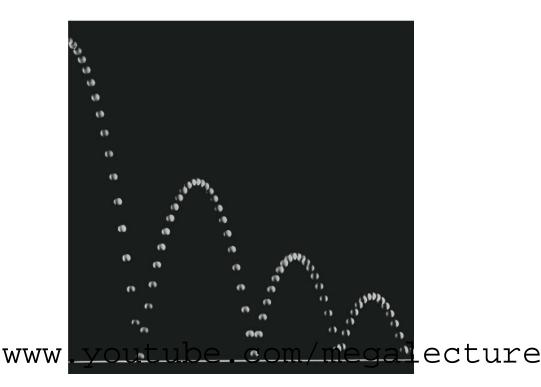
- <u>http://www.youtube.com/watch?v=go9uekKO</u>
 <u>cKM</u>
- <u>http://www.youtube.com/watch?v=xE71aKXjs</u>
 <u>s0&feature=related</u>

Last sub topic of Chapter 3

The projectile Motion

3. Kinematics

(k) describe and explain motion due to a uniform velocity in one direction and a uniform acceleration in a perpendicular direction.



PROJECTILE is a body which is thrown horizontally or at an angle relative to the horizontal which follows a curved path called trajectory.

A projectile is an object moving in two dimensions under the influence of Earth's gravity; its path is a parabola

Examples: Ball being thrown, water coming out of the hose, a bullet fired from a gun, arrow shot from a bow, fountains.

What is projectile motion?

*Made up of horizontal and vertical components

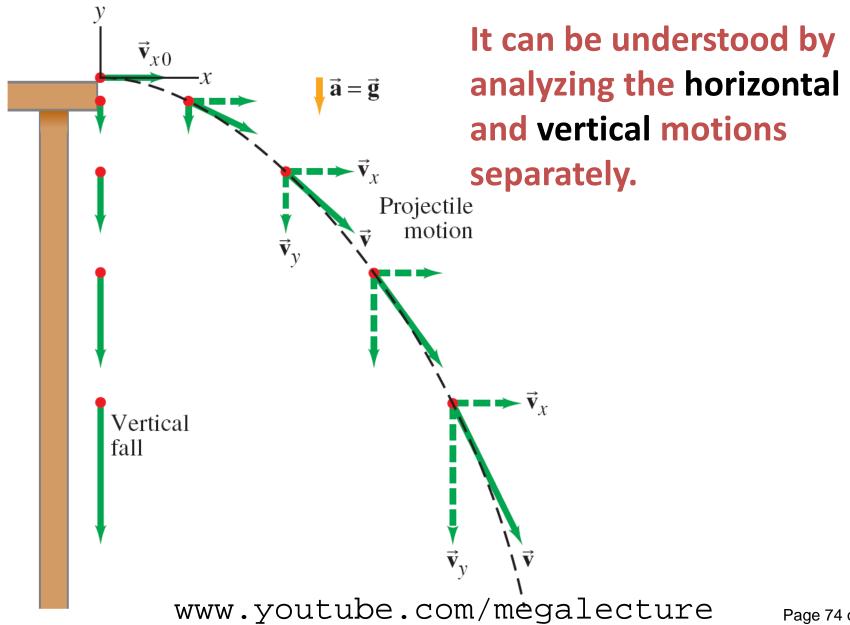
*Movement wherein an object is acted upon by gravity and air resistance

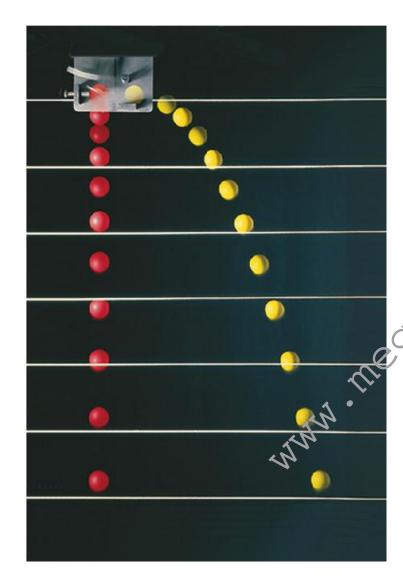
*Motion of a body following a curved path

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The speed in the *x*-direction is constant; in the *y*-direction the object moves with constant acceleration *g*.

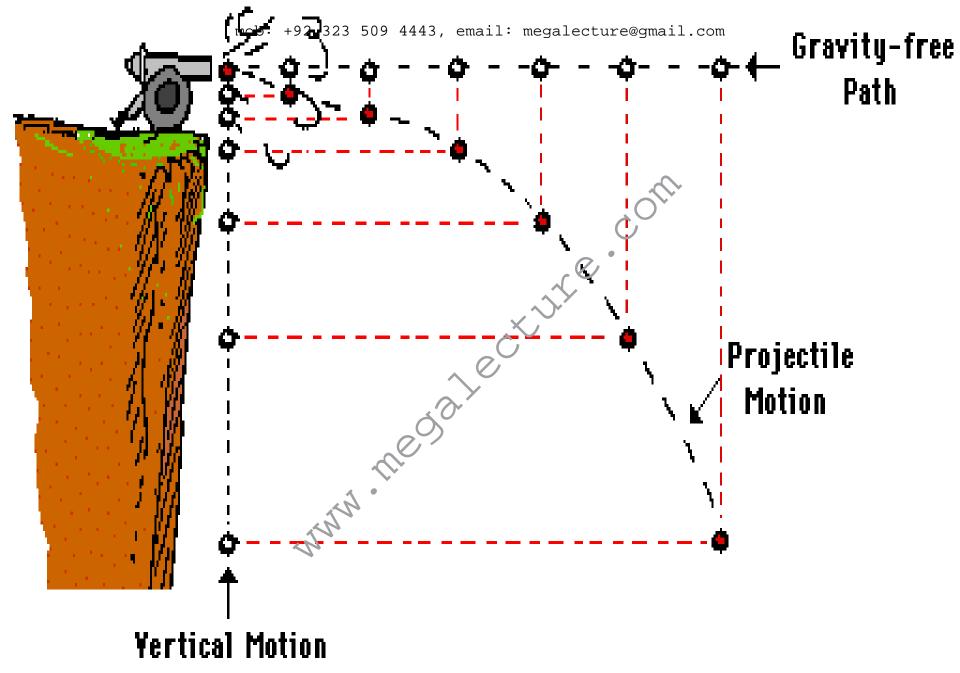
This photograph shows two balls that start to fall at the same time. The one on the right has an initial speed in the *x*-direction. It can be seen that vertical positions of the two balls are identical at identical times, while the horizontal position of the yellow ball increases linearly.

REMEMBER:

1. The horizontal velocity of a projectile is <u>constant</u> (never changing in value),

2. There is uniform vertical acceleration <u>caused by</u> <u>gravity</u>; its value is 9.8 m/s²

3. The vertical velocity of a projectile changes by ~10 m/s each second,
the horizontal motion of a projectile is <u>independent</u> of its vertical motion.



PROJECTILE I

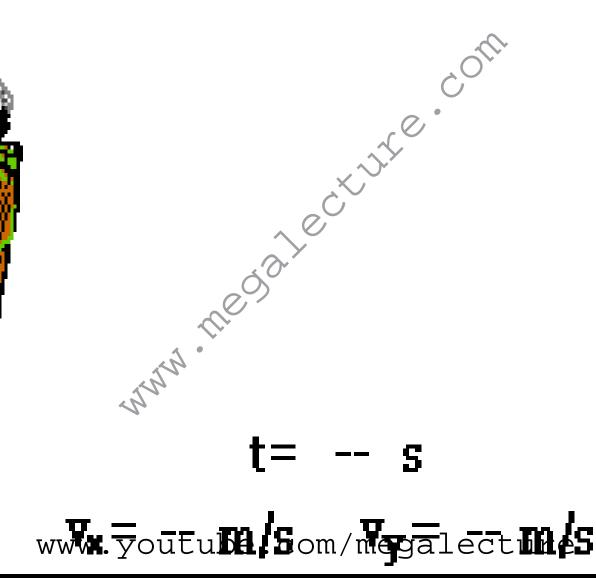
(SIMPLE PROJECTILE)



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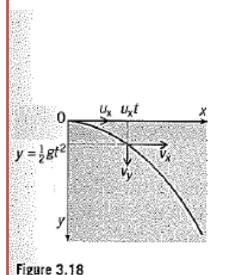
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*All vertical components have y subscripts :
vy, dy, ty,
*All horizontal components have x subscripts:
vx, dx

RANGE is the horizontal displacement of the projectile (dx)

MAXIMUM HEIGHT is the vertical displacement of the projectile (dy)

How to calculate – Projectile Motion (From your reference book)

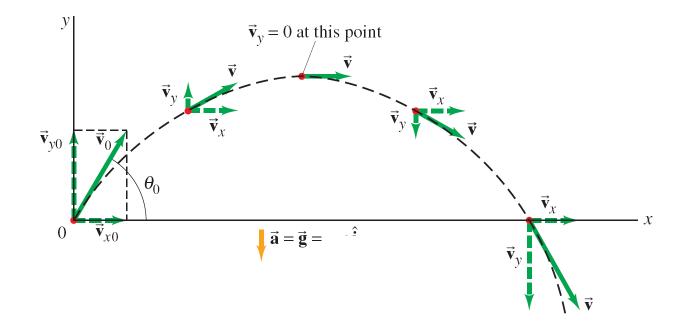


This topic is often called **projectile motion**. Galileo first gave an accurate analysis of this motion. He did so by splitting the motion up into its vertical and horizontal components, and considering these separately. The key is that the two components can be considered independently.

As an example, think about a particle sent off in a horizontal direction and subject to a vertical gravitational force (its weight). As before, air resistance will be neglected. We will analyse the motion in terms of the horizontal and vertical components of velocity. The particle is projected at time t = 0 at the origin of a system of x, y ∞ -ordinates (Figure 3.18) with velocity u_x in the x-direction. Think first about the particle's vertical motion (in the y-direction). Throughout the motion, it has an acceleration of g (the acceleration of free fall) in the y-direction. The initial value of the vertical component of velocity is $u_y = 0$. The vertical component increases continuously under the uniform acceleration g. Using v = u + at, its value v_y at time t is given by $v_y = gt$. Also at time t, the vertical displacement y downwards is given by $y = \frac{1}{2}gt^2$. Now for the horizontal motion (in the x-direction): here the acceleration is zero, so the horizontal component of velocity remains constant at u_x . At time t the horizontal displacement x is given by $x = u_x t$. To find the velocity of the particle at any time t, the two components v_x and v_y must be added vectorially. The direction of the resultant vector is the direction of motion of the particle. The curve traced out by a particle subject to a constant force in one direction is a parabola.

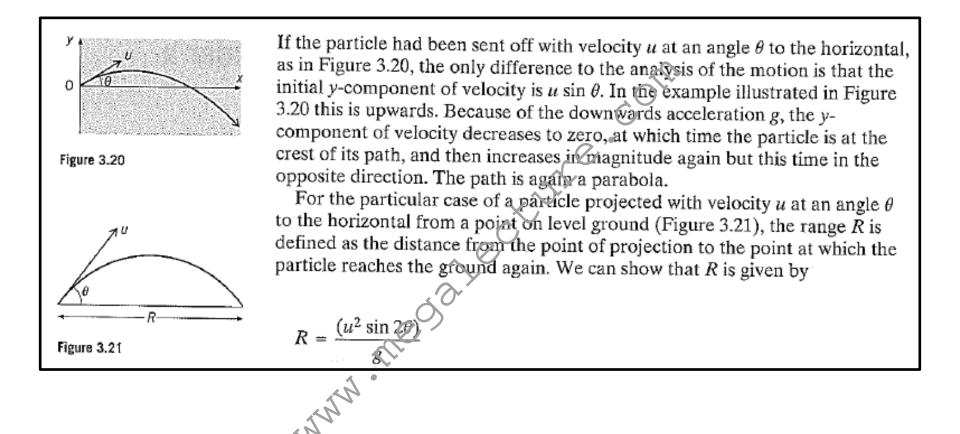
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If an object is launched at an initial angle of ϑ_0 with the horizontal, the analysis is similar except that the initial velocity has a vertical component.



Path of a projectile fired with initial velocity v_0 at angle θ_0 to the horizontal. Path is shown dashed in black, the velocity vectors are green arrows, and velocity components are dashed. The acceleration a = dv/dt is downward. That is, a = g. WWW.YOUTUBE.COM/megalecture Page 82 of 85 nob. +92 323 509 4443, email. megalecture@gmail.com

(Not in syllabus, only for your info)



Sample Problem – Projectile Motion

A stone is thrown from the top of a vertical cliff, 45 m high above level ground, with an initial velocity of $15 \text{ m} \text{ s}^{-1}$ in a horizontal direction (Figure 3.22). How long does it take to reach the ground? How far from the base of the cliff is it when it reaches the ground?

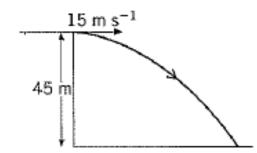


Figure 3.22

To find the time t for which the stone is in the air, work with the vertical component of the motion, for which we know that the initial component of velocity is zero, the displacement y = 45 m, and the acceleration a is 9.81 m s⁻². The equation linking these is $y = \frac{1}{2}gt^2$. Substituting the values, we have $45 = \frac{1}{2} \times 9.81t^2$. This gives $t = \sqrt{(2 \times 45/9.81)} = 3.0$ s.

For the second part of the question, we need to find the horizontal distance x travelled in the time t. Because the horizontal component of the motion is not accelerating, x is given simply by $x = u_x t$. Substituting the values we have $E = \frac{15}{m^2} = \frac{41}{2}$

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Any Questions?

